
ストレンジネスを持つ原子核

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 - $\Lambda\Lambda$ ハイパー核
5. $K^{\bar{b}ar}$ 中間子原子核

J-PARC (Japan Proton Accelerator Research Complex)

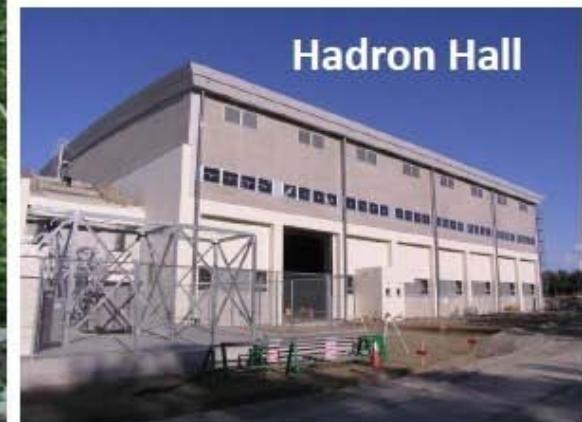


J-PARC 施設配置図(<http://i-parc.jp/>より)



ハドロン実験ホール
K1.8ビームライン
2009/5/12現在

大強度陽子加速器施設
茨城県那珂郡東海村
(2008-)



Hadron Hall



Proposed experiments for SNP @J-PARC

S = -2

- E03: Measurement of X rays from Ξ^- atom /K. Tanida (Kyoto)
- E05: Spectroscopic study of Ξ -hypernucleus, $^{12}\Xi\text{Be}$, via the $^{12}\text{C}(\text{K}^-, \text{K}^+)$ reaction /T. Nagae (Kyoto) [Day 1]
- E07: Systematic study of **double strangeness system** with an emulsion-counter hybrid method/K. Imai (Kyoto), K. Nakazawa (Gifu), H. Tamura (Tohoku)

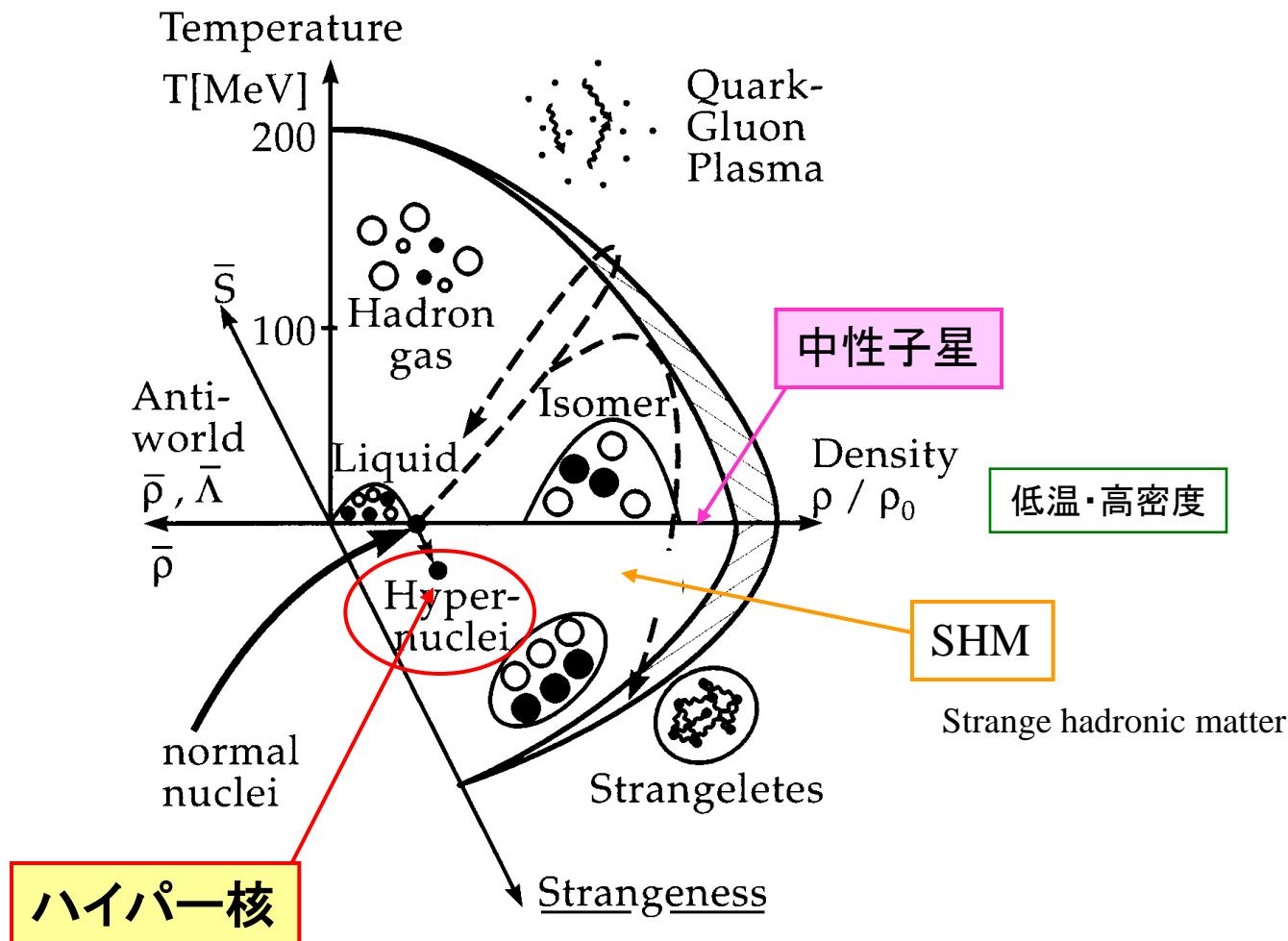
S = -1

- E10: Production of **neutron-rich Lambda-hypernuclei** with the double charge exchange reaction /A. Sakaguchi (Osaka), T. Fukuda (Osaka E. -C.)
- E13: **Gamma-ray spectroscopy** of light hypernuclei/H. Tamura (Tohoku) [Day 1]
- E15: A search for **deeply-bound kaonic nuclear states** by in-flight $^3\text{He}(\text{K}^-, \text{n})$ reaction/M. Iwasaki (RIKEN), T. Nagae (Kyoto) [Day 1]
- E17: Precision spectroscopy of **kaonic ^3He 3d \rightarrow 2p X-rays** /R. S. Hayano (Tokyo), H. Outa (RIKEN) [Day 1]
- E18: Coincidence measurement of the weak decay of $^{12}\Lambda\text{C}$ and the **three-body weak interaction process**/H. C. Bhang (Seoul), H. Outa (RIKEN), H. Park (KRISS)
- E22: Exclusive study on the **ΛN weak interaction** in $A=4$ Λ -Hypernuclei/S. Ajimura (Osaka), A. Sakaguchi (Osaka)
- E23: Search for a **nuclear Kbar bound state K^-pp** in the $d(\pi^+, \text{K}^+)$ reaction/T. Nagae (Kyoto)

ハドロン物質の相図

高温・低密度

By C.Greiner, J. Schaffner-Bielich

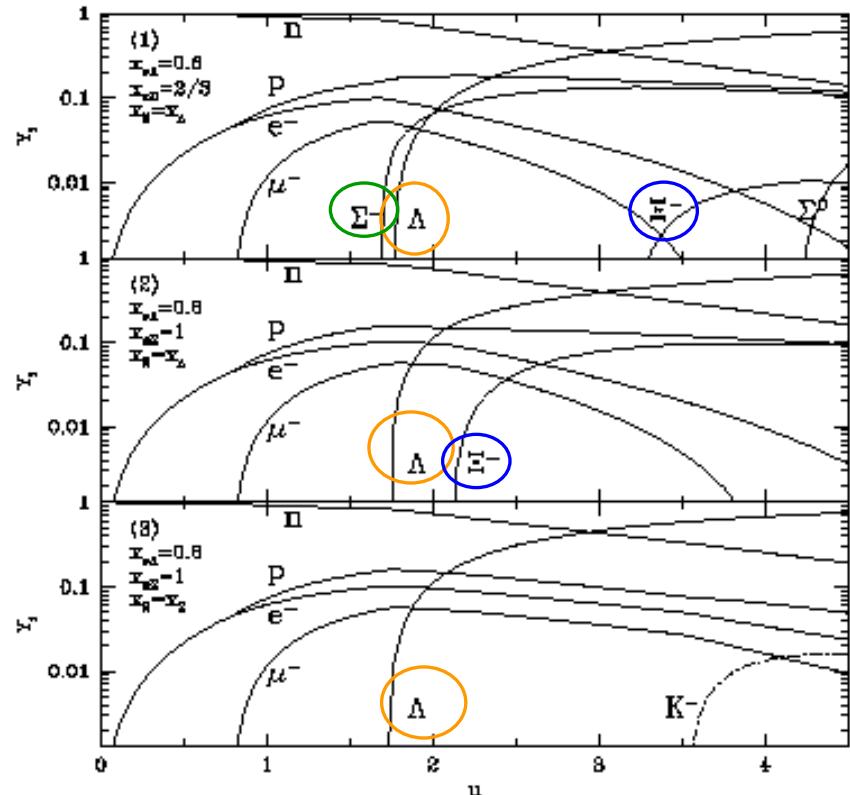


Neutron star core

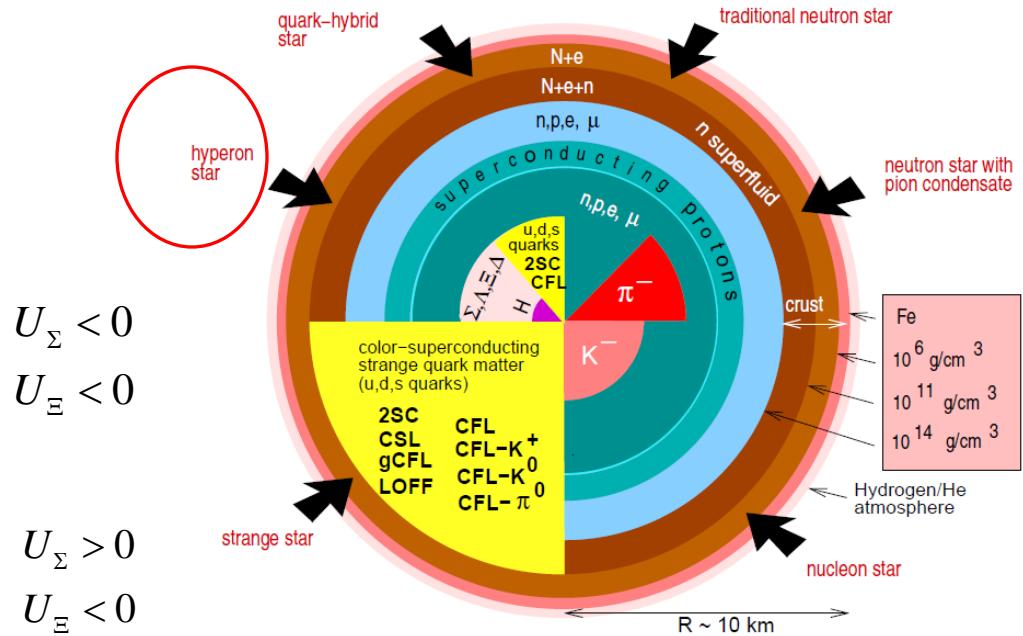
“An interesting neutron-rich hypernuclear system”

Hyperon-mixing

Coupling constant ratio; $x_{iY} = g_{iY}/g_{iN}$ ($i = \sigma, \omega, \rho$)

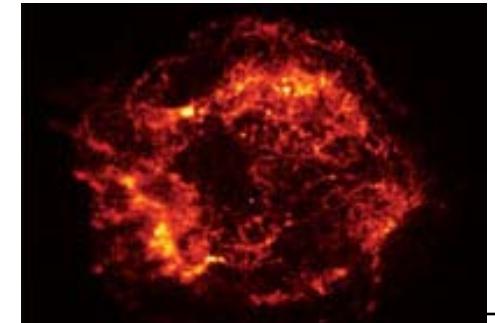


R. Knorren, M. Prakash, P.J.Ellis, PRC52(1995)3470



F. Weber, Prog. Part. Nucl. Phys. 54 (2005) 193

$$U_\Sigma > 0 \\ U_\Xi > 0$$



Cassiopeia A nebula
NASA/CXC/SAO.

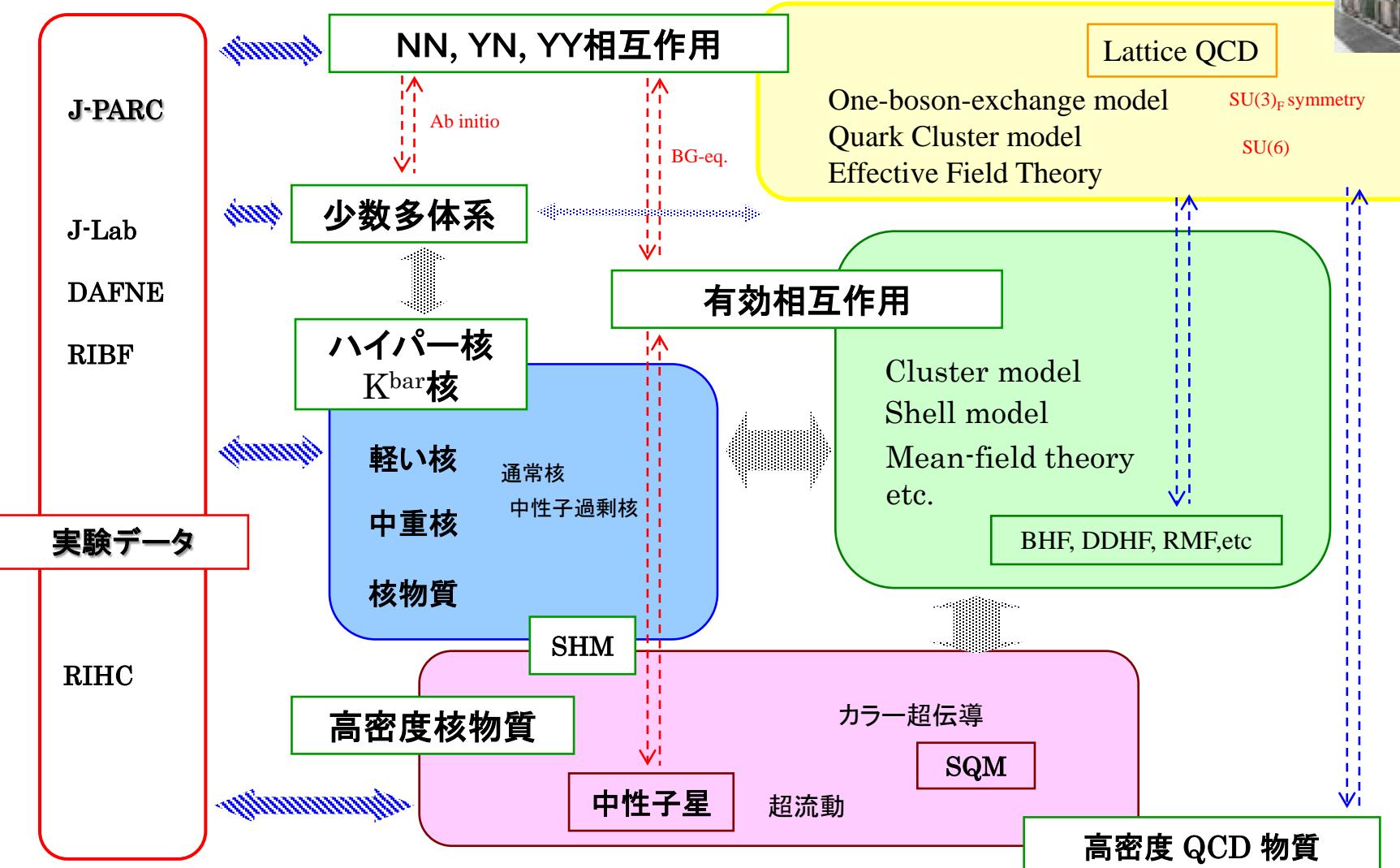
ストレンジネス核物理

- ストレンジネスは原子核深部を探るプローブ
 - ハイペロンはパウリ排他律を受けない
- Impurity Physics
 - “糊”としての役割
 - 原子核構造の変化
 - 媒質中のハドロンの性質
- “*Hyperon-mixing*”
で探る
- Baryon-Baryon Interaction
 - YN, YY Interaction based on $SU_f(3)$
 - 核力の統一的理解・斥力芯の起源
- Neutron Starの構造と進化
 - 高密度核物質の解明, EOS,

ストレンジネス核物理の展開

by E.Hiyama

“QCD,核力から核構造へ”と“核構造からQCD,核力へ”



2. $S = -1$ の原子核

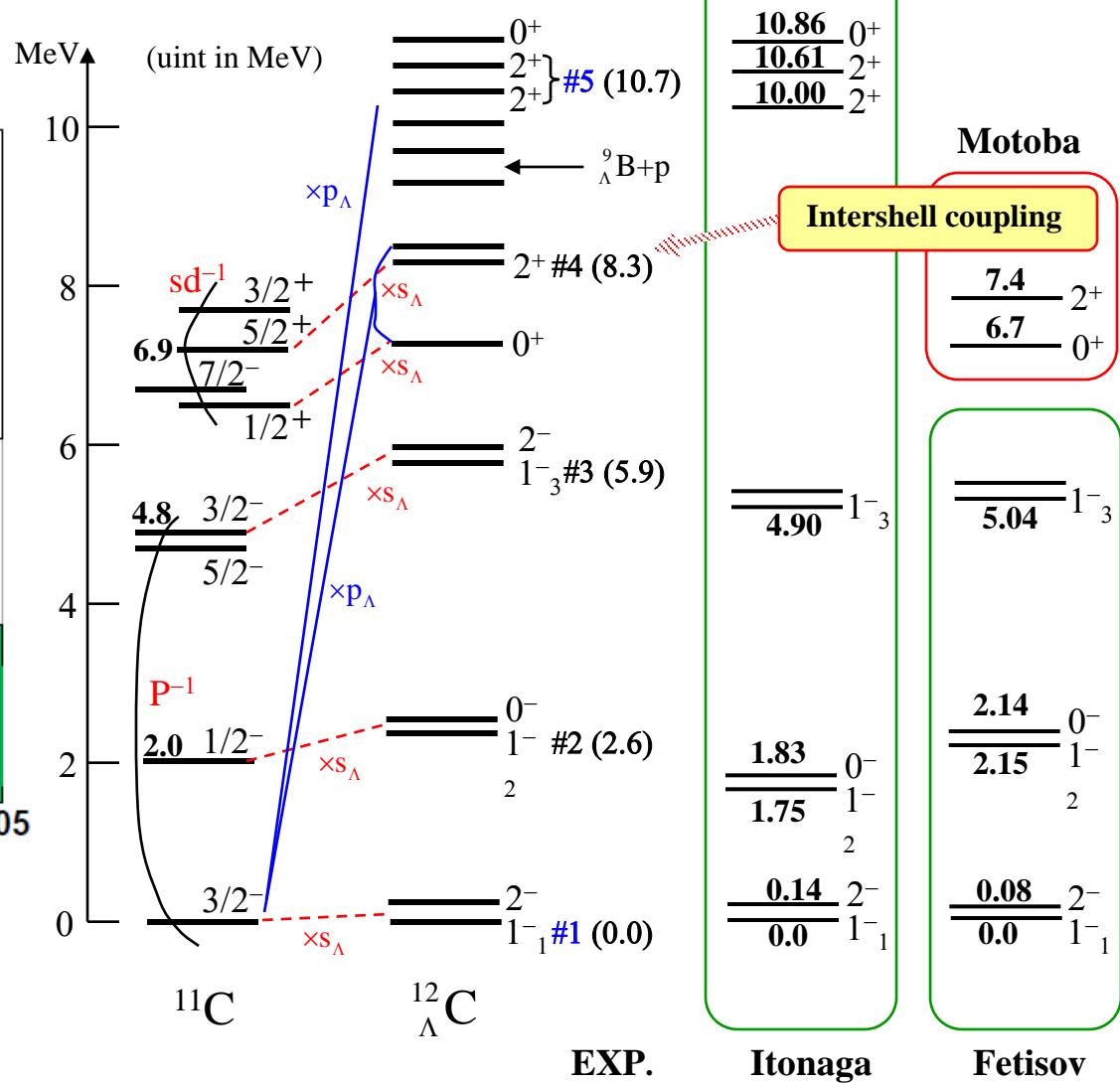
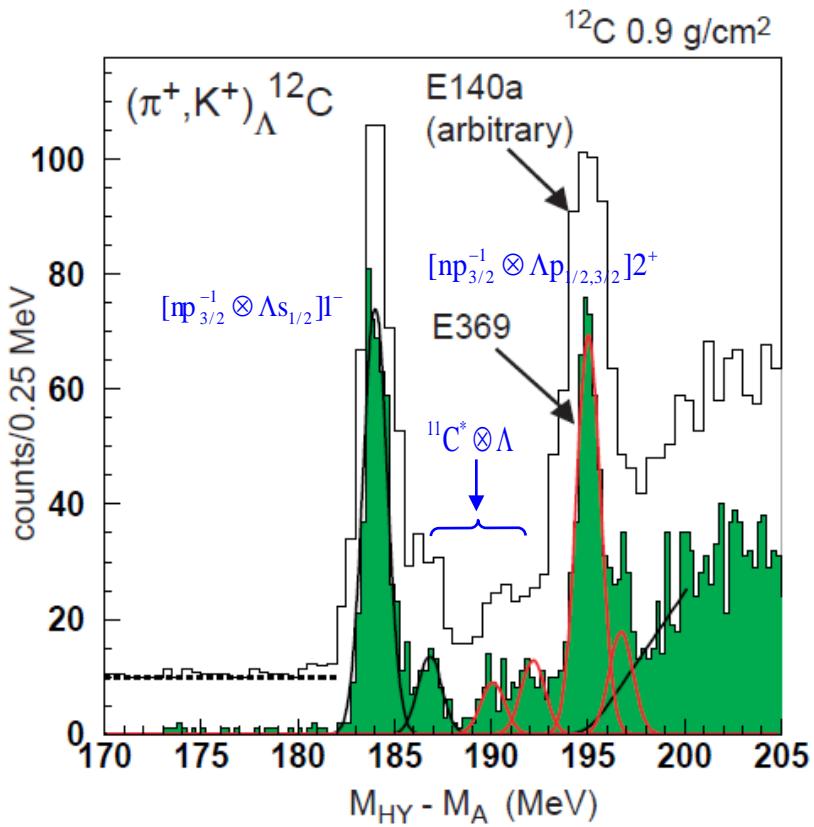
Λハイパー核

- (π^+, K^+) 反応によるハイパー核の生成
芯核の励起状態, ハイパー核らしい状態, etc.
- 核内 Λ 粒子の働き
- Gamma-ray spectroscopy of light hypernuclei
- Λ 粒子の 1 粒子ポテンシャルとスピン軌道力
- Overbinding Problem on s-Shell Hypernuclei
- 中性子過剰ハイパー核
- Λ ハイパー核の弱崩壊

$^{12}\text{C}(\pi^+, \text{K}^+)$ 反応実験 KEK-E369

ハイパー核の励起状態、芯核の励起状態を観測

H.Hochi et al., PRC64(2001)044302



K. Itonaga, et al., PTP.Supp.177(1997)17
 V.N.Fetisov, et al., Z.Phys.A339(1991)399
 T. Motoba, NPA639(1998)135c

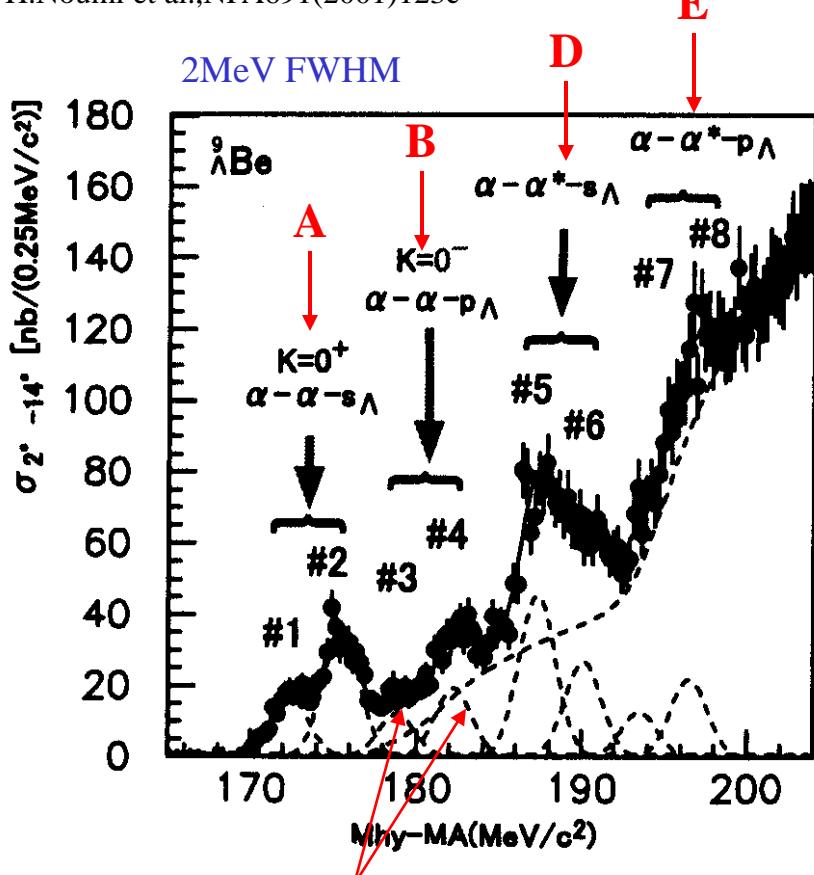
ハイパー核らしい状態の生成

対称性と集団性

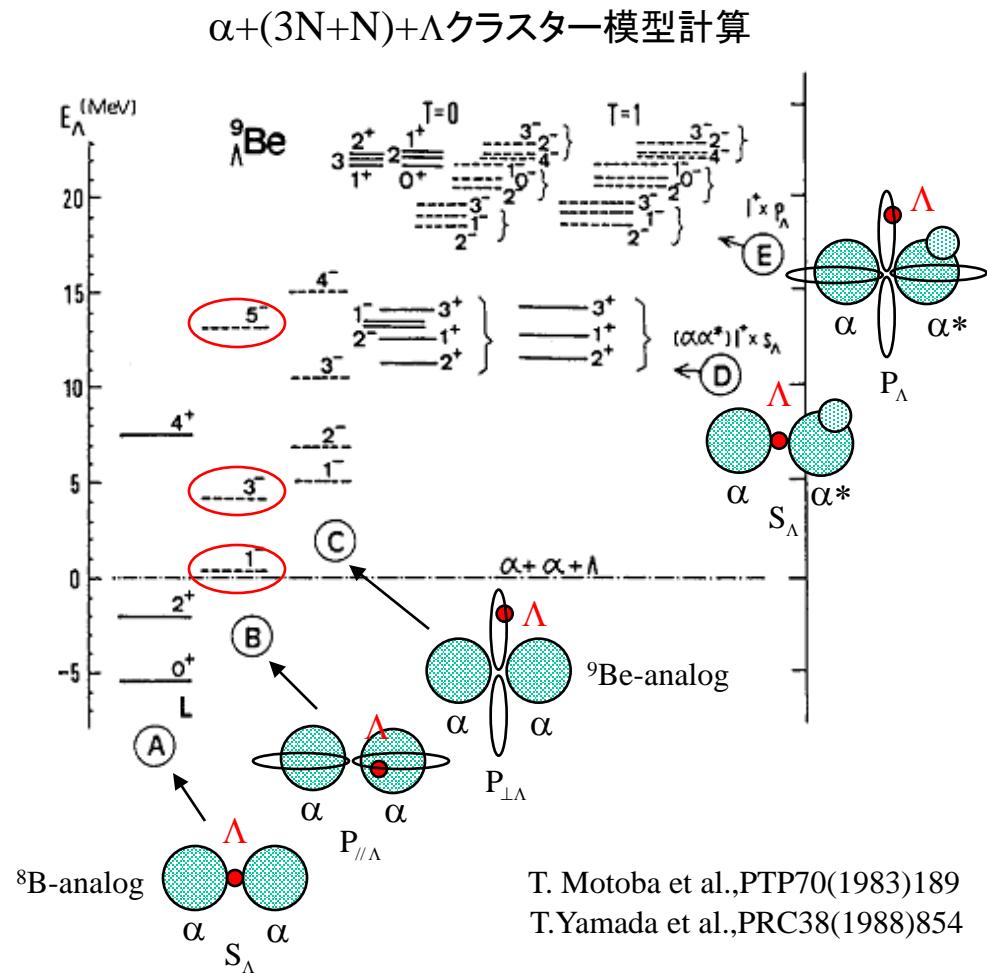
$${}^9\text{Be}(\pi^+, \text{K}^+) {}^9_\Lambda\text{Be}$$

High-resolution, high-statistics

H.Noumi et al., NPA691(2001)123c



“genuine hypernuclear states”



coupling of Λ to rotational bands

Role of the Λ -hyperon in nuclei

“gule”

T. Motoba, et al., PTP70(1983)189
E. Hiyama, et al., PRC59(1999)2351

➤ Shrinkage effects (19% for the ${}^6\text{Li}$ core)

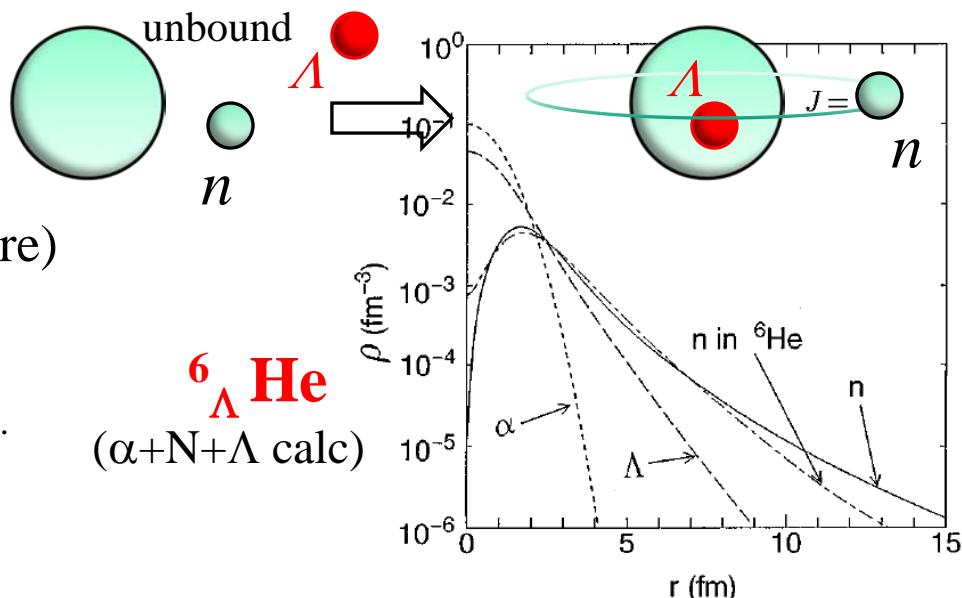
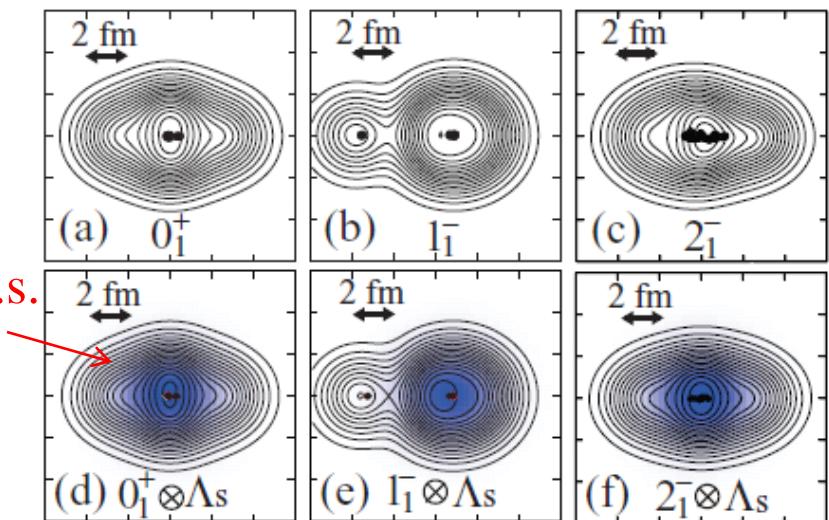
➤ neutron-skin or neutron halo

E. Hiyama, et al., PRC59(1999)2351
Tretyakova, Lanskoy, EPJ.A5(1999) 391.

“Stabilizing”

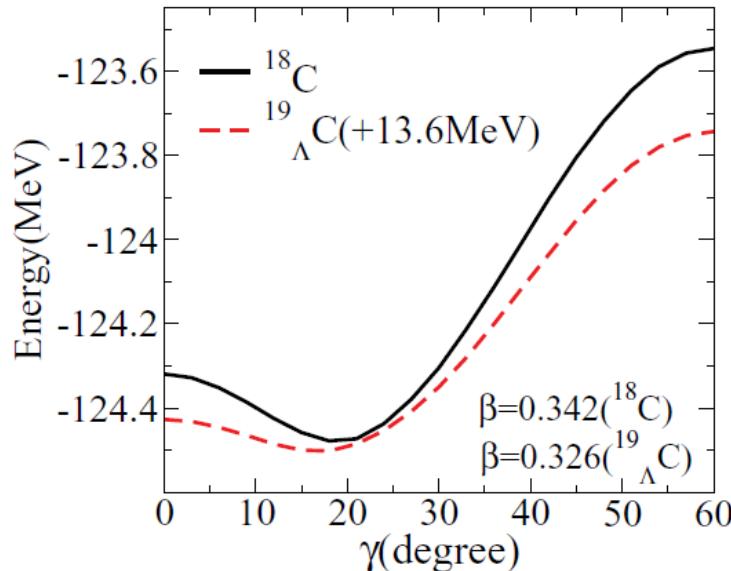
${}^{21}_{\Lambda}\text{Ne}$ (AMD calc)

M. Isaka et al, PRC83(2011)054304



${}^{19}_{\Lambda}\text{C}$ (CSHF+BCS calc)

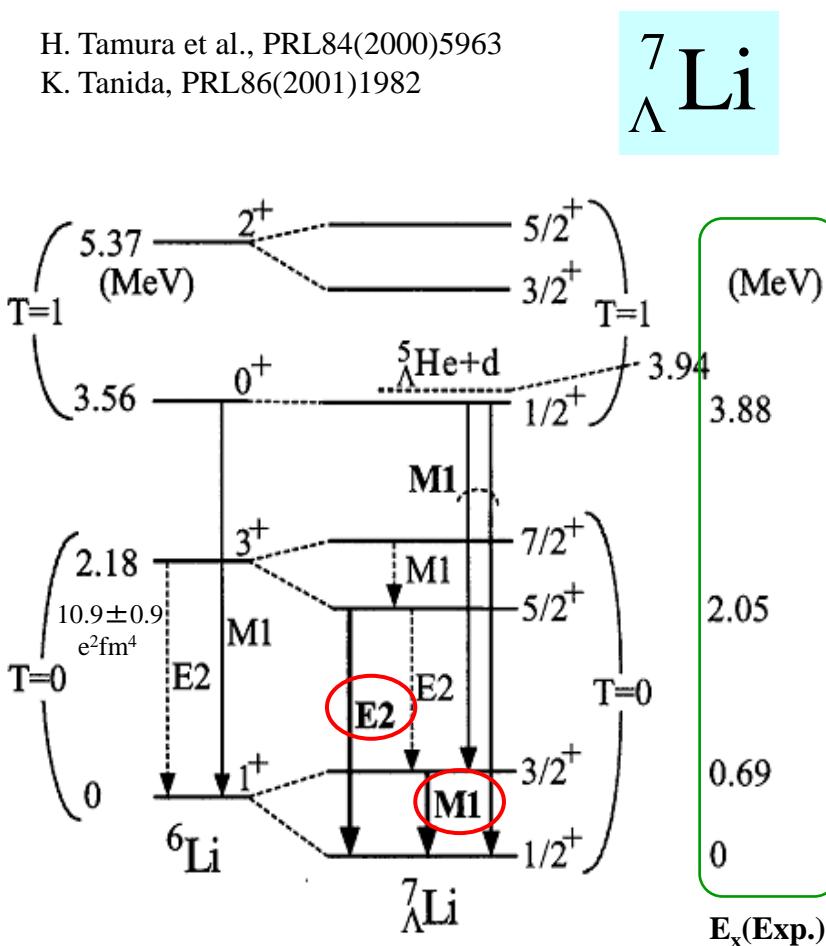
M.T. Win, K.Hagino et al, PRC83 (2011) 014301



精密 γ 線分光実験 KEK-E419

Ge detector resolution \sim a few keV

H. Tamura et al., PRL84(2000)5963
K. Tanida, PRL86(2001)1982



$$B(E2; 5/2^+ \rightarrow 1/2^+) = 3.6 \pm 0.5 e^2 \text{fm}^4 \text{ (Exp.)}$$

$8.6 e^2 \text{fm}^4$ (Shell Model)

$2.5 e^2 \text{fm}^4$ (Cluster Model)

Spin-flip M1 vs. ΛN spin-spin interaction

Shell Model

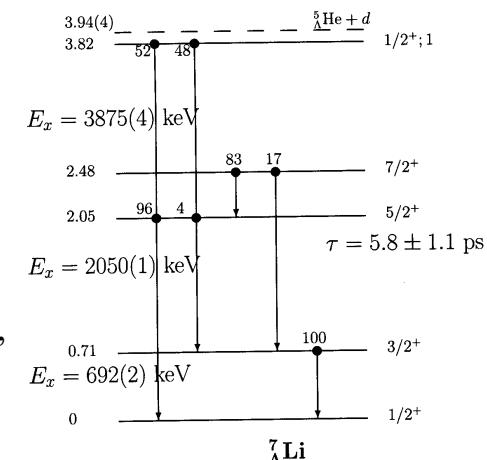
$\Delta = 0.50, S_\Lambda = -0.04, S_N = -0.47,$
 $T = 0.04$ (No $\Lambda\Sigma$ coupling)
[D.J.Millener, NPA691(2001)93c]

$$\Delta E(3/2^+ - 1/2^+) = 0.712 \text{ MeV}$$



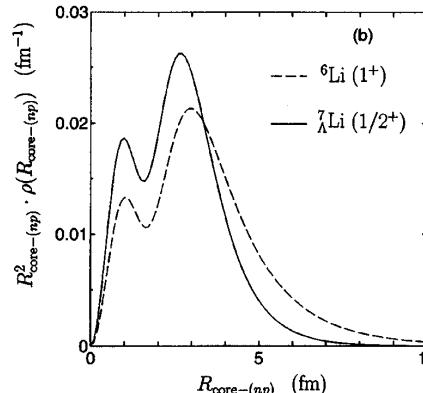
$\Delta = 0.43, S_\Lambda = -0.015, S_N = -0.39,$
 $T = 0.30$ ($\Lambda\Sigma$ coupling)
[D.J.Millener, NPA835(2010)11]

$$\Delta E(3/2^+ - 1/2^+) = 0.693 \text{ MeV}$$



$B(E2)$ vs. Shrinking effects

$$\frac{R_{c-d}({}^7\Lambda\text{Li})}{R_{\alpha-d}({}^6\text{Li})} = \left[\frac{B(E2; 5/2^+ \rightarrow 1/2^+)}{B(E2; 3^+ \rightarrow 1^+)} \right]^{1/4} \quad \begin{array}{ll} 0.81 \pm 0.04 & (\text{Exp}) \\ 0.84 & (\text{Motoba83}) \\ 0.78 & (\text{Hiyama99}) \end{array}$$

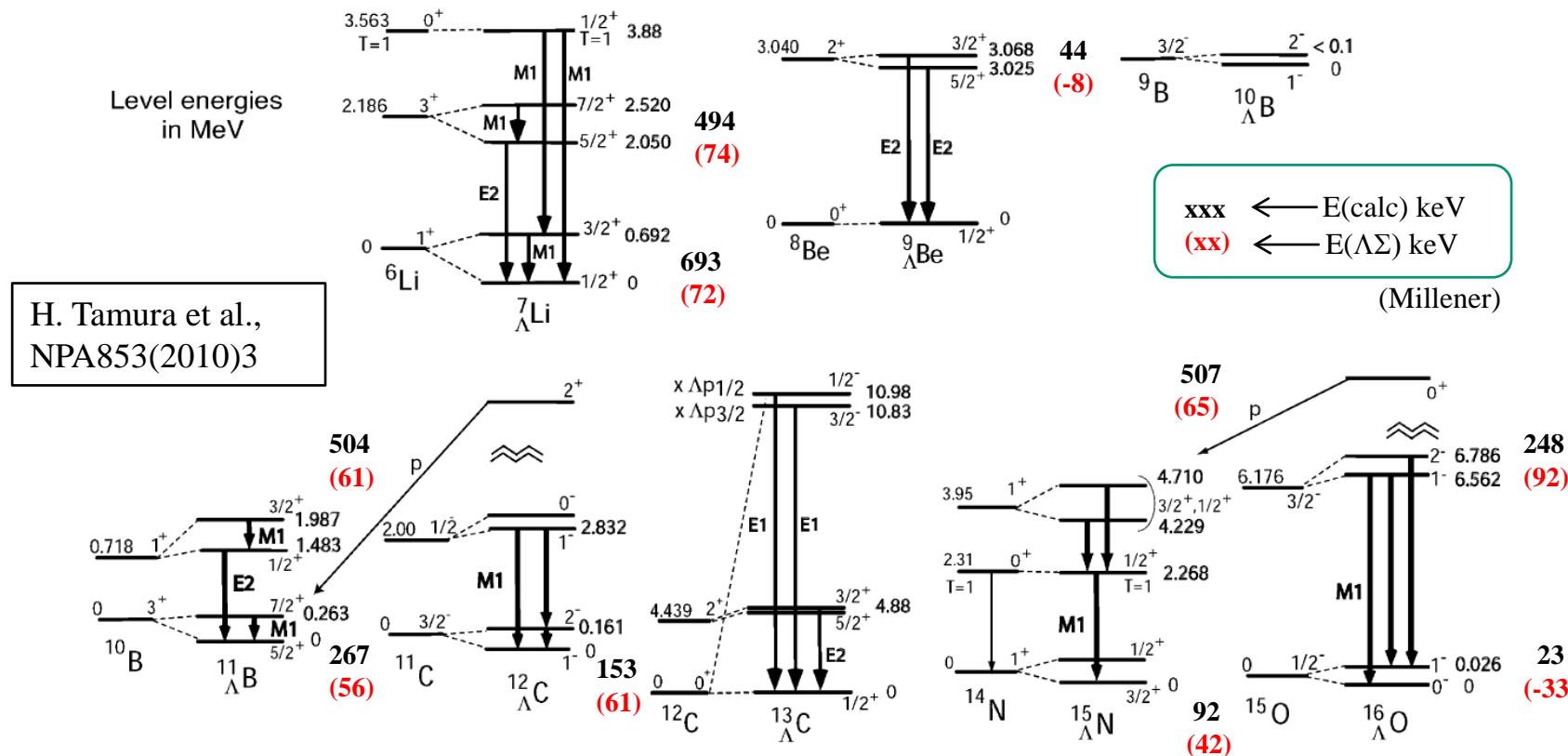


Shrinkage of the ${}^6\text{Li}$ core: 19% !

Cluster Model

T. Motoba, et al., PTP70(1983)189
E. Hiyama, et al., PRC59(1999)2351

Gamma-ray spectroscopy of light hypernuclei



Spin-dependence of the effective ΛN interaction

[R.H.Dalitz, A.Gal, AnnPhys.116(1978)167]

$$V_{\Lambda N} = \bar{V} + \Delta \vec{s}_N \cdot \vec{s}_A + S_A \vec{l}_N \cdot \vec{s}_A + S_N \vec{l}_N \cdot \vec{s}_N + T S_{12}$$

$$A = 7,9 \quad \Delta = 430, \quad S_A = -15, \quad S_N = -390 \quad T = 30 \text{ (keV)}$$

$$A > 9 \quad \Delta = 330, \quad S_A = -15, \quad S_N = -350, \quad T = 23.9 \text{ (keV)}$$

Microscopic Shell-Model

including ΛN - ΣN coupling effects

[D.J.Millener,NPA835(2010)11]



E13@J-PARC

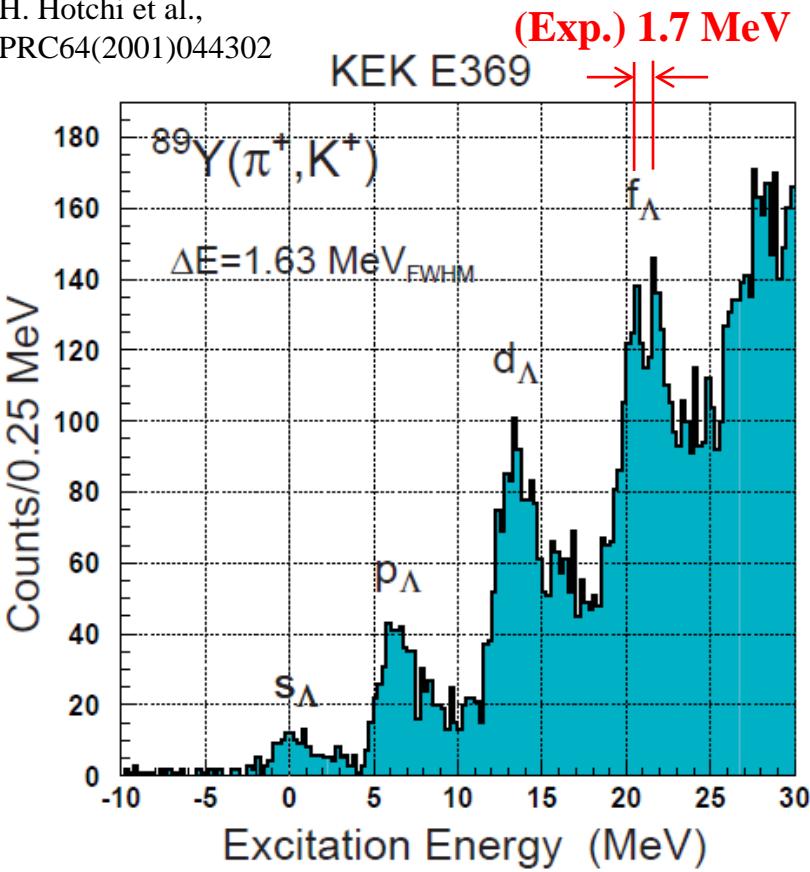
- ΛN spin-dependent force/ ΛN - ΣN coupling force/Charge symmetry breaking ($\Lambda p \neq \Lambda n$)
- Magnetic moments μ_Λ in a nucleus from B(M1)

${}^4_\Lambda He$, ${}^{10}_\Lambda B$, ${}^{11}_\Lambda B$, ${}^{19}_\Lambda F$

最近の梅谷らの計算に期待

Λ s.p. structure and Λ spin-orbit splitting in $^{89}\Lambda\text{Y}$

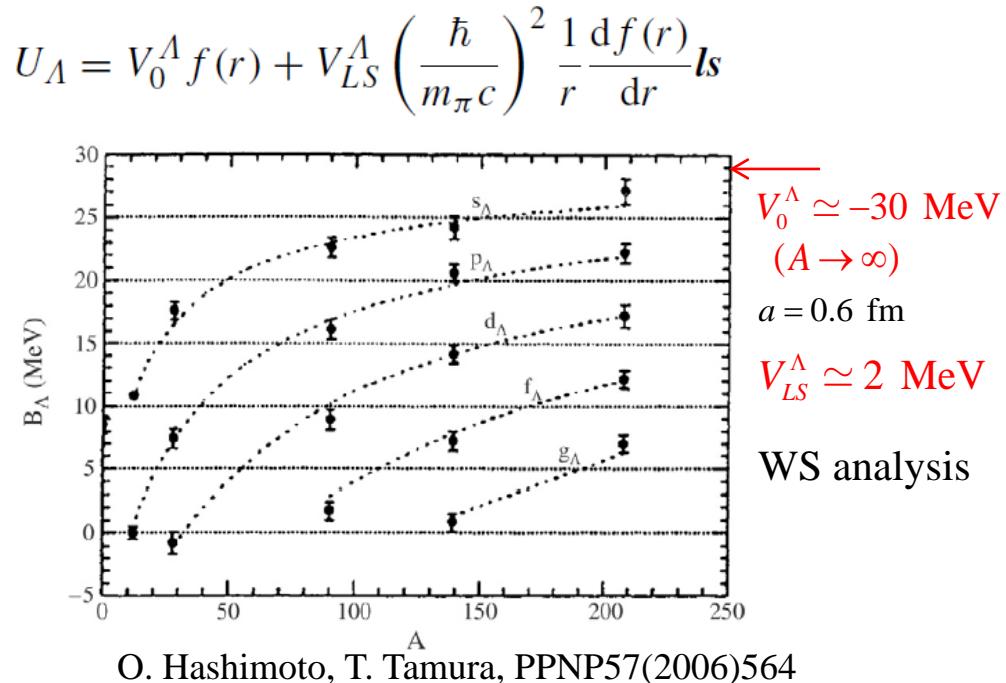
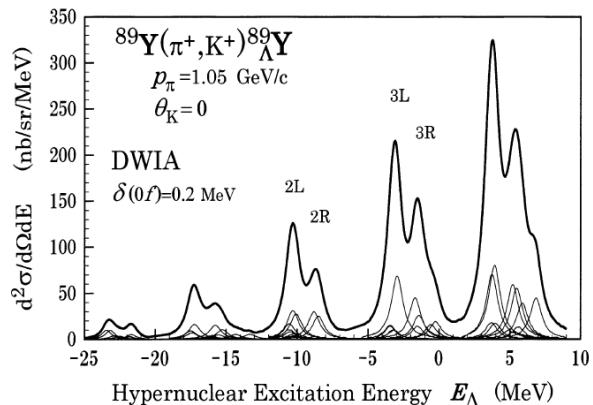
H. Hotchi et al.,
PRC64(2001)044302



T. Motoba et al.,
PTPS185(2010)197

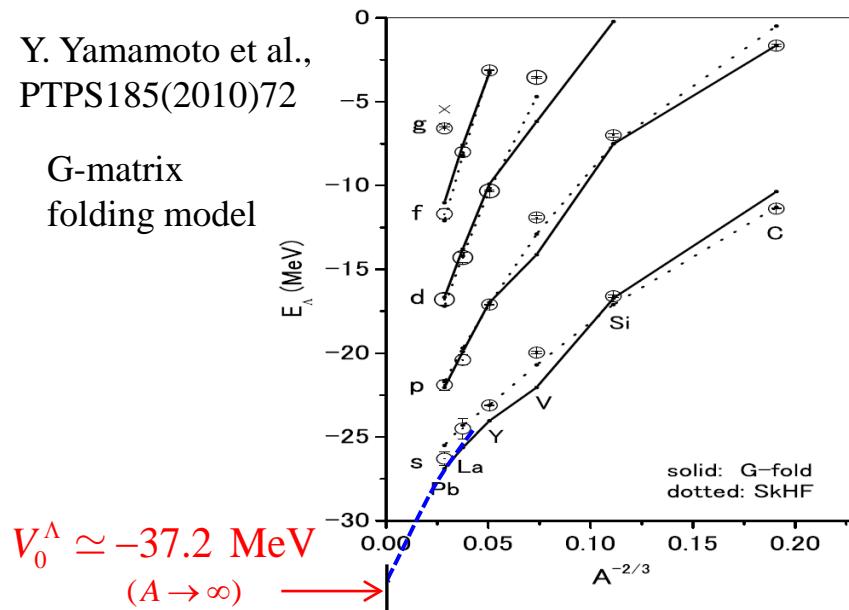
SM analysis
➤ ΛN^{-1} particle-hole ex.
➤ inter-shell coupling

$$V_{LS}^\Lambda \simeq 0.2 \text{ MeV}$$



Y. Yamamoto et al.,
PTPS185(2010)72

G-matrix
folding model



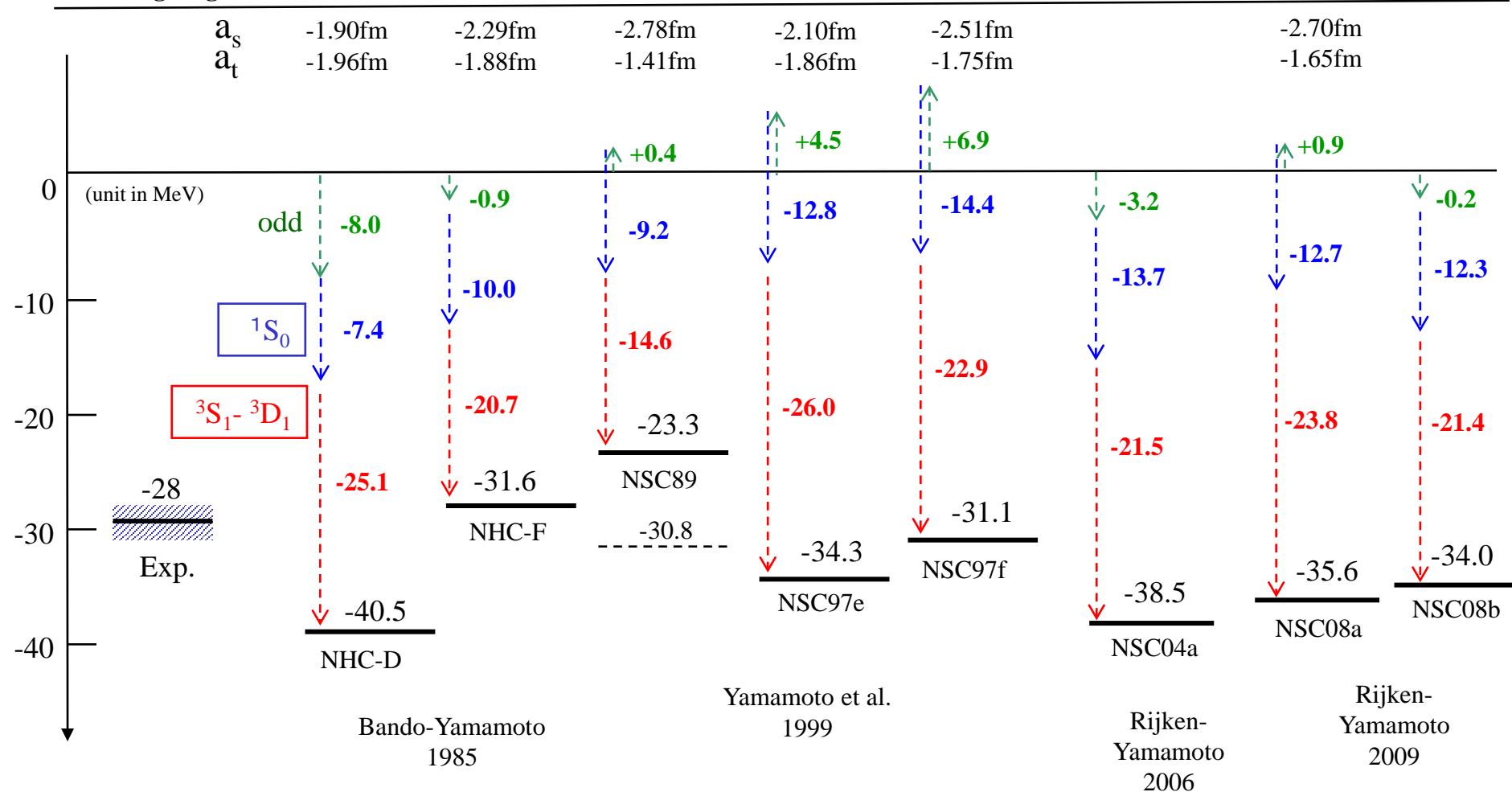
Λ single-particle energies in symmetric nuclear matter

OBEP: Nijmegen YN potential Models

$$U_{\Lambda}(k_F, \varepsilon_{\Lambda}) \quad k_F = 1.35 \text{ fm}^{-1}$$

G-matrix calc. QTQ

Scattering length



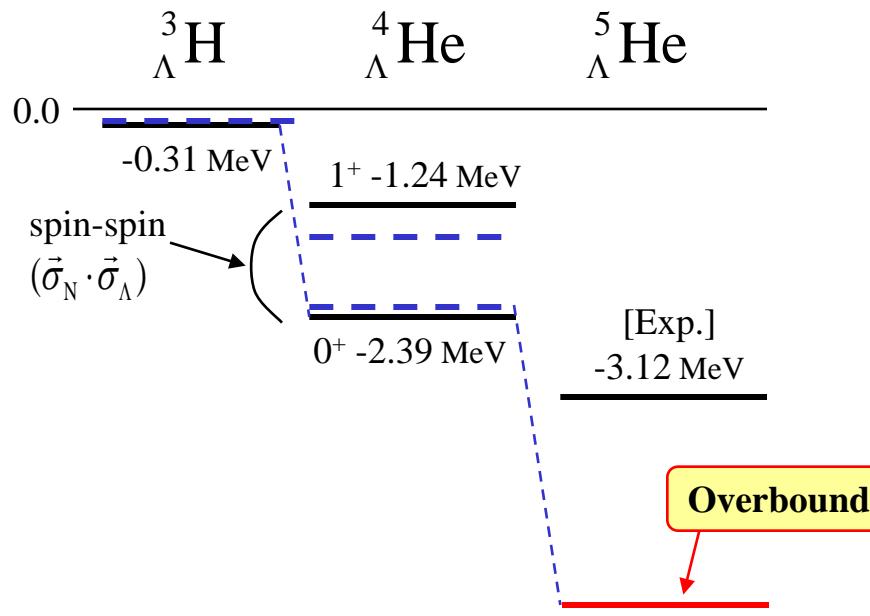
Y. Yamamoto, H. Bando, PTP Suppl. 81(1985)9; Y. Yamamoto, et al., PTP Suppl. 117(1994)361;

Th.A.Rijken, V.G.J.Stoks, Y.Yamamoto, PRC59(1999)21; Th.A.Rijken, Y.Yamamoto, PRC73(2006) 044008;

Y. Yamamoto, T.Motoba, T.A.Rijken, PTP Suppl. 185(2010)72.

Overbinding Problem on s-Shell Hypernuclei

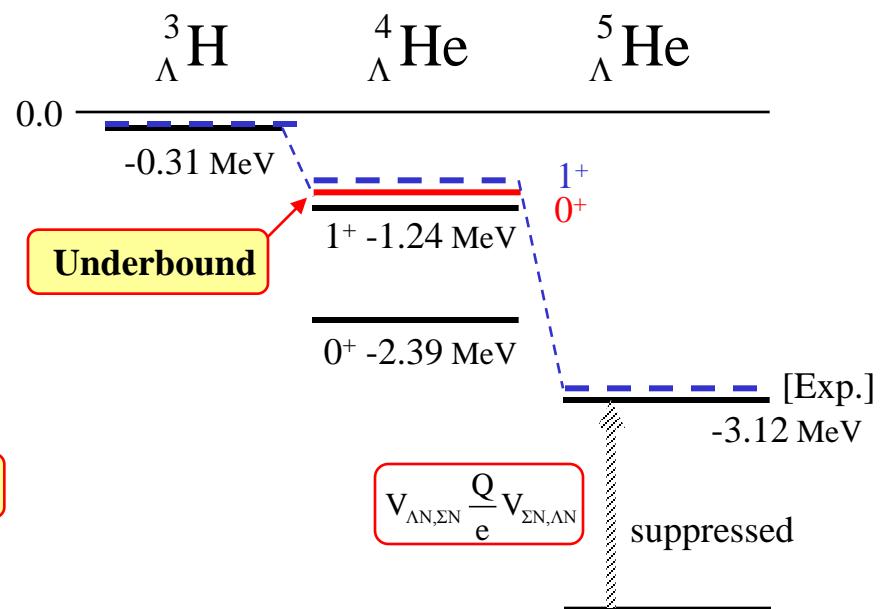
The Overbinding Problem



ΛN single-channel calc.

Dalitz et al., NP **B47** (1972) 109.

The Underbinding Problem



g-matrix calc. with $\Lambda N-\Sigma N(D2)$

Akaishi et al., PRL **84** (2000) 3539.

“The $0^+ - 1^+$ difference is not a measure of ΛN spin-spin interaction.”

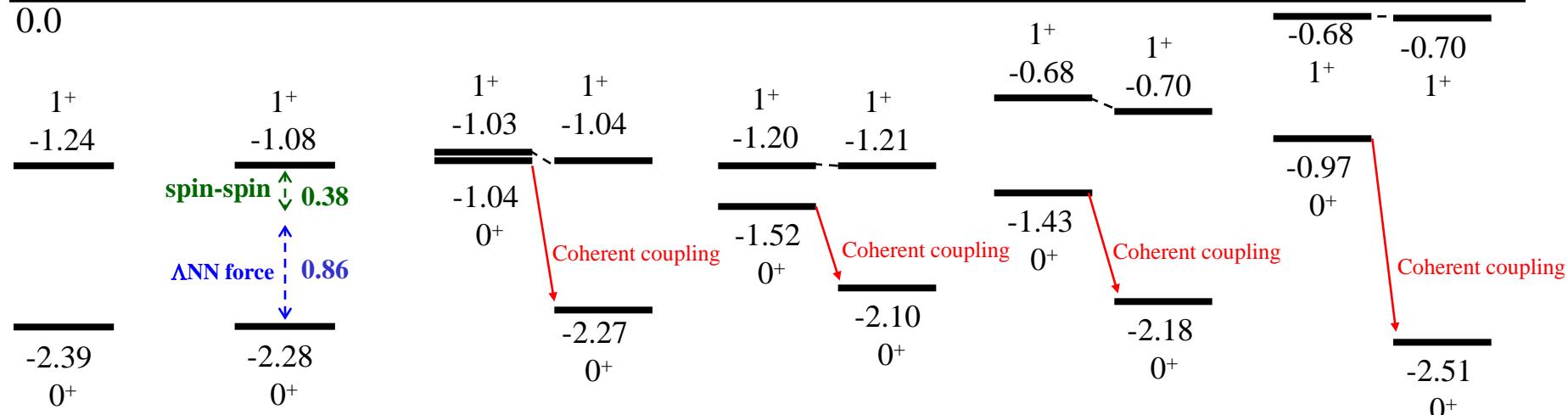
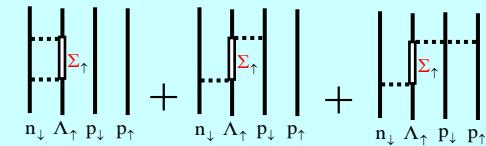
by B.F. Gibson

Hyperon-mixing

(unit in MeV) (${}^4_{\Lambda} \text{H}$)

${}^4_{\Lambda} \text{He}$

ANN three-body force



Exp.
phenomenological
 $V_{\text{AN}} + V_{\text{ANN}}$
 $\bar{V} = 6.20$

$$P_{\text{coh},\Sigma} = 1.9\%$$

$$P_{\text{coh},\Sigma} = 0.7\%$$

$$P_{\text{coh},\Sigma} = 0.9\%$$

$$P_{\text{coh},\Sigma} = 2.0\%$$

VMC

R. Sinha, Q.N.Usmali,
NPA684(2001)586c

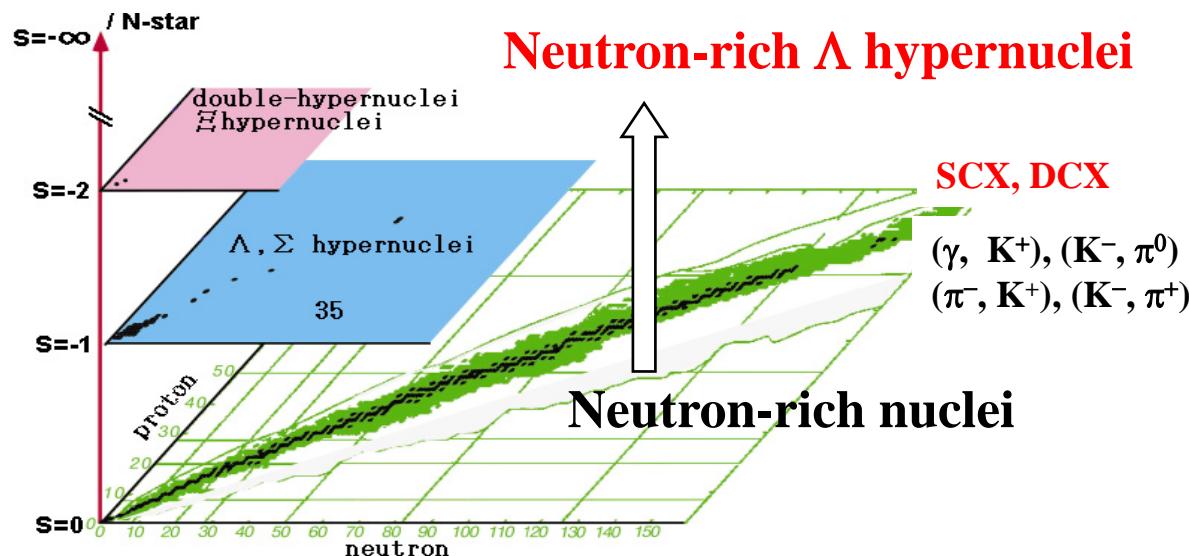
Breuckner-Hartree-Fock

Y. Akaishi, T.Harada, S.Shinmura, Khun Swe Myint,
PRL84(2000)3539

中性子過剰 Λ ハイパー核

E10@J-PARC

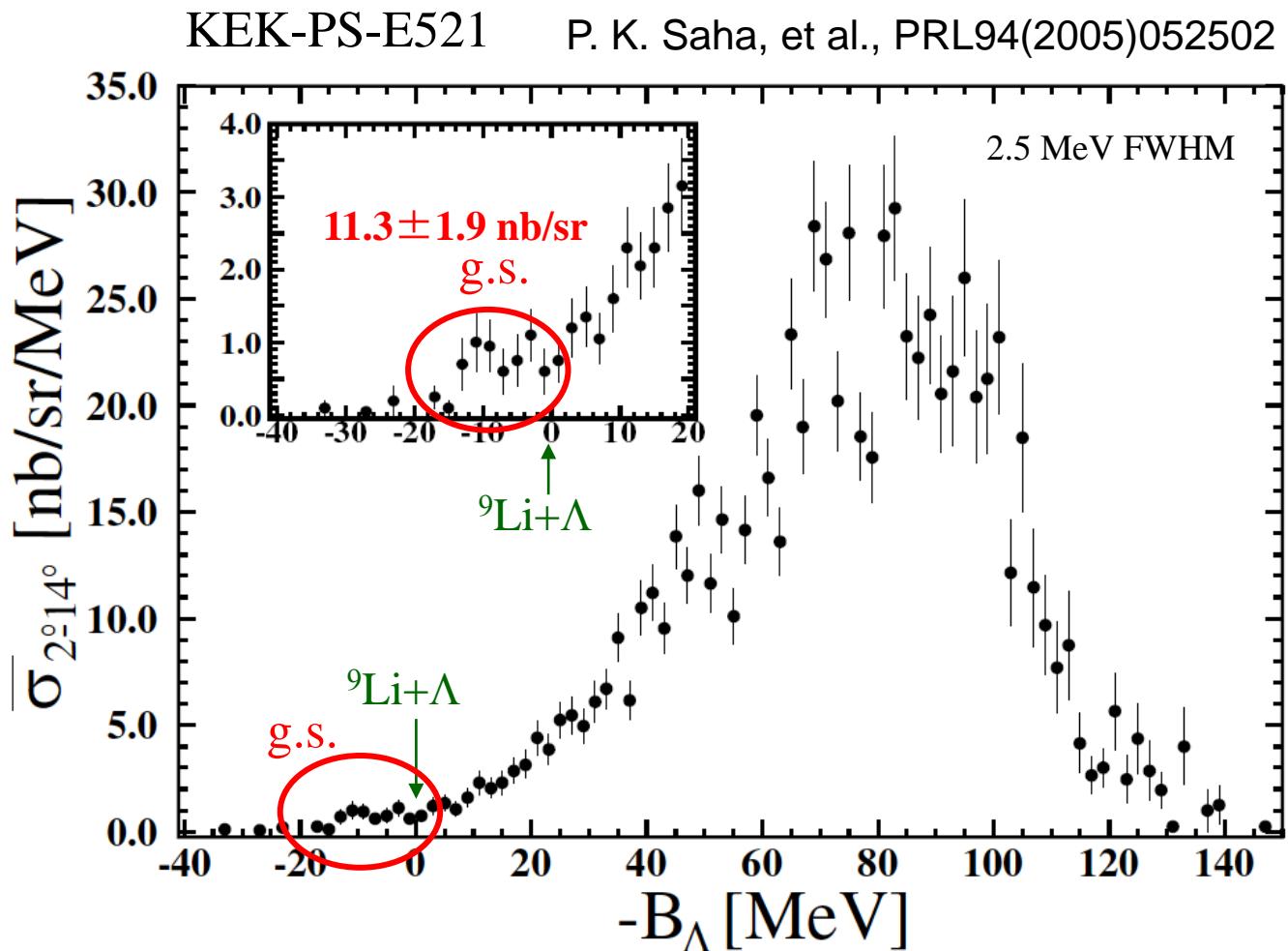
Production of **neutron-rich Lambda-hypernuclei** with the double charge exchange reaction



First production of neutron-rich Λ hypernuclei

$^{10}\text{B}(\pi^-, K^+) {}_{\Lambda}^{10}\text{Li}$

Λ spectrum by DCX (π^- , K^+) reaction at 1.2GeV/c



Cross sections

- $p_\pi = 1.20 \text{ GeV/c}$
- $\frac{d\sigma}{d\Omega_L} \approx 11.3 \pm 1.9 \text{ nb/sr}$

- $p_\pi = 1.05 \text{ GeV/c}$
- $\frac{d\sigma}{d\Omega_L} \approx 5.8 \pm 2.2 \text{ nb/sr}$

$\sim 1/1000$

${}^{12}\text{C}(\pi^+, K^+) {}_{\Lambda}^{12}\text{C}$ (1.2 GeV/c)

$17.5 \pm 0.6 \mu\text{b/sr}$

$(\pi^-$, $K^+)$ – Double Charge Exchange (DCX) Reaction

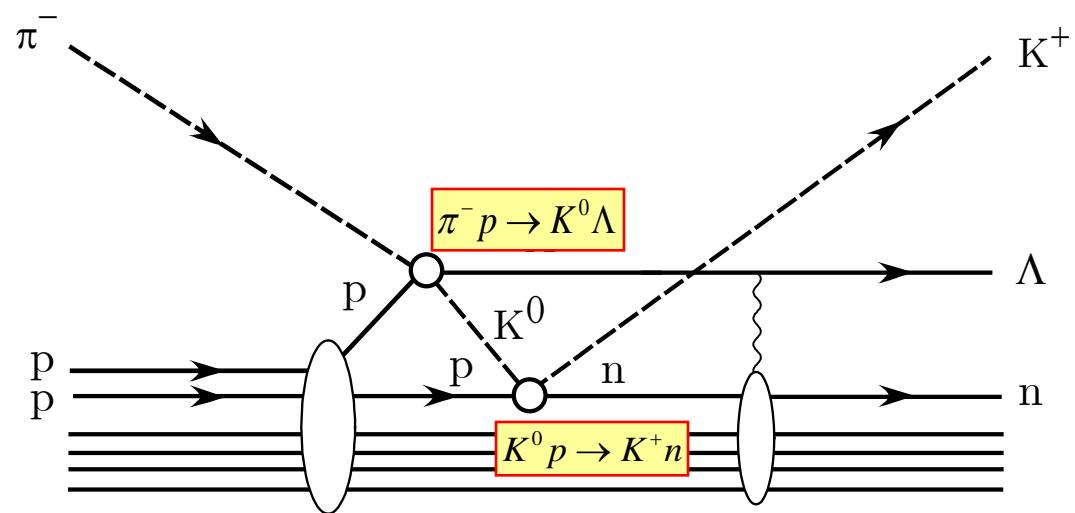
Two-step process:

$$\pi^- p \rightarrow K^0 \Lambda$$

$$K^0 p \rightarrow K^+ n$$

$$\pi^- p \rightarrow \pi^0 n$$

$$\pi^0 p \rightarrow K^+ \Lambda$$

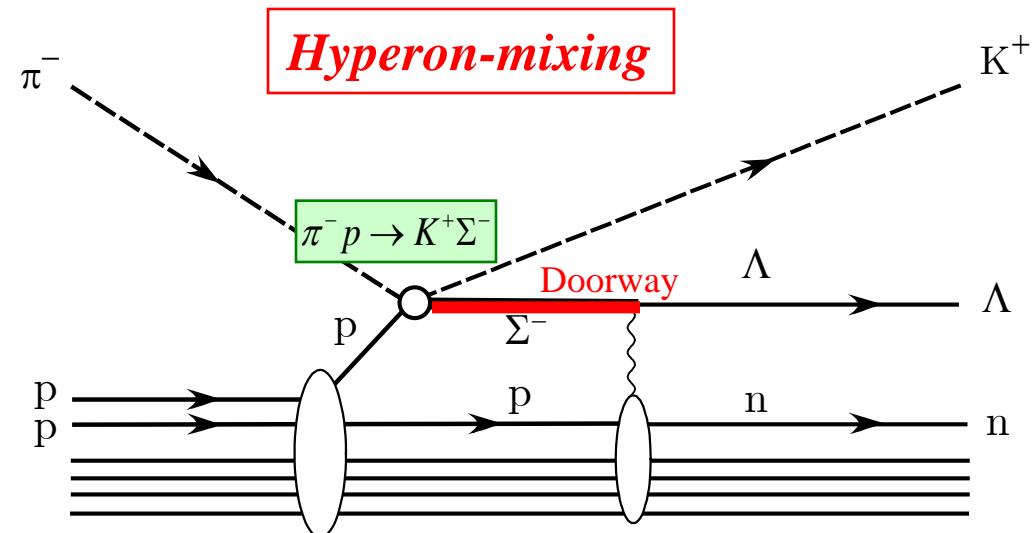


One-step process:

$$\pi^- p \rightarrow K^+ \Sigma^-$$

$$\Sigma^- p \leftrightarrow \Lambda n$$

via Σ^- doorways caused by $\Lambda N - \Sigma N$ coupling



Λ spectrum by DCX (π^- , K^+) reactions at 1.2GeV/c

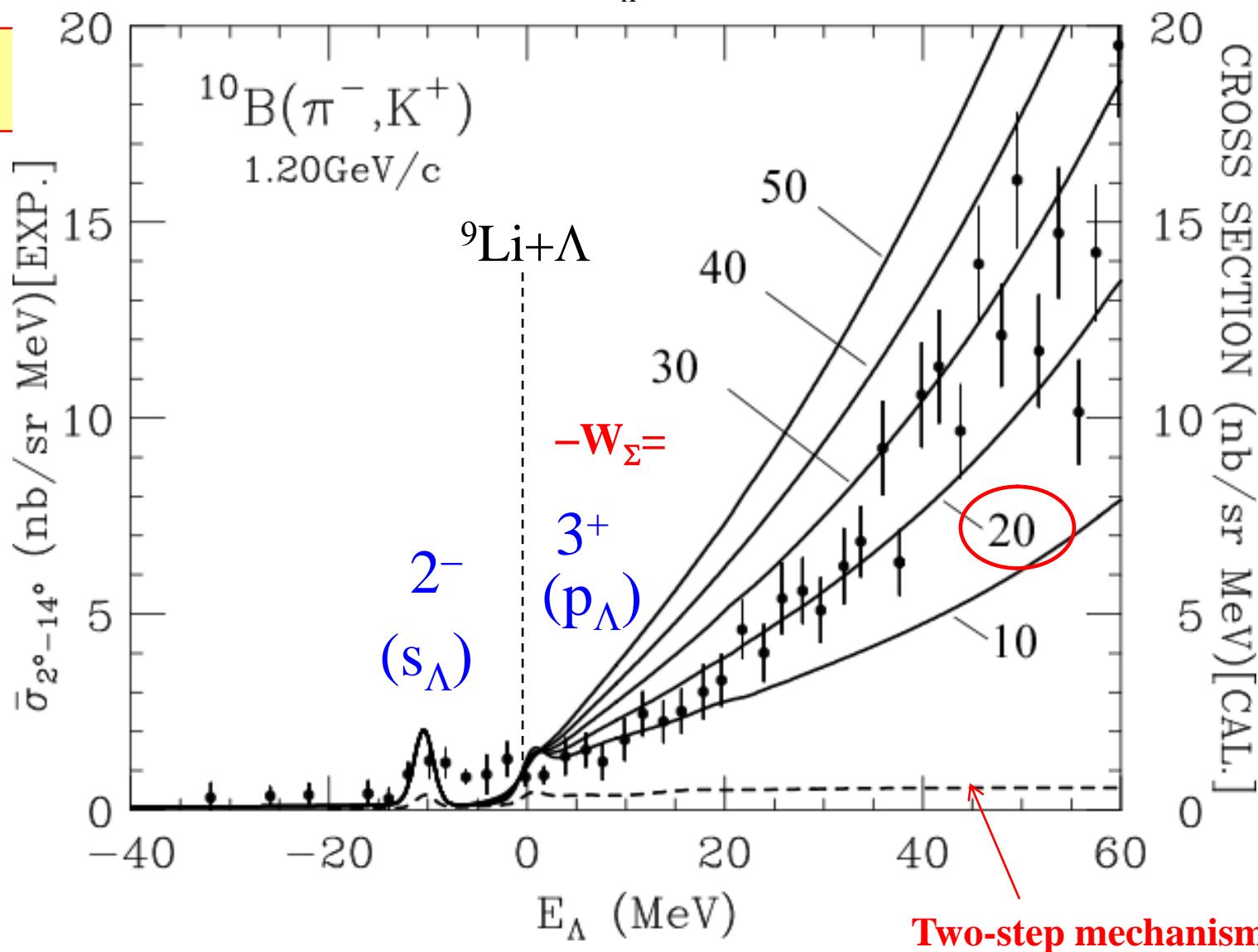
Harada, Umeya,Hirabayashi, PRC79(2009)014603

Spreading potential dep.

W_Σ

$U_X = 11$ MeV is fixed. $P_{\Sigma^-} = 0.57\%$

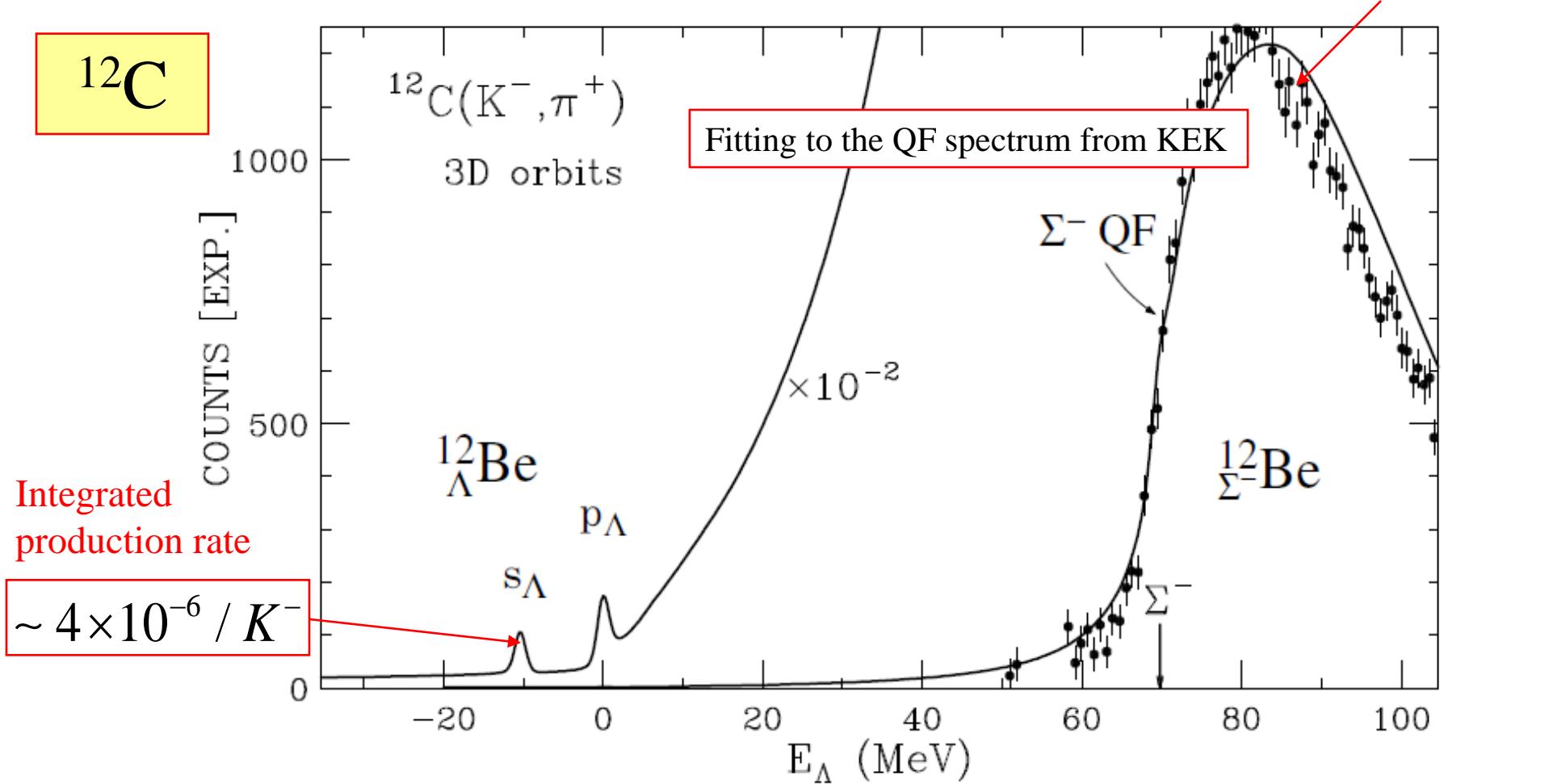
^{10}B



Λ spectrum by DCX (stopped K^- , π^+) reactions

If the Σ^- admixture probability of $\sim 0.6\%$ is assumed in $^{12}\Lambda\text{Be}$,
we demonstrate the (stopped K^- , π^+) spectrum on a ^{12}C target.

Early
KEK data

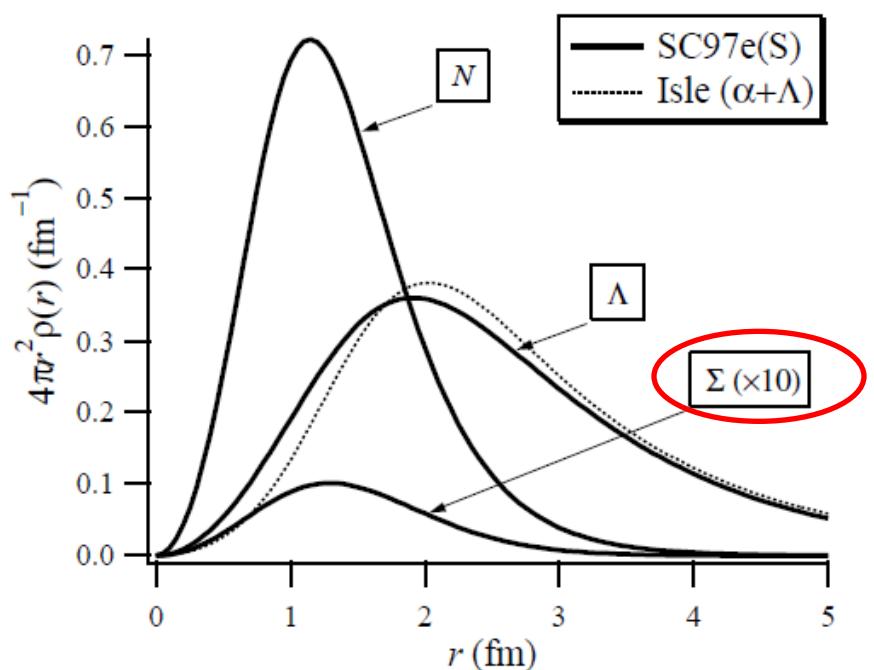


DAΦNE data: U.L. $\sim (2.0 \pm 0.4) \times 10^{-5} / K^-$

M.Agnello, et al., PLB640(2006)145.

Ab initio calculation of $\Lambda^5\text{He}$ with full realistic interactions

H.Nemura et al., PRL89(2002)142504



Better understanding of the Λ - Σ coupling and Tensor force

Hyperon-mixing

α^* $T_c = 1 \otimes \Sigma$ ~ 1.5 % admixture

Incoherent Λ - Σ coupling

$$\begin{array}{c} \alpha^* \\ \uparrow \\ T_c = 1 \otimes \Sigma \\ \downarrow \\ \alpha \end{array}$$

$$T_c = 0 \otimes \Lambda$$

- The Σ admixture of ~1.5 % appears in ${}^5\Lambda\text{He}$.
- The α -particle is not a rigid core.



The incoherent Σ admixture is also important.

| | $L = 0$ | | $L = 2$ | | |
|-----------------------------|-------------------|-----------|-------------------|-----------|-------------------|
| | $S = \frac{1}{2}$ | $S_c = 0$ | $S = \frac{3}{2}$ | $S_c = 1$ | $S = \frac{5}{2}$ |
| ${}^5\Lambda\text{He}$ | | | | | |
| $(T_c = 0) \otimes \Lambda$ | 89.14 | 0.03 | 0.19 | 3.74 | 5.36 |
| $(T_c = 1) \otimes \Sigma$ | 0.10 | 0.09 | 1.34 | ~ 0 | 0.01 |
| ${}^4\text{He}$ | 89.56 | | 10.44 | | |

Production of neutron-rich Λ -hypernuclei with the DCX reaction

E10@J-PARC

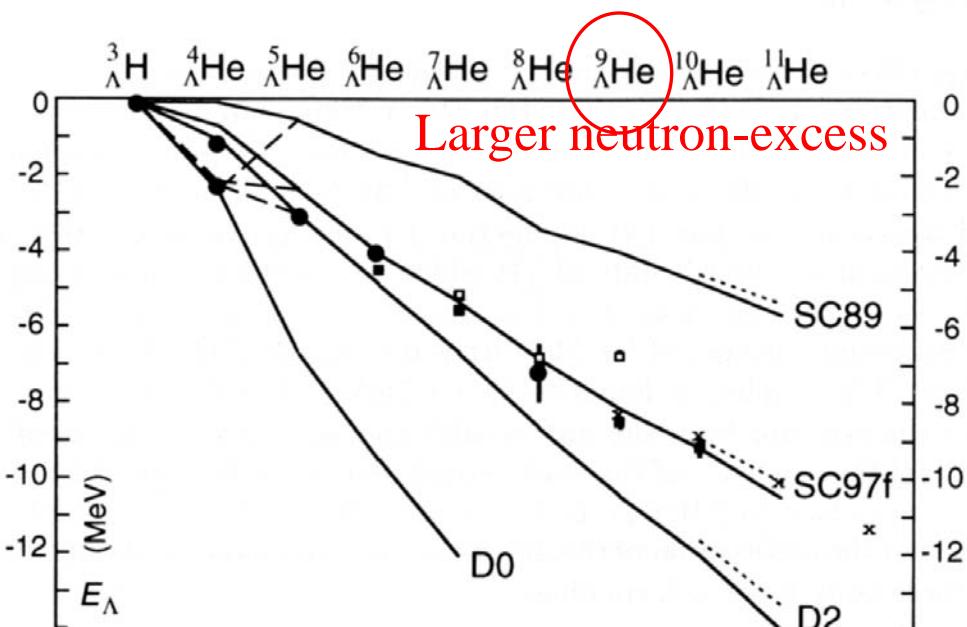


“Hyperheavy hydrogen”

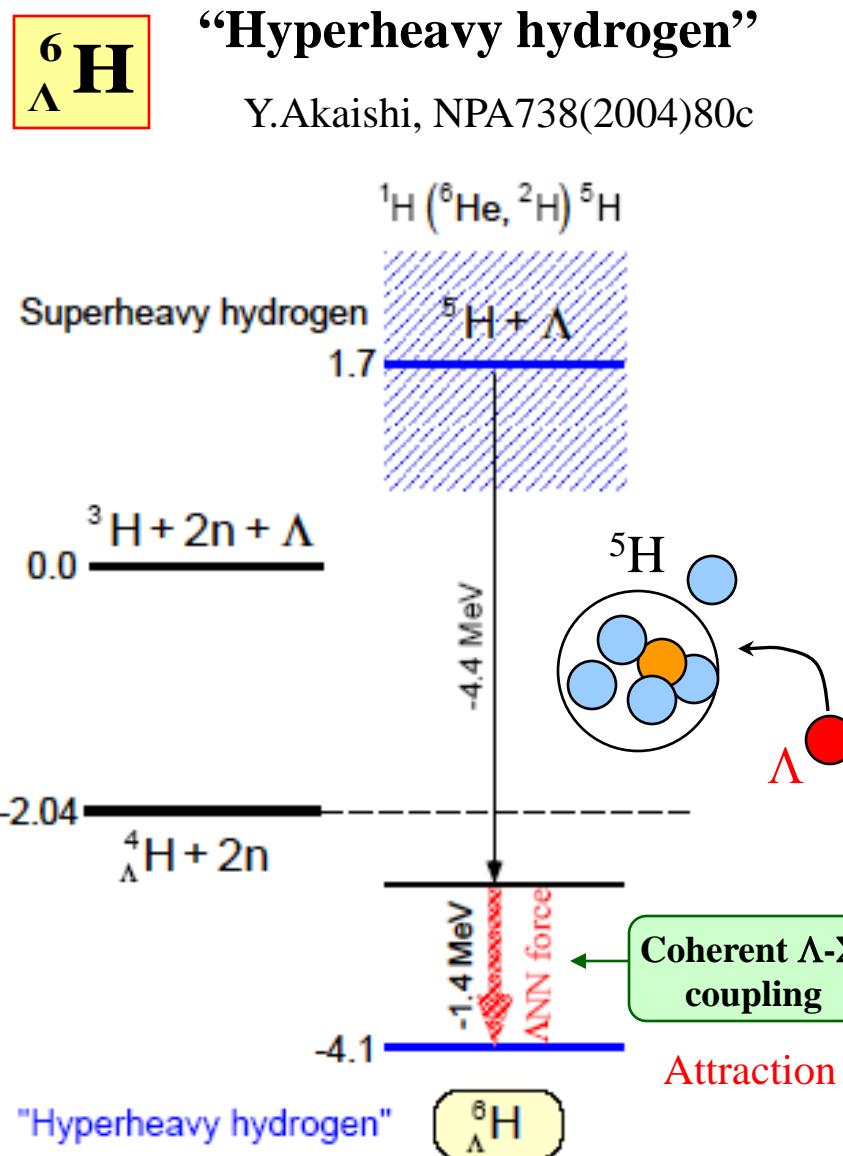
Y.Akaishi, NPA 738(2004)80c



Khin Swe Myint et al.,
FBS. Suppl. 12(2000)383



Λ binding energies



Coherent Λ - Σ coupling in neutron-excess environment

Extremely enhanced

ハイペロン-核子間相互作用

■ One-Boson-Exchange model

➤ Nijmegen potential

NHC-D/F → NSC89 → NSC97e,f → ESC04a-d →
ESC06 → ESC08a-c

[Th.A. Rijken, M. M. Nagels, Y. Yamamoto, PTPS185(2010)14]

➤ Funabashi-Gifu potential

[I. Arisaka et al., PTP104(2000)995; FBS.Suppl.12(2000)395]

■ Quark Cluster model

➤ Kyoto-Niigata potential

RGM-F → FSS → fss2

[Y. Fujiwara et al, PRC54(1996) 2180; PPNP58 (2007)439]

■ Chiral LO Effective Field Theory

➤ Julich potential

[H.Polinder, et al., NPA779 (2006) 244;PLB653 (2007) 29]

■ Lattice QCD

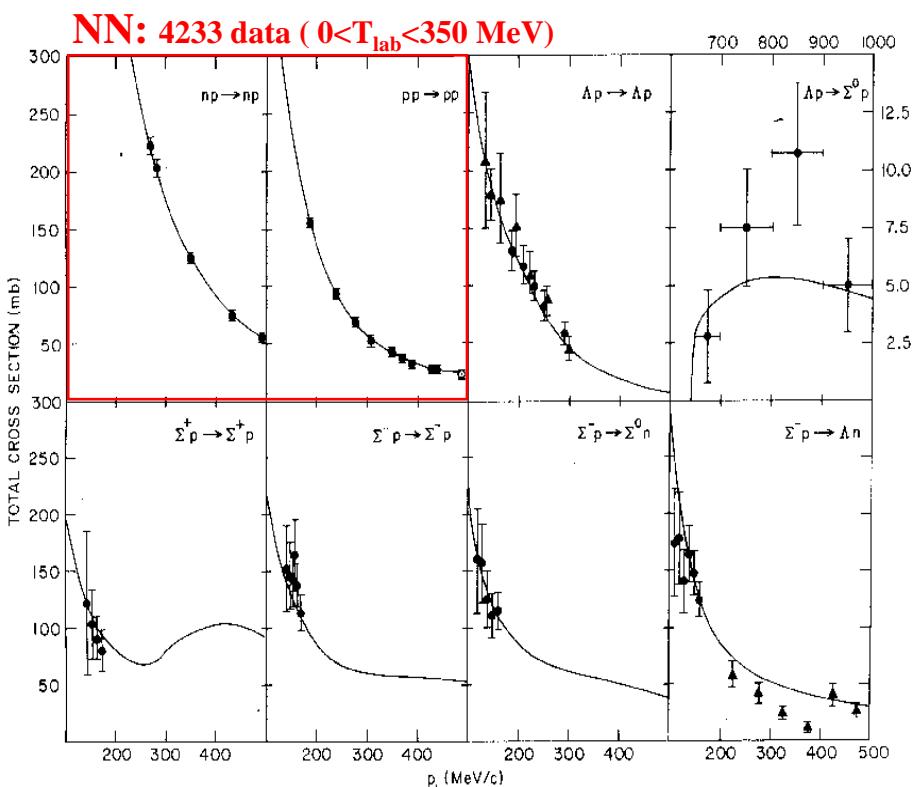
NN, YN, YY interactions

Flavor SU(3)_f symmetry

symmetric

antisymmetric

$$[8] \otimes [8] = [27] \oplus [10^*] \oplus [10] \oplus [8_s] \oplus [8_a] \oplus [1]$$



1S_0

3S_1

NN NN

$\Sigma N, \Sigma N - \Lambda N, \Lambda N$

35 data

S= 0

S= -1

$\Sigma\Sigma, \Xi N - \Sigma\Lambda - \Sigma\Sigma, \Xi N - \Sigma\Sigma - \Lambda\Lambda$ S= -2

$\Xi\Sigma, \Xi\Sigma - \Xi\Lambda$

S= -3

$\Xi\Xi$

$\Xi\Xi$

S= -4

Total cross section for baryon-baryon scattering

C.B. Dover and H. Feshbach, Ann. Phys. 198(1990)321

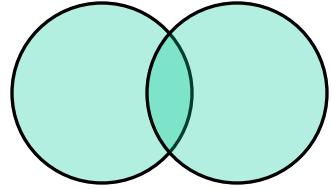
バリオン-バリオン間相互作用の短距離斥力

Quark Cluster Model

M.Oka,K.Shimizu,K.Yazaki, PLB130(1983)365; NPA464(1987)700

Spin-flavor SU(6) symmetry

クオーク交換力(反対称化)



$$[3] \otimes [3] = [6] \oplus [42] \oplus [51] \oplus [33]$$

symmetric antisymmetric

orbital x flavor-spin x color singlet $\downarrow L=0$

Pauli forbidden state

S = 0 state

[51]

[33]

| | | |
|----------|--|--|
| 1 | | $\Lambda\Lambda-\Xi\bar{N}-\Sigma\Sigma(I=0)$, H-dibaryon |
|----------|--|--|

8_S

1

$\Sigma N(I=1/2, ^1S_0)$ ***Pauli forbidden***

27

4/9

5/9

$NN(^1S_0)$

S = 1 state

[51]

[33]

| | | | |
|----------------------|------------|------------|--|
| 8_A | 5/9 | 4/9 | |
|----------------------|------------|------------|--|

10

8/9

1/9

$\Sigma N(I=3/2, ^3S_1)$ ***almost Pauli forbidden***

10*

4/9

5/9

$NN(^3S_1)$, $\Lambda N-\Sigma N(I=1/2, ^3S_1)$

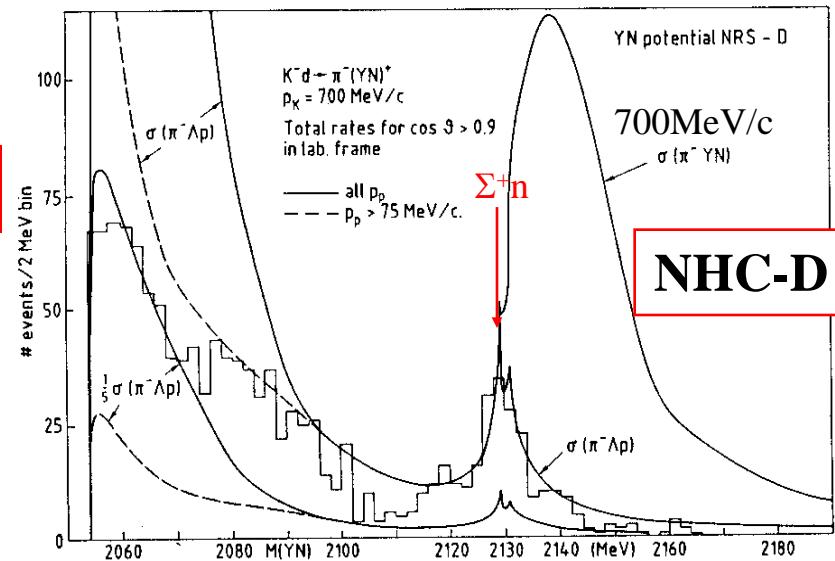
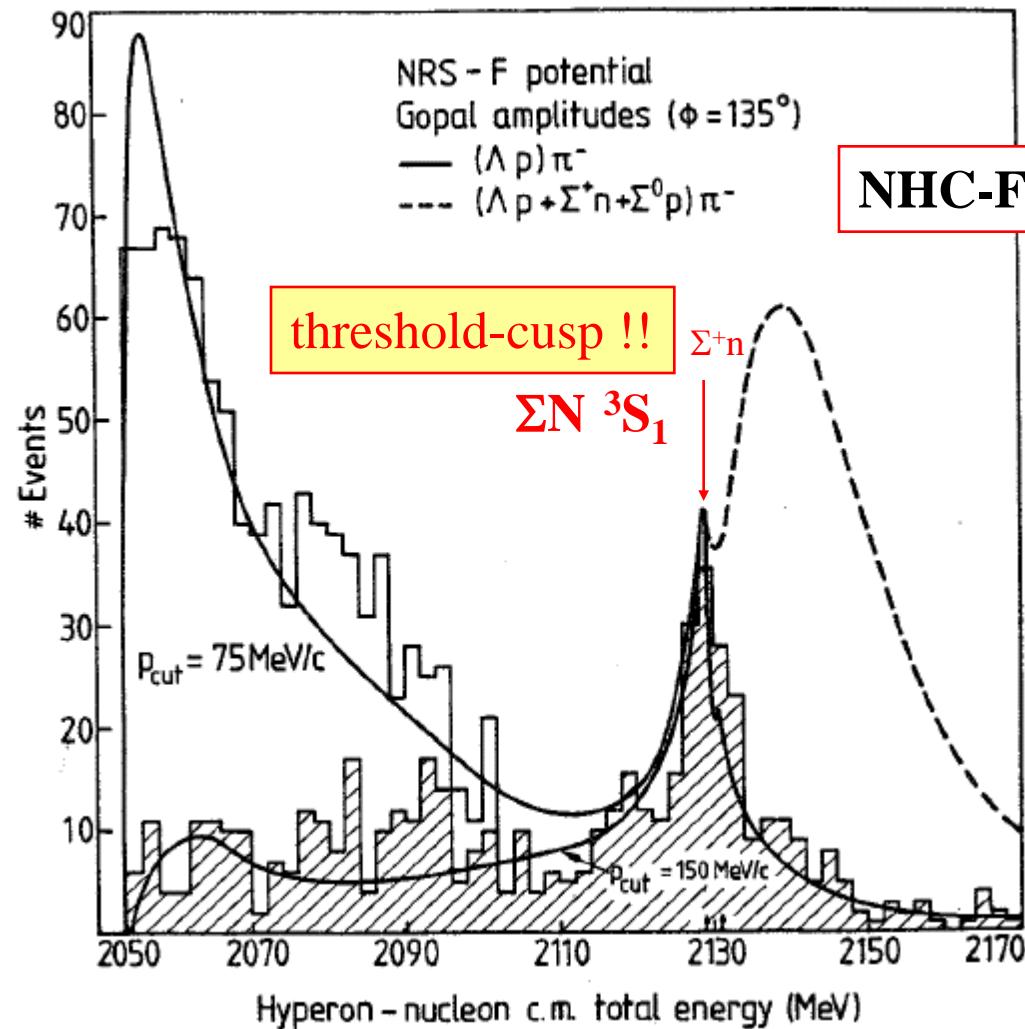
➤ SU(6)sp symm. → Strongly spin-isospin dependence, $V_{ALS}(\Lambda N) \sim V_{LS}(\Lambda N)$

K⁻d → π⁻Λp spectrum in ²H(K⁻, π⁻) Reactions

ΣN ³S₁ [10*]: “Strangeness partner of deuteron”

R.H.Dalitz, Deloff,

R.H.Dalitz, Deloff, Czech.J.Phys.B32(1982)1021



R.H.Dalitz

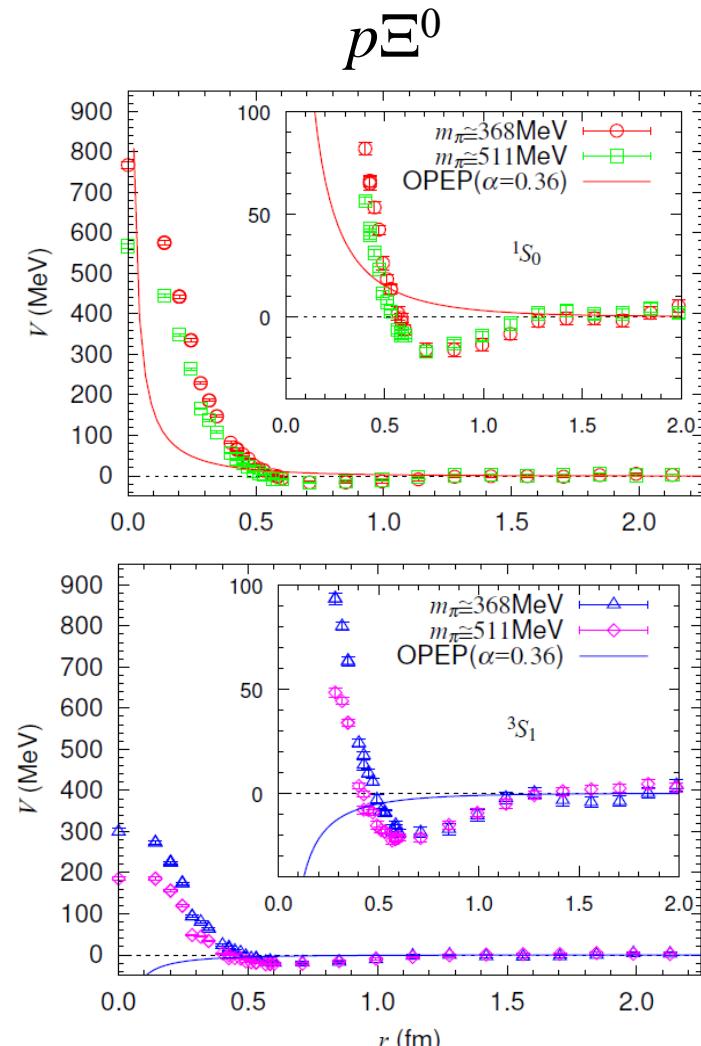
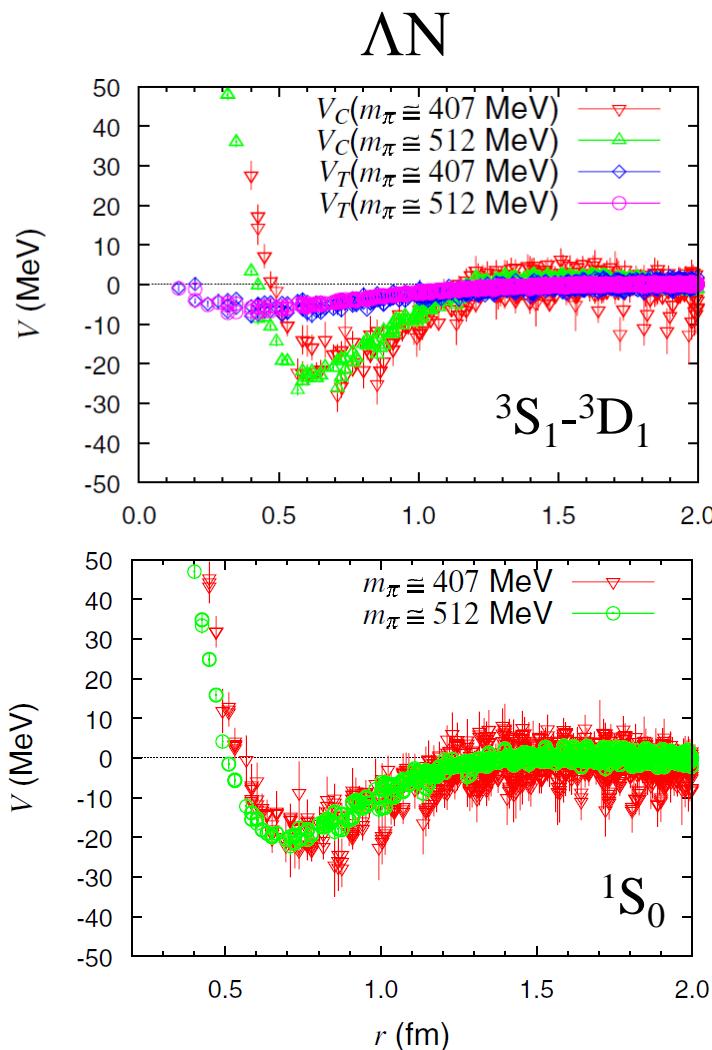


Baryon-Baryon force from lattice QCD

[NN] N. Ishii, S. Aoki, T. Hatsuda, PRL99(2007)022001

[ΛN,ΞN] H. Nemura et al., PLB673(2009)136; HAL QCD Collaborations, NPA835(2010)176

$$V_{\Lambda N} = V_0(r) + V_\sigma(r)(\vec{\sigma}_\Lambda \cdot \vec{\sigma}_N) + V_T(r)S_{12} + V_{LS}(r)(\vec{L} \cdot \vec{S}_+) + V_{ALS}(r)(\vec{L} \cdot \vec{S}_-) + O(\nabla^2)$$



Σ ハイパー核

■ Σ single-particle potentialの性質

(π -, K^+)反応スペクトルの解析

Σ -原子のX線データの解析

■ 強いアイソスピン依存性

(K -, π^+)反応スペクトルの解析

■ Σ ハイパー核の束縛状態, ${}^4\Sigma$ He

Coherent Lane-term / Coherent Λ - Σ coupling term

α 粒子のstrangeness partner

Σ^- spectrum by (π^-, K^+) reaction at 1.2GeV/c

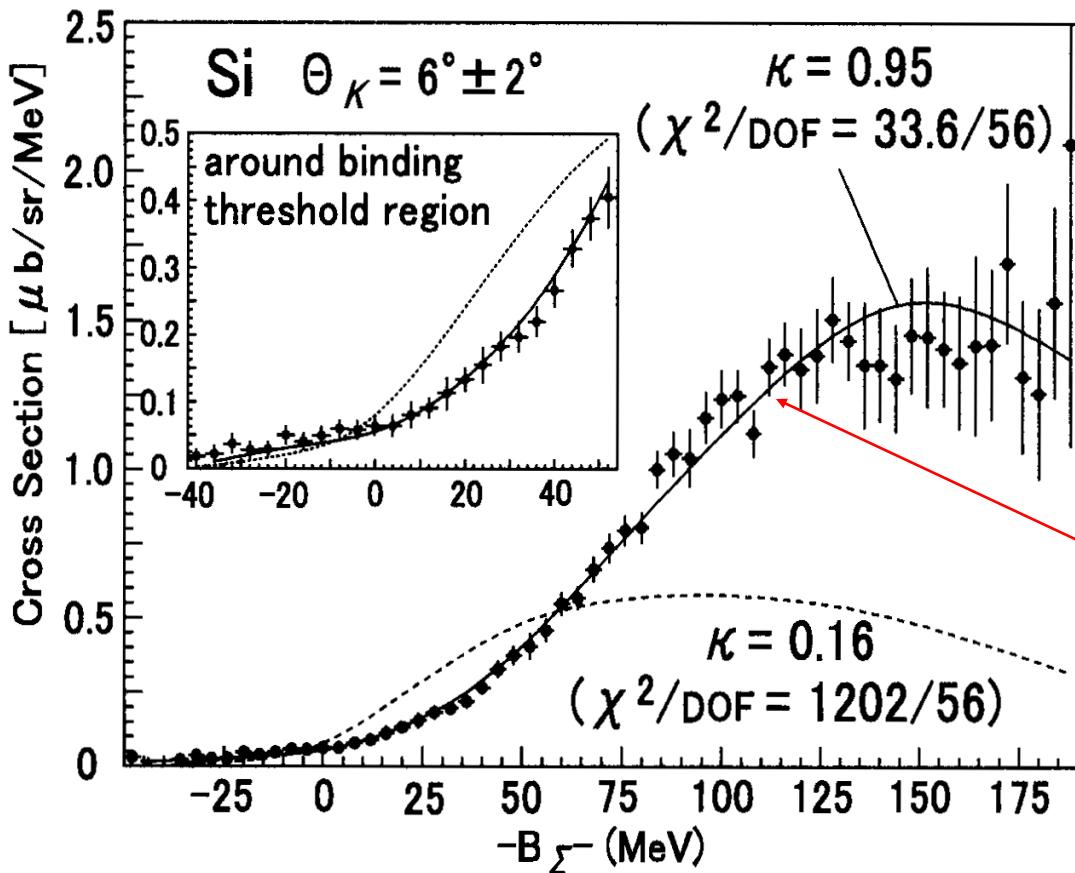
Study of Σ s.p. potential by (π^-, K^+) reactions

Targets: ^{28}Si , ^{58}Ni , ^{115}In , ^{209}Bi

^{28}Si

Direct Σ production at the nuclear interior

H.Noumi, et al. PRL89(2002)072301



Woods-Saxon form

$$U_\Sigma = \frac{V_\Sigma + iW_\Sigma}{1 + \exp[(r - R)/a]}$$

$$R = r_0(A-1)^{1/3} \text{ fm}$$

$$a = 0.67 \text{ fm} \quad r_0 = 1.1 \text{ fm}$$

$V_\Sigma = +90 \text{ MeV}$

$W_\Sigma = -40 \text{ MeV}$

Strong repulsion

Large imaginary

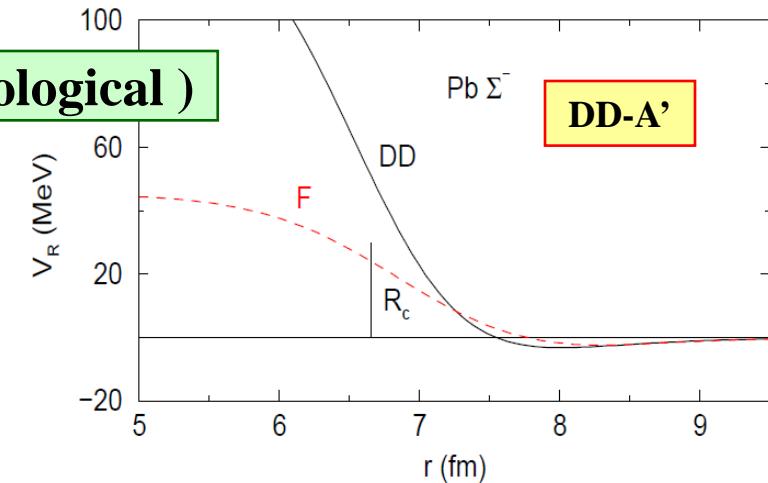
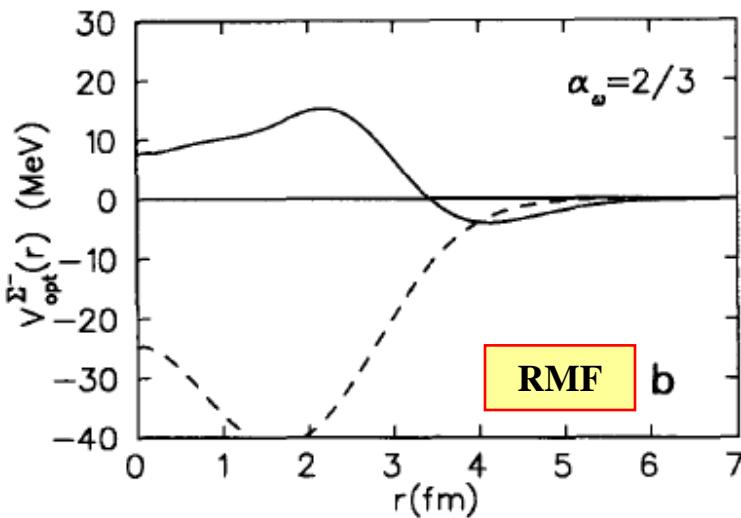
P.K.Saha, et al., PRC70(2004)044613

These Σ -nucleus potentials have a repulsion with a sizable imaginary potential.

Σ^- -nucleus potentials fitted to the Σ^- atomic data

Density-dependent (DD) potential (Phenomenological)

C.J.Batty et al., Phys.Rep.287(1997)385,
E. Friedman and A. Gal, Phys. Rep. 452 (2007)89.



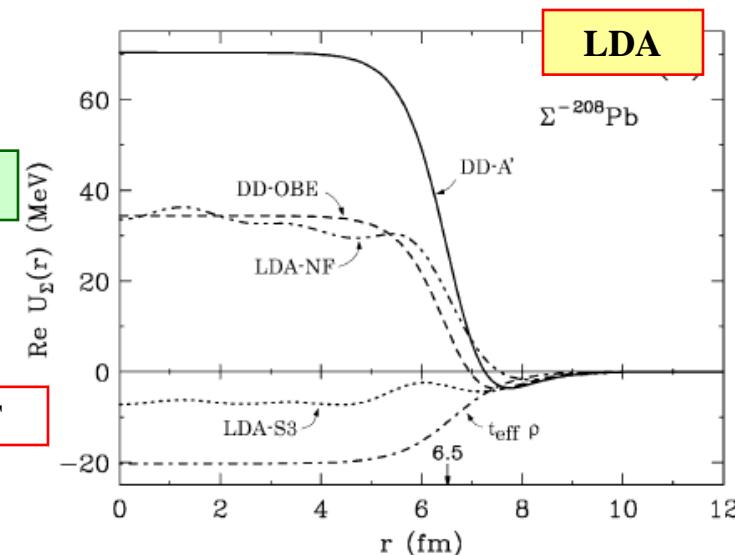
Relativistic mean-field (RMF) potential

J. Mares et al., NPA594(1995)311.
K.Tsubakihara et al., EPJA33(2007)295

Folding-model potential for LDA with G-matrix

D. Halderson, Phys. Rev. C40(1989)2173.
T.Yamada and Y.Yamamoto, PTP. Suppl. 117(1994)241
J. Dabrowski, Acta Phys. Pol. B31(2001)2179
T.Harada, Y.Hirabayashi, NPA759 (2005) 143; 767(2006)206

YNG-F



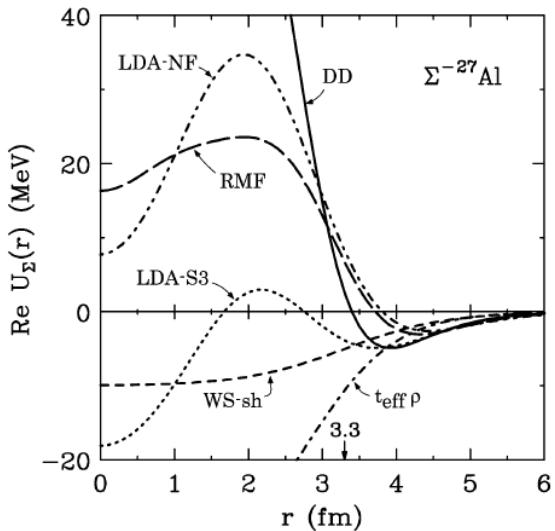
Not so sensitive to the radial behavior of the potential inside the nucleus !!

$^{28}\text{Si}(\pi^-, \text{K}^+)$ reaction at 1.2 GeV/c

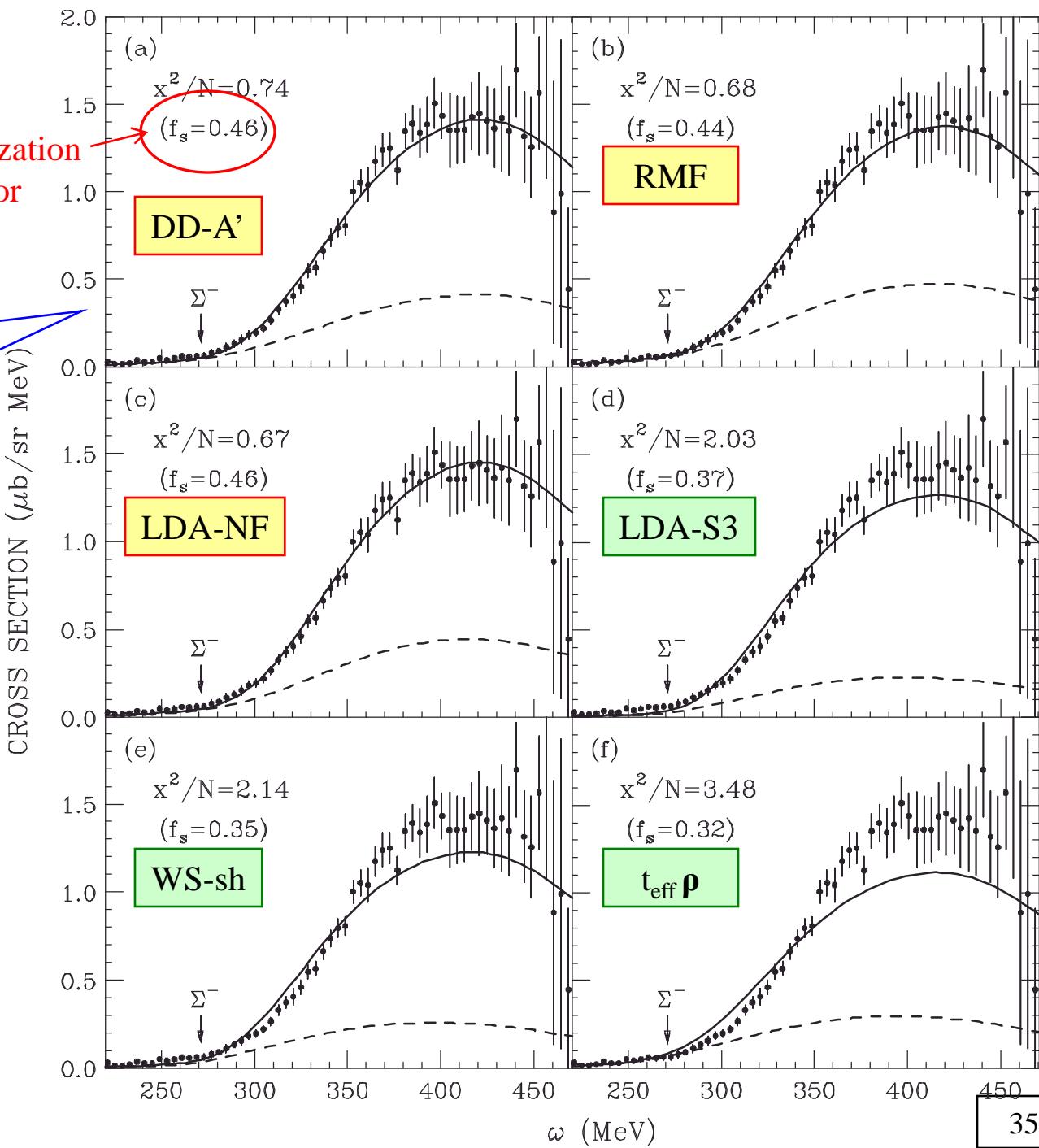
^{28}Si

Normalization
factor

Consistent with the
potentials fitted to
 Σ^- atomic data !!



T.Harada, Y.Hirabayashi,
NPA759 (2005) 143

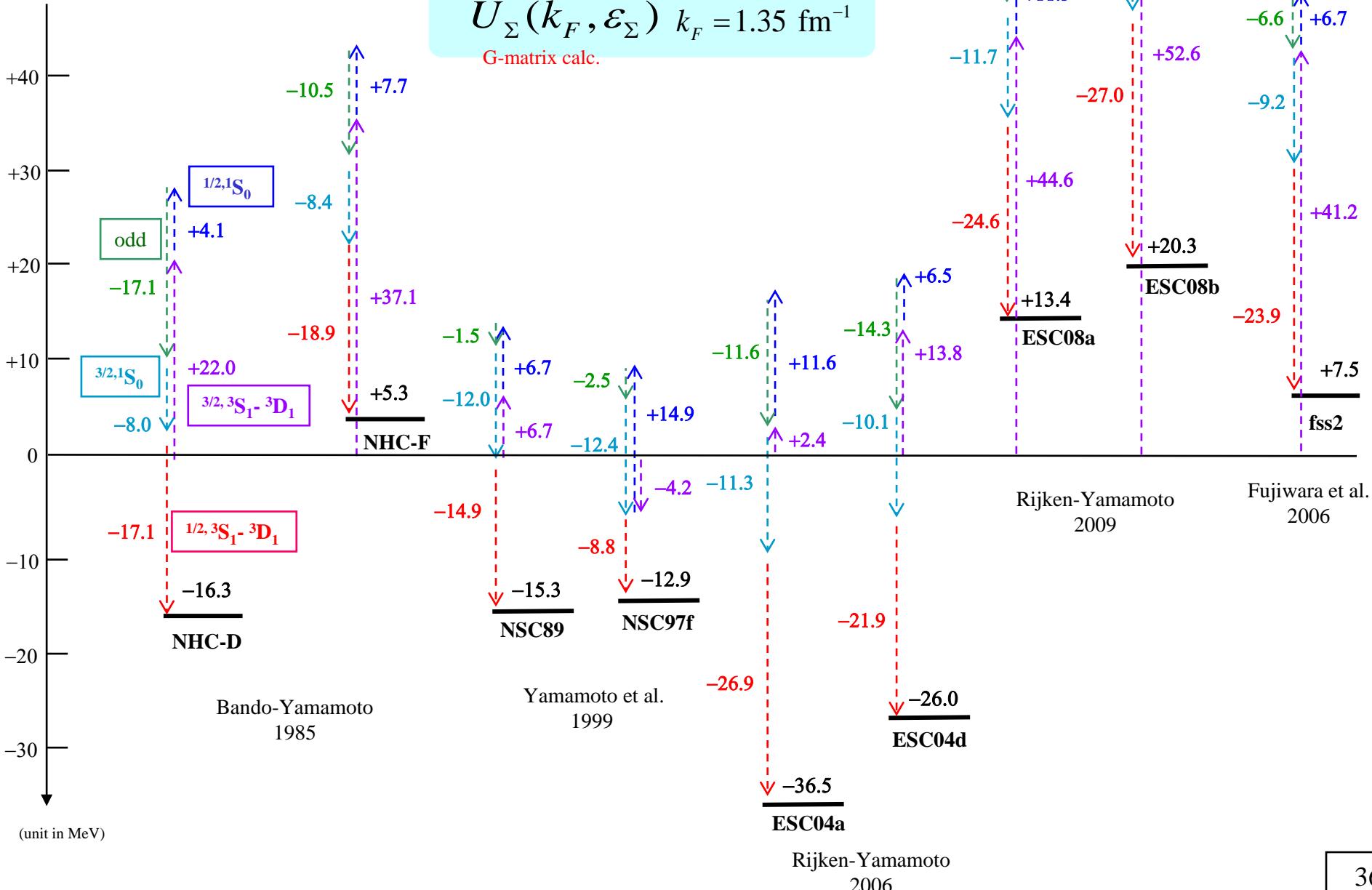


Σ s.p. energies in symmetric nuclear matter

May, 2010 update

$$U_{\Sigma}(k_F, \epsilon_{\Sigma}) \quad k_F = 1.35 \text{ fm}^{-1}$$

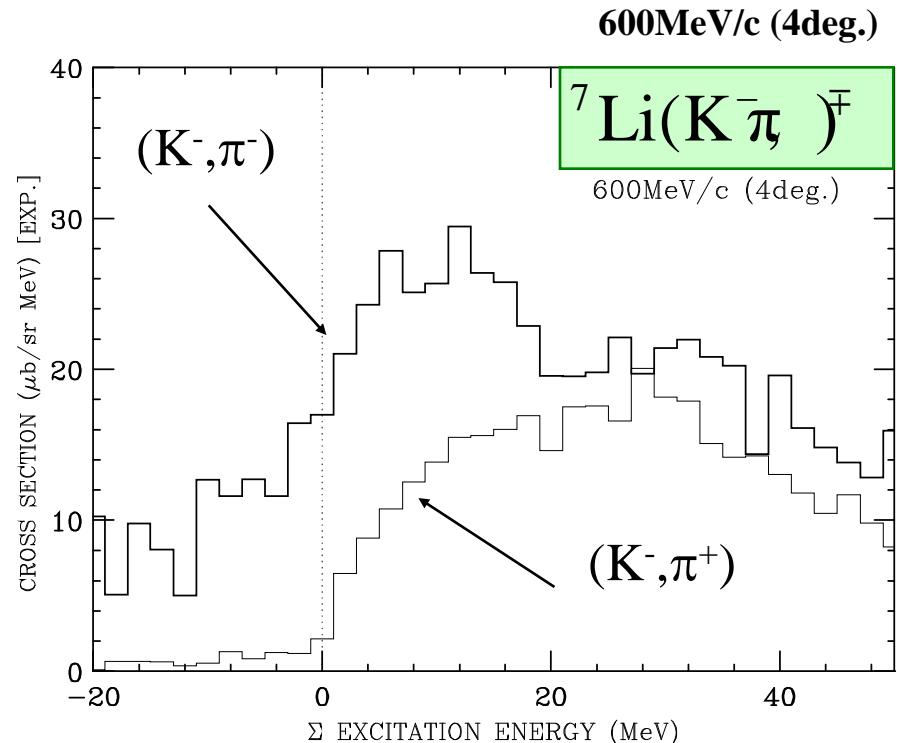
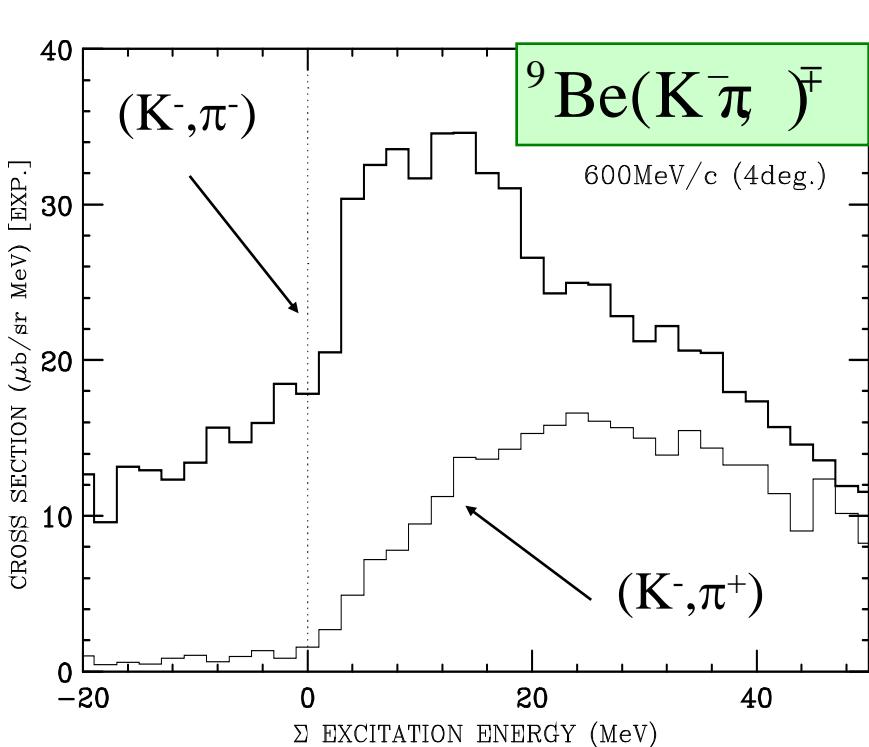
G-matrix calc.



(K⁻,π[±]) Experiments at BNL-AGS in 1990-2000

“The Σ narrow width puzzle was disappeared.”

by S.Bart et al., PRL83(1999)5239.



- There is no Σ bound state on both ${}^6\text{Li}$ and ${}^9\text{Be}$.
- The π^- and π^+ spectra are very different each other.

→ *Strong isospin dependence of the Σ -nucleus potentials*

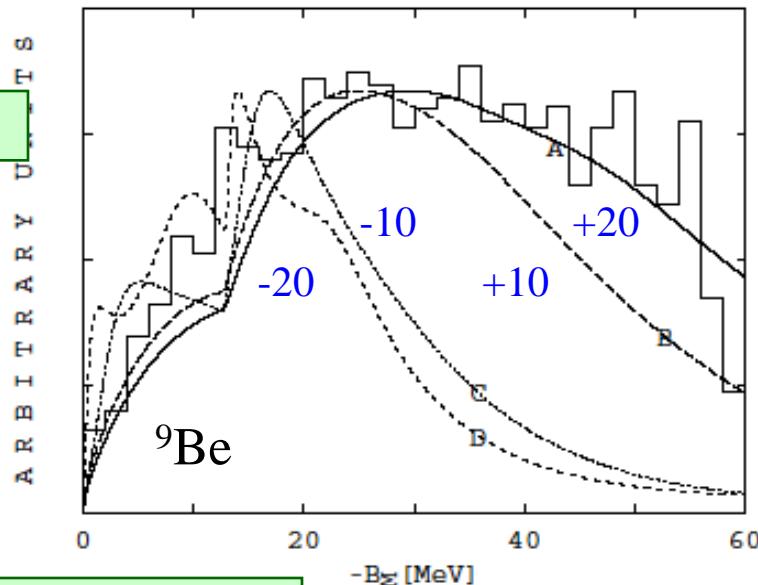
Comparison with resent studies

PWIA analysis with the Square-Well potential

J. Dabrowski, PRC60 (1999) 025205.

J. Dabrowski, J. Rozynek, Acta. Phys. Pol. B35 (2004) 2303.

*“The Σ s.p. potential is **repulsive** inside nucleus.
Only NHC-F is acceptable.”*

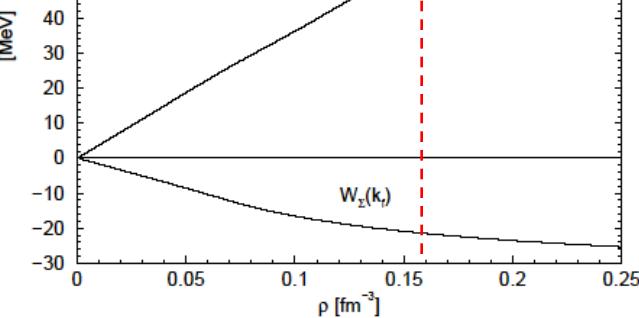


Chiral dynamics in the nuclear medium

N. Kaiser, PRC71 (2005) 068201

$$U_{\Sigma}(\rho_0) \sim 59 \text{ MeV} : \text{repulsive}$$

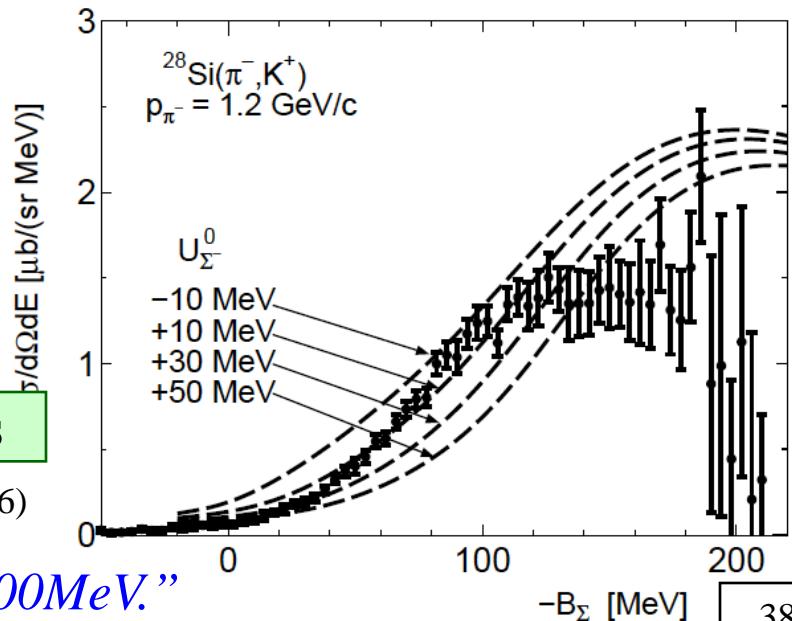
$$W_{\Sigma}(\rho_0) \sim -21 \text{ MeV}$$



Semi-Classical Distorted Wave Model Analysis

M. Kohno, Y. Fujiwara, et al., nucl-th/0611080 (2006)

*“The **repulsive** Σ potential is not so strong as ~ 100 MeV.”*



Remarks

Properties of the Σ -nucleus potentials by comparing theoretical calculations with the available data:

$$U_{\Sigma}(\mathbf{r}) = U_{\Sigma}^0(\mathbf{r}) + \frac{1}{A_{\text{core}}} U_{\Sigma}^{\tau}(\mathbf{r})(\vec{T}_{\text{core}} \cdot \vec{t}_{\Sigma})$$

“repulsion inside the nuclear surface”

“shallow attraction outside the nucleus”

“strong isospin-dependence”

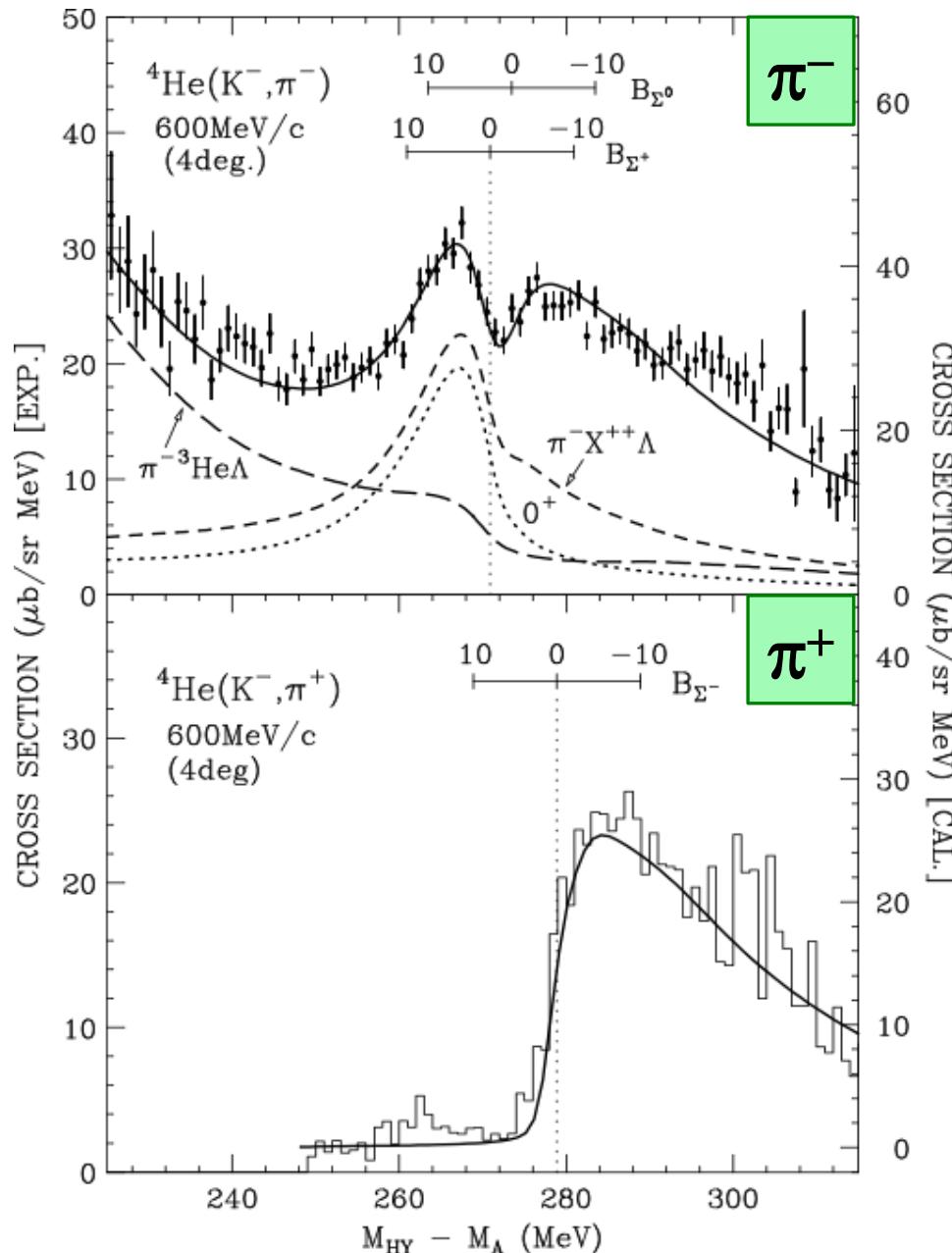
The calculated spectra for ${}^4\text{He}(K^-, \pi^\pm)$ reaction can explain consistently the available data from BNL, KEK, and ANL.

Σ -3N potential: the ${}^4\text{He}$ bound state with $T=1/2, J^\pi=0^+$

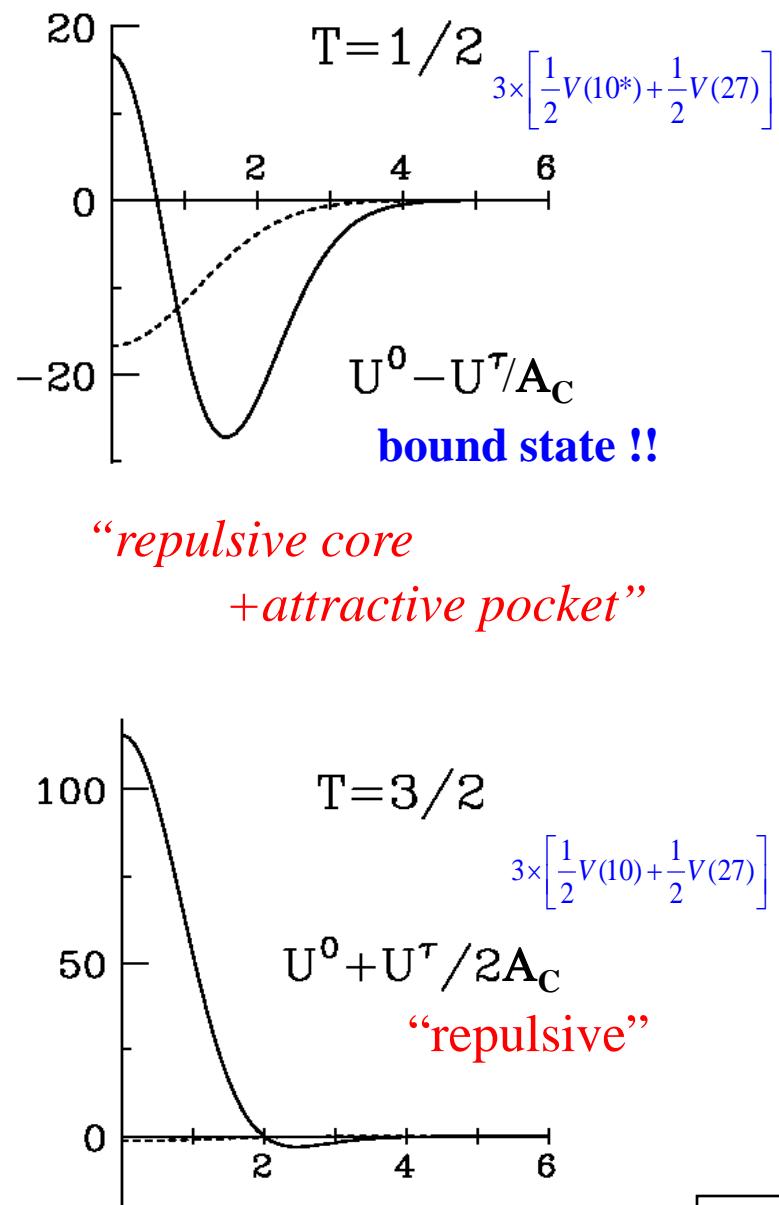
Strong Lane (isospin-dependent) potential and Coherent Λ - Σ coupling

Isospin dependence of the (3N)- Σ potentials

T.Harada, PRL81(1998)5287.



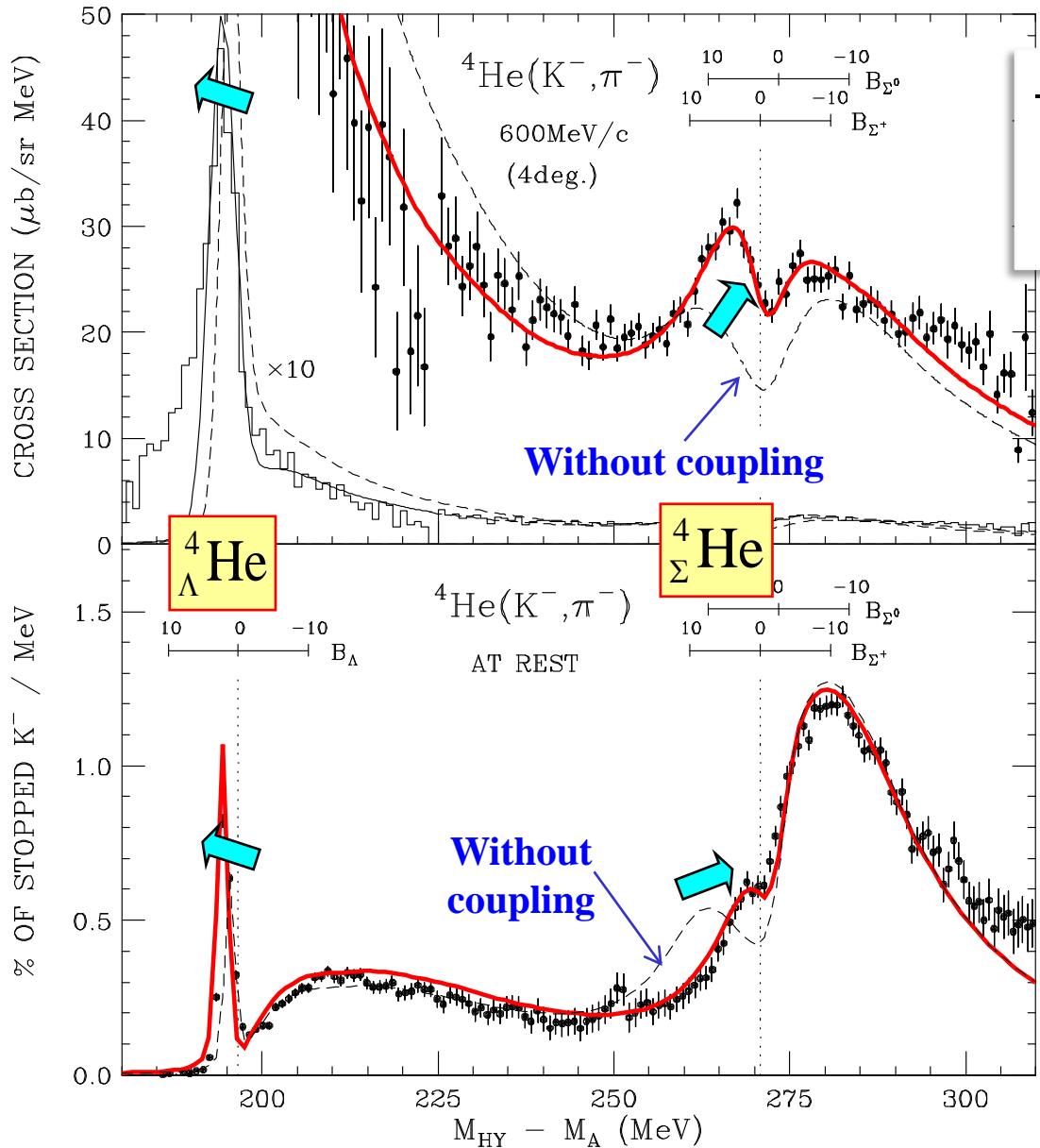
T.Harada, NPA507 (1990) 715.



Λ - Σ coupling effects on the (K^- , π^-) spectrum

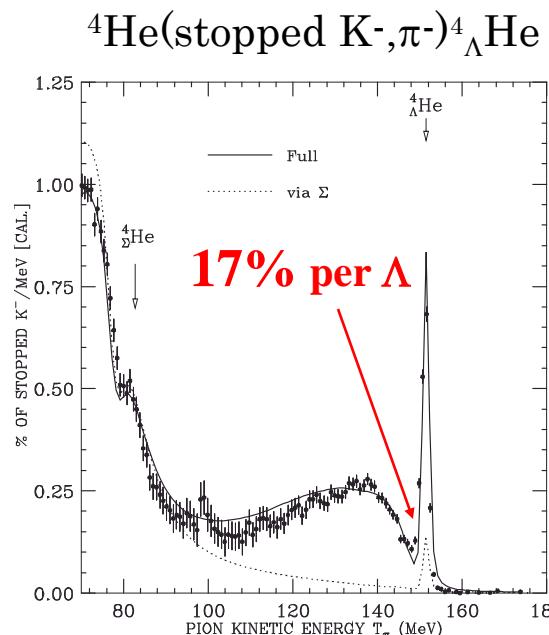
Hyperon-mixing

T.Harada, NPA507(1990)715.



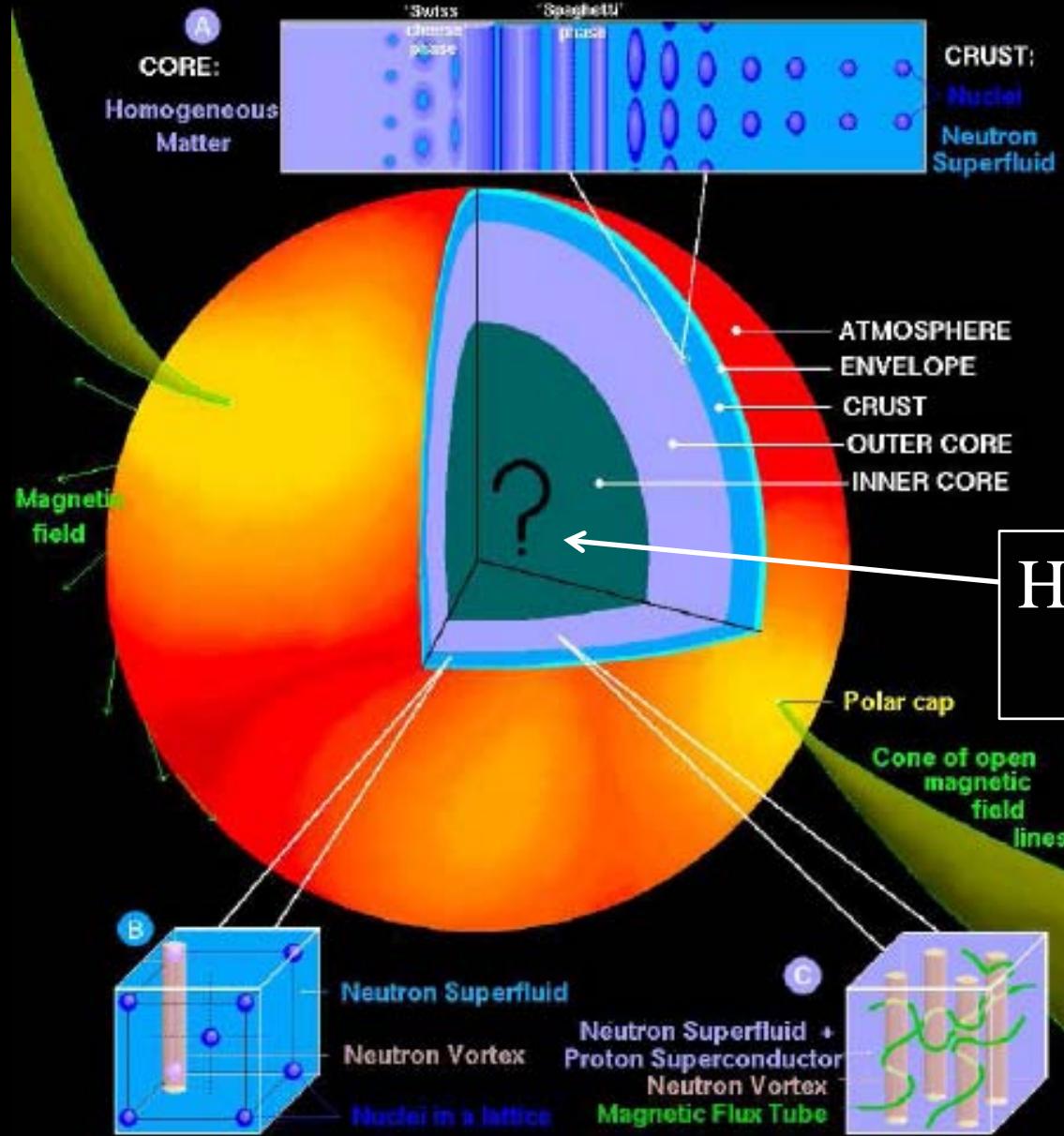
-The Λ - Σ coupling effects play a important role in reproducing the spectrum.

- The Λ state is produced via Σ components in the ground state.



3. 中性子星と高密度バリオン物質

A NEUTRON STAR: SURFACE and INTERIOR

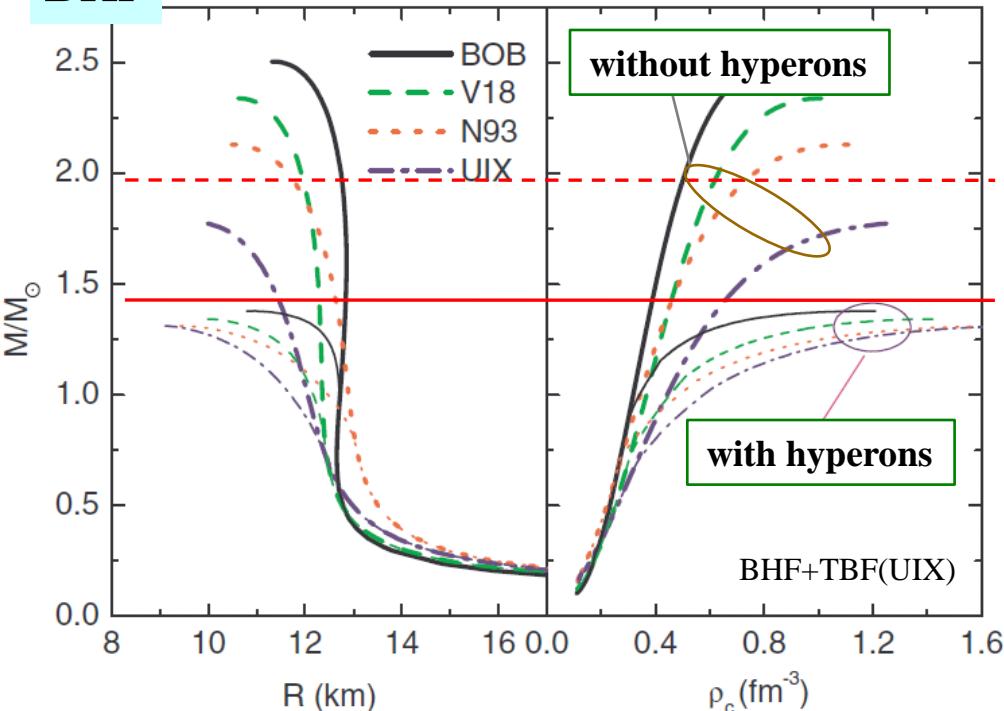


Hyperon mixing
 $\rho \sim (2-3) \rho_0$

中性子星の構造とEOS

BHF

Z.H.Li, H.-J.Schulze, PRC 78 (2008) 028801



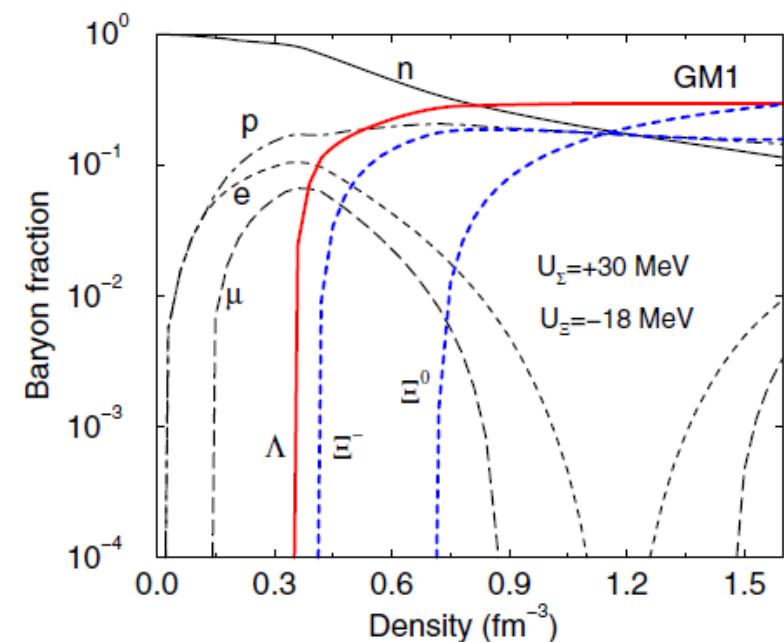
PSR J1614-2230

P. B. Demorest et al.,
Nature 467(2010)1081

最大質量の下限

RMF

J. Schaffner-Bielich,
NPA 835 (2010) 279



Softening on the EOS

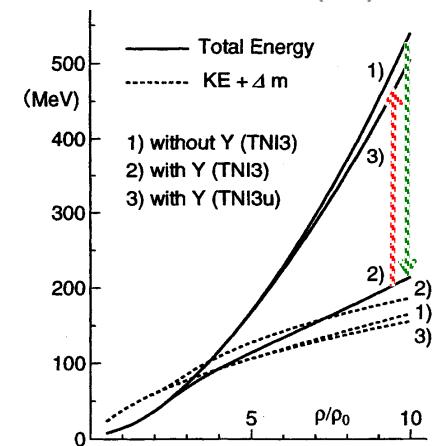
短距離斥力をハイペロン混合
により回避

$$n_c(Y) \approx (2-3)n_0$$

YN, YY: extra repulsion TNIu

$$M_{\max} > M_{\text{OBS}} \quad n_c(Y) \approx (4-5)n_0$$

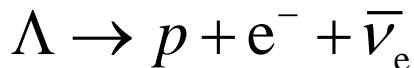
ハイペロン混合によって
強く影響



Thermal evolution of hyperon-mixed neutron stars

S. Tsuruta et al., *Astrophys. J* 691(2009)621

Rapid neutrino emission
via weak processes
(Direct/Modified Uruca)



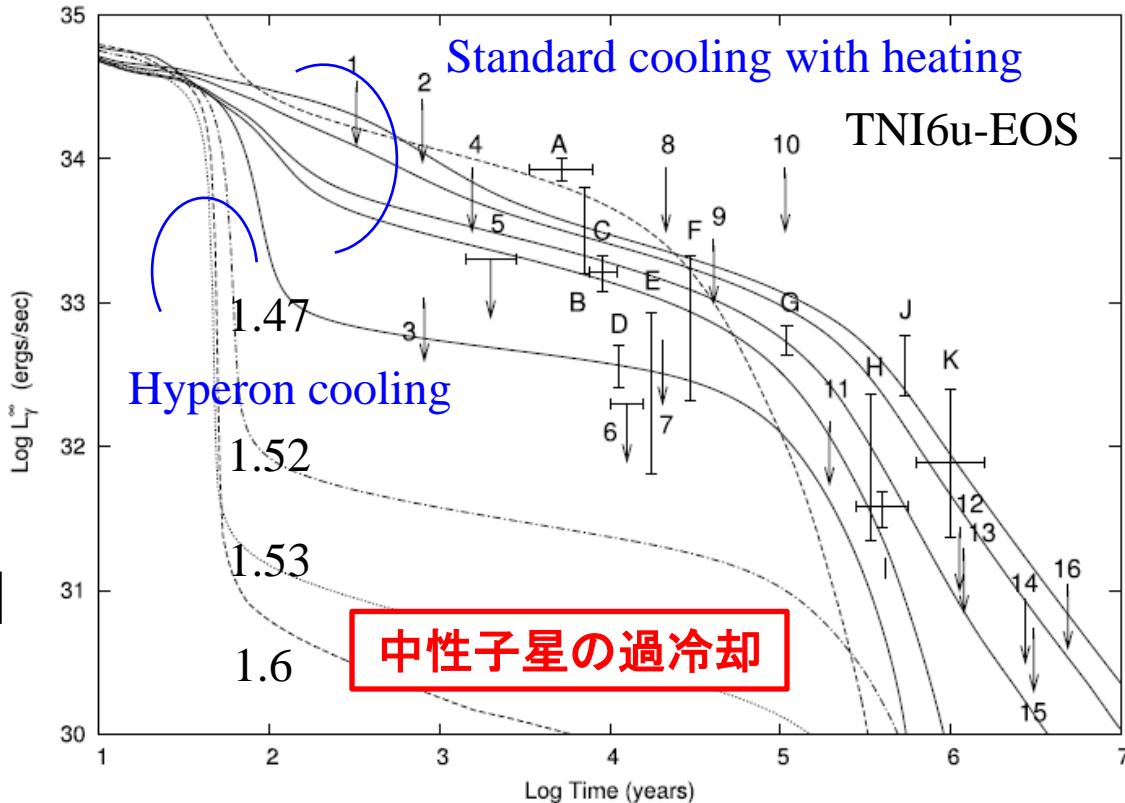
- Cooper pair
 1S_0 [inner crust]
 3P_2 - $^3F_2(n)$, $^1S_0(p)$ [core]
→ Standard cooling

- YY pairing
→ Hyperon cooling

Rapid coolingを抑制する役割

- Hyperon superfluidity v.s. YY interactions

Nagara event $\Delta B_{\Lambda\Lambda} \sim 0.7$ MeV → no $\Lambda\Lambda$ superfluidity ?



YN相互作用の強さ
によって強く影響

Multi-strange hadronic systemの存在可能性

Generalized Bethe-Weizsäcker mass formula

$$E_B(\{p, n\}) = -a_V^{(0)} A + a_S^{(0)} A^{2/3} + a_C^{(0)} \frac{Z}{A^{1/3}} + a_X^{(0)} \frac{(N-Z)^2}{A}$$

(unit in MeV)

$$a_V^{(0)} \rightarrow a_V - b_V^{(w)} w - b_V^{(y)} y$$

↓ ↓

18 0.72

(Set II) 16 28.7 -5.5 -4.75

$$a_X^{(0)} x^2 \rightarrow a_X x^2 + a_U u^2 + a_W w^2 + a_Y y^2 + a_{WY} w y$$

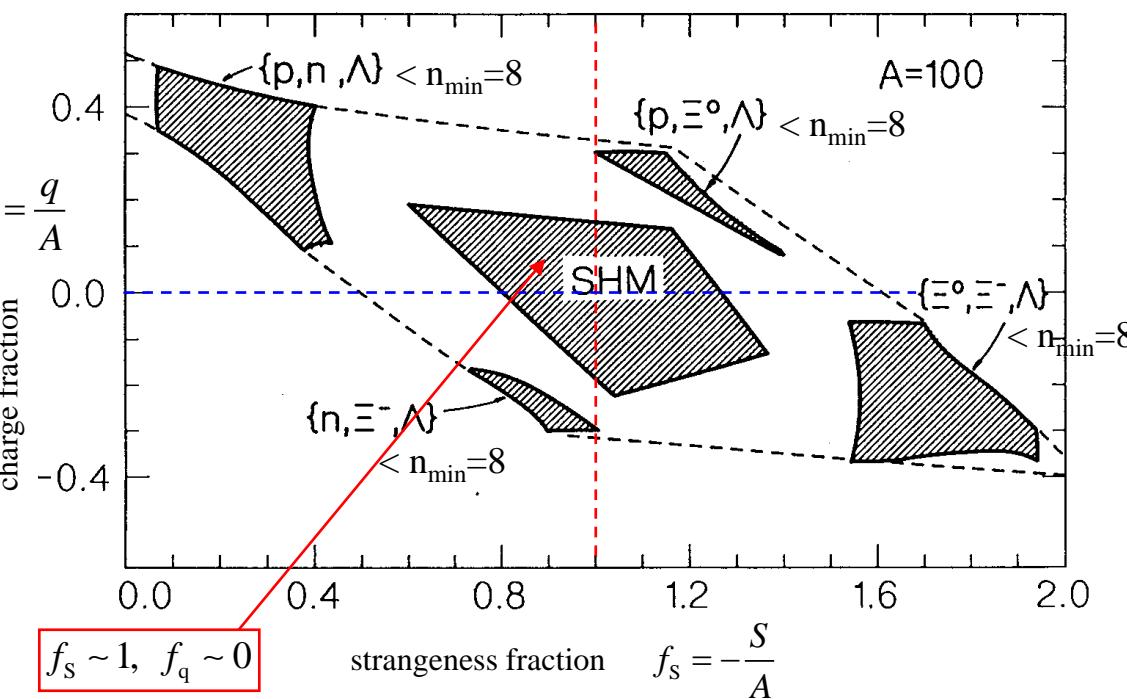
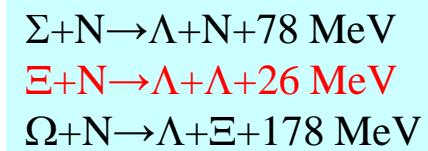
23 43 23.7 57.1 45 7.7

$$E_B / A \rightarrow -28.3 \text{ MeV}, f_s \rightarrow 0.96, f_q \rightarrow 0$$

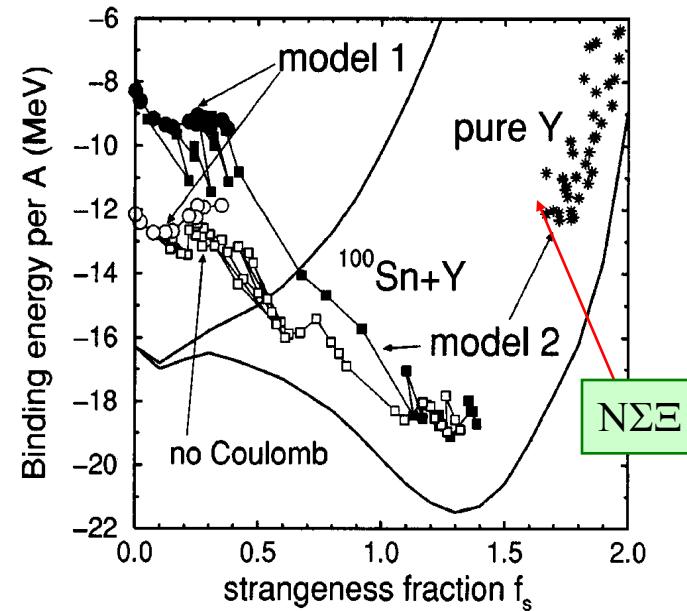
S. Balberg, A. Gal, J. Schaffner, PTP117(1994)325

$$x = (N-Z)/A, \quad y = [(N+Z+\Xi^0+\Xi^-)/4 - \Lambda]/A$$

$$u = (\Xi^0 - \Xi^-)/A, \quad w = [(N+Z)/2 - (\Xi^0 + \Xi^-)/2]/A$$



RMF J. Schaffner-Bielich, A. Gal,
PRC62(2000)034311



4. $S = -2$ の原子核

Ξ ハイパー核

■ Ξ single-particle potentialの性質

(K⁻,K⁺)反応スペクトルの解析

Ξ -原子のX線の測定へ

■(K⁻,K⁺)反応による Ξ ハイパー核の生成

$\Lambda\Lambda$ ハイパー核

■エマルジョンによる $\Lambda\Lambda$ ハイパー核の発見

$\Lambda\Lambda$ bond energy

■ $\Lambda\Lambda$ - Ξ coupled channel approach

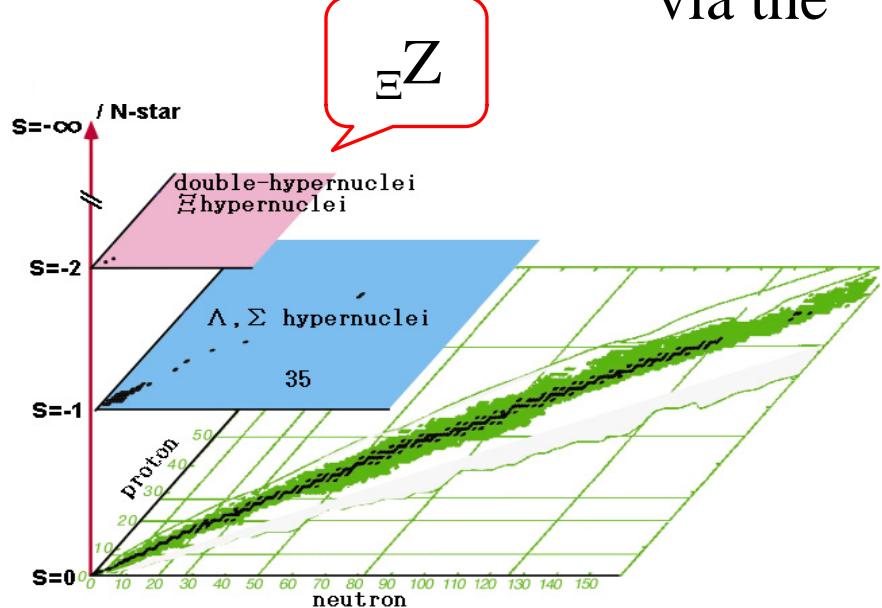
■(K⁻,K⁺)反応による $\Lambda\Lambda$ ハイパー核の励起状態の生成

Ξ ハイパー核

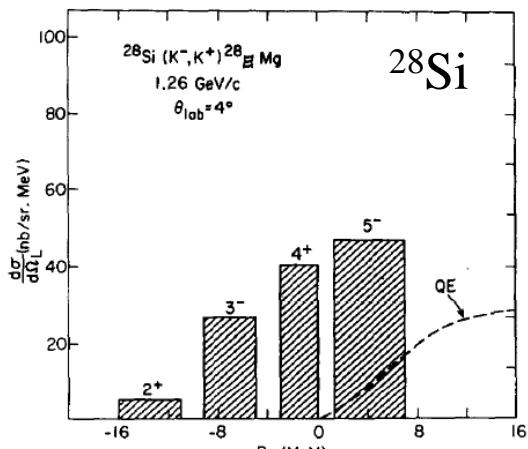
E03,E05@J-PARC

E03 Measurement of X rays from Ξ - atom

E05: Spectroscopic study of Ξ -hypernucleus, $^{12}_{\Xi}\text{Be}$
via the $^{12}\text{C}(\text{K}-,\text{K}+)$ reaction (Day-1)



Studies of Ξ^- hyperon interaction with the nucleus



Ξ -hypernuclei via (K-,K+) reactions

C.B. Dover, A.Gal, Ann. Phys. 146 (1989) 309.

V_Ξ ?

Analysis of the nuclear $\text{K}^-\text{p} \rightarrow \text{K}^+\Xi^-$ reaction
The potential depth parameters is obtained by

$$V_\Xi^0 = -24 \pm 4 \text{ MeV} \quad \text{for} \quad r_0 = 1.1 \text{ fm} \quad (W_\Xi^0 \approx -1 \text{ MeV})$$

DWIA analysis of $^{12}\text{C}(\text{K}^-, \text{K}^+)$ data at 1.8GeV/c

T.Iijima et al., NPA546(1992)588.

Tadokoro et al., PRC51(1995)2656

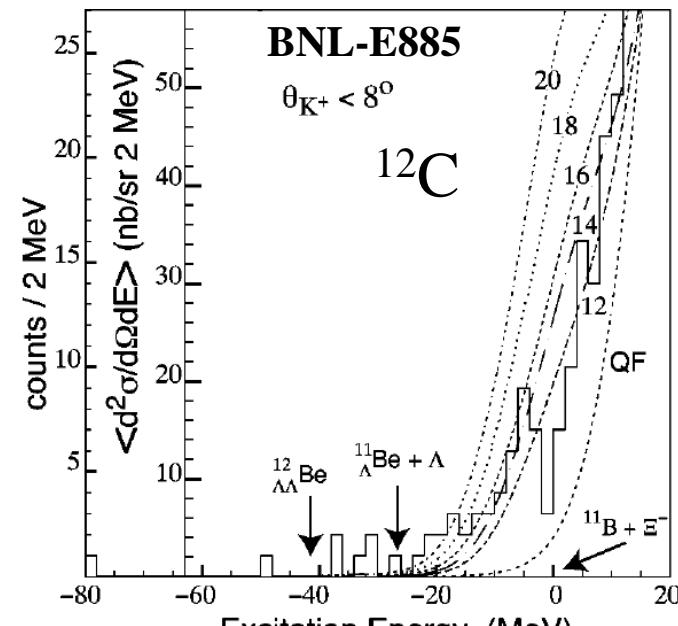
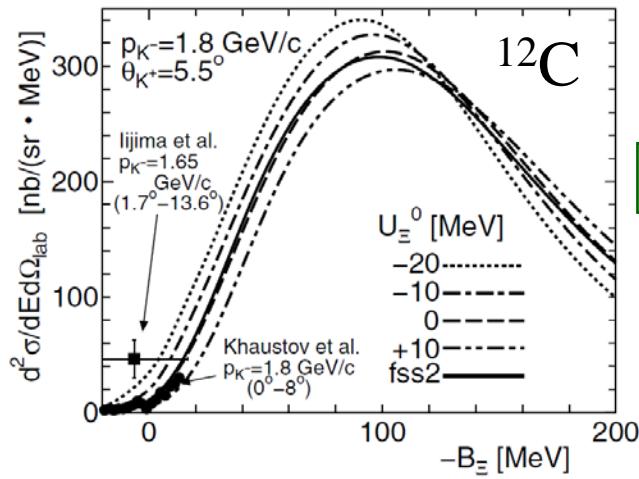
Analysis of $^{12}\text{C}(\text{K}^-, \text{K}^+)$ spectrum suggests

P.Khaustov et al., PRC61(2000)054603

Comparison with the data in the Ξ bound region

$$V_\Xi^0 \approx -16 \text{ MeV}$$

$$V_\Xi^0 \approx -14 \text{ MeV}$$



Semi-Classical Distorted Wave Model Analysis

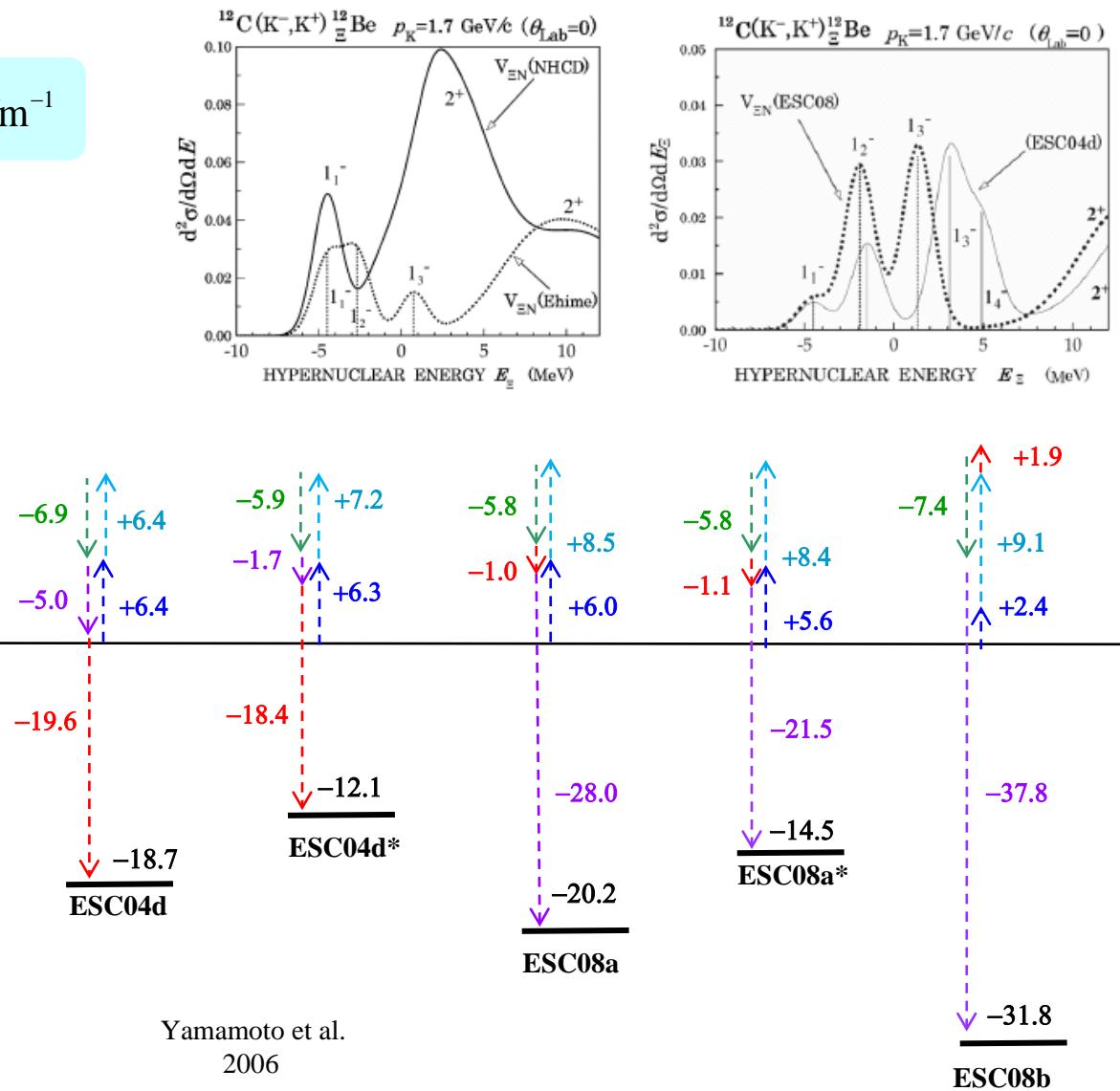
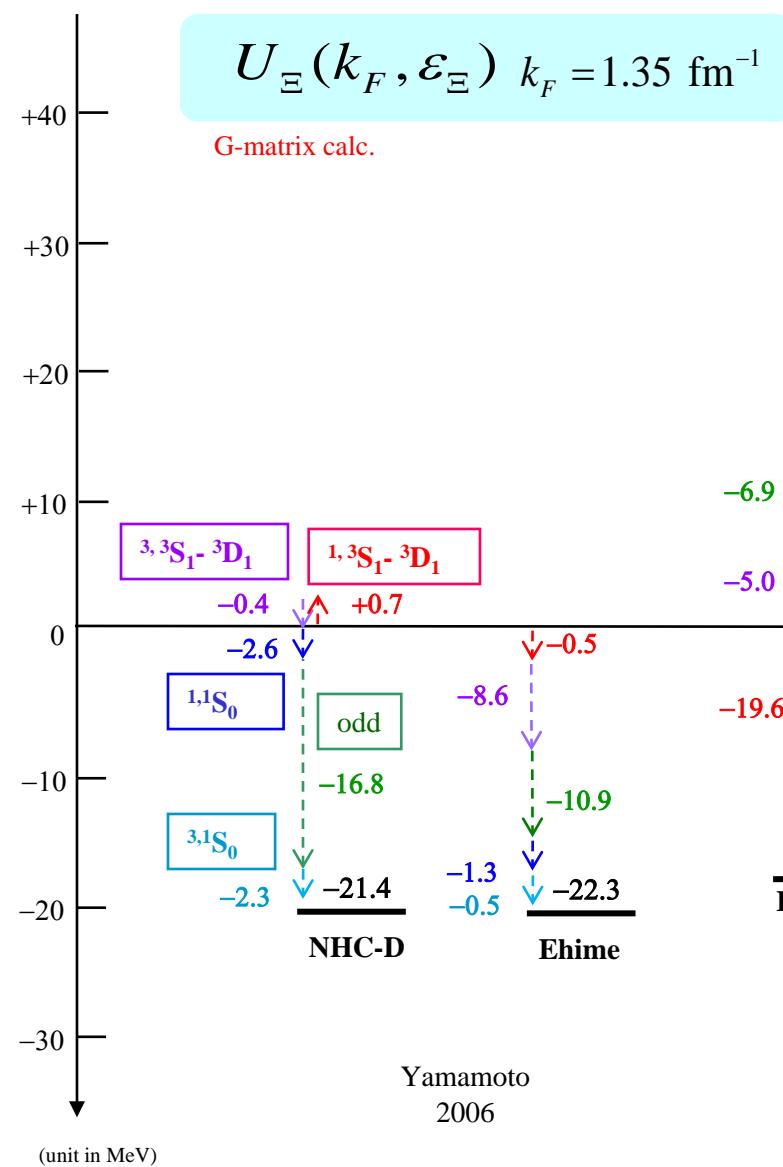
M. Kohno et al., PTP123(2010)157; NPA835(2010)358.

$$V_\Xi^0 = -20, -10, 0, +10, +20 \text{ MeV}$$

↔ fss2

E⁻ s.p. energies in symmetric nuclear matter

T.Motoba, S.Sugimoto, NPA835(2010)223.



Yamamoto et al.
2006

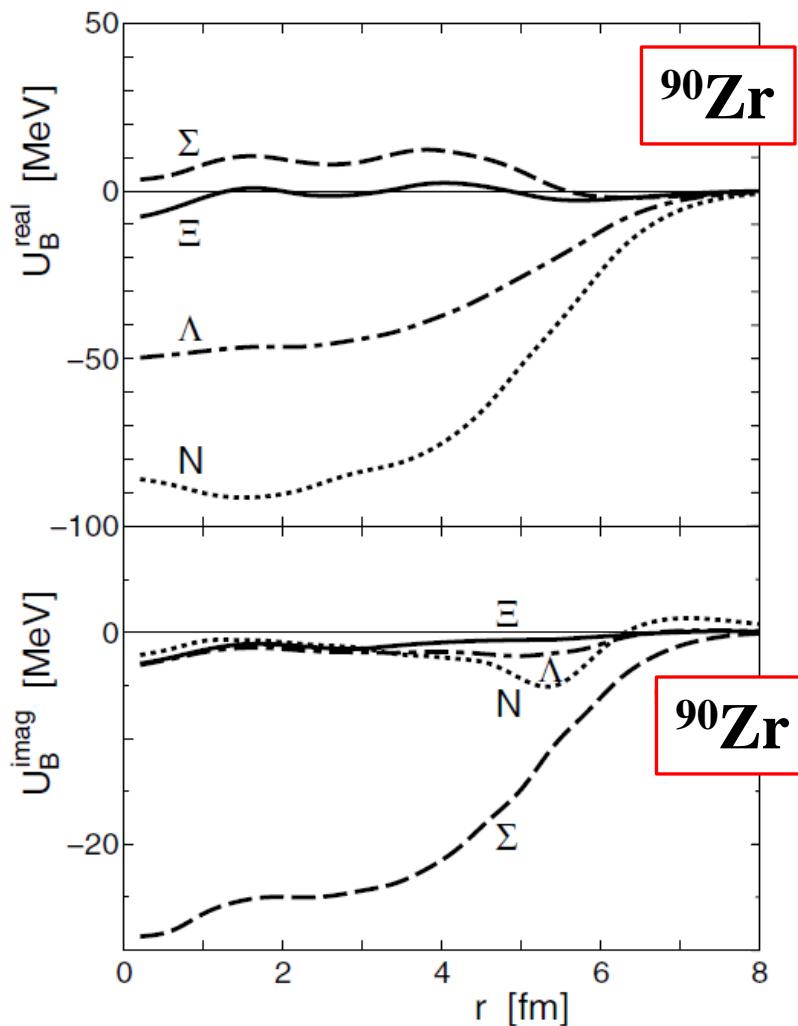
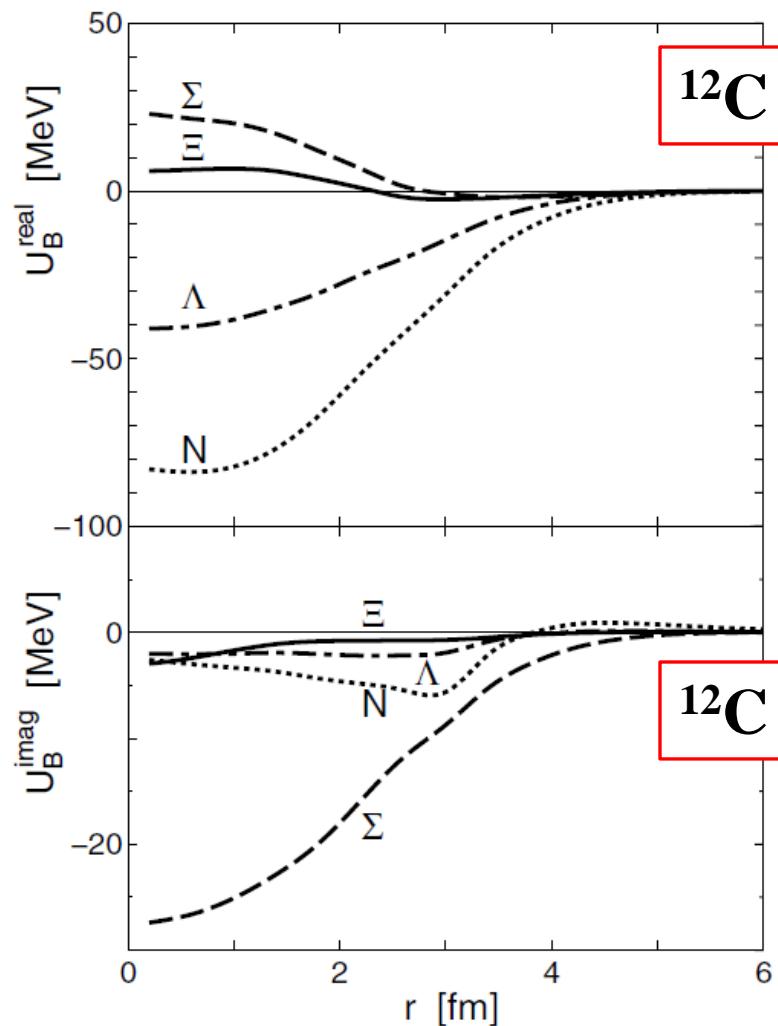
Rijken-Yamamoto
2009

Hyperon s.p. potentials in finite nuclei

G-matrix+local density approximation

M. Kohno, Y. Fujiwara, PRC79(2009)054318.

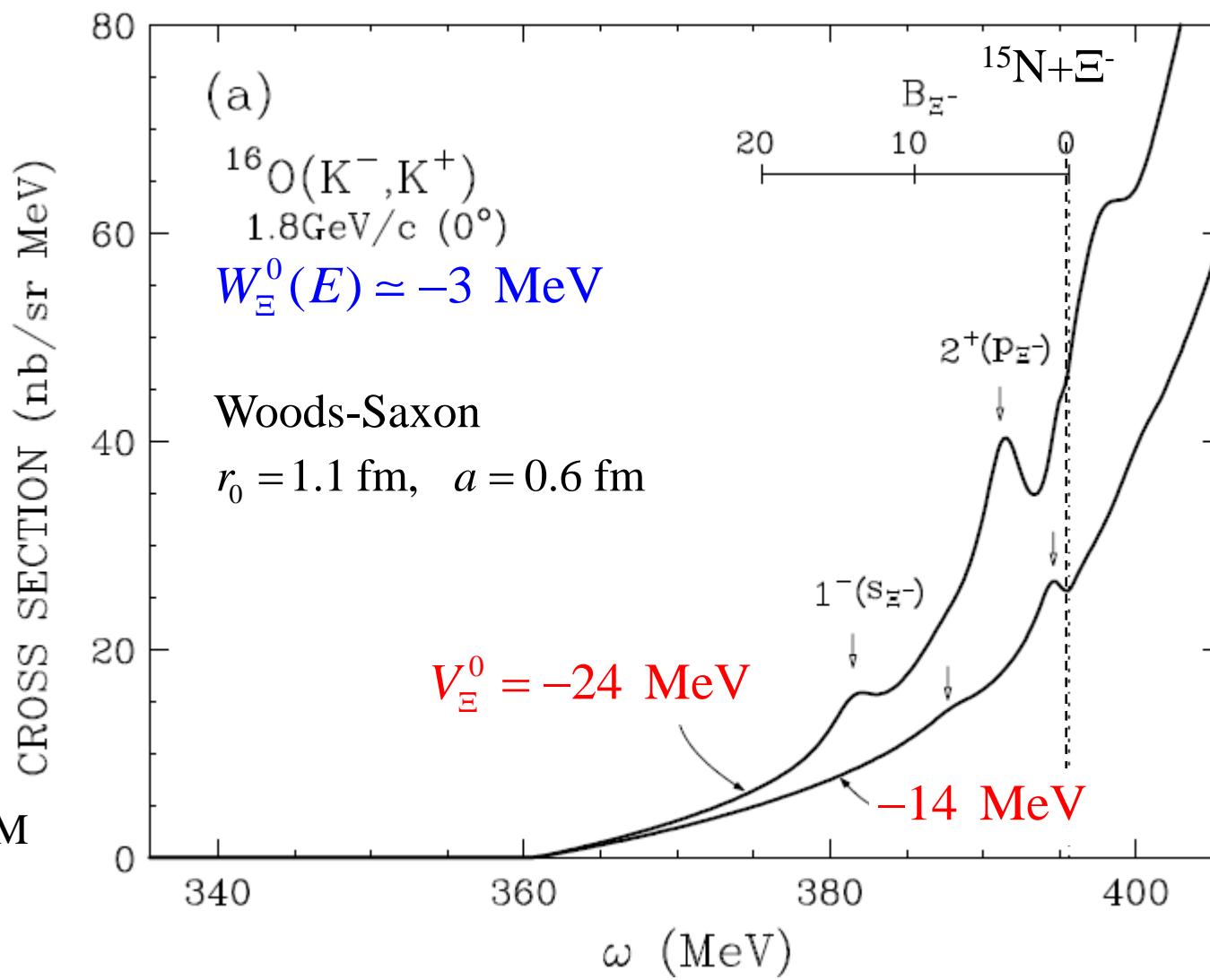
fss2 : SU_6 quark-model BB interaction by Kyoto-Niigata group



Ξ^- spectrum in DCX (K^-, K^+) reactions at 1.8GeV/c

T. Harada, Y. Hirabayashi, A. Umeya, PLB690(2010)363.

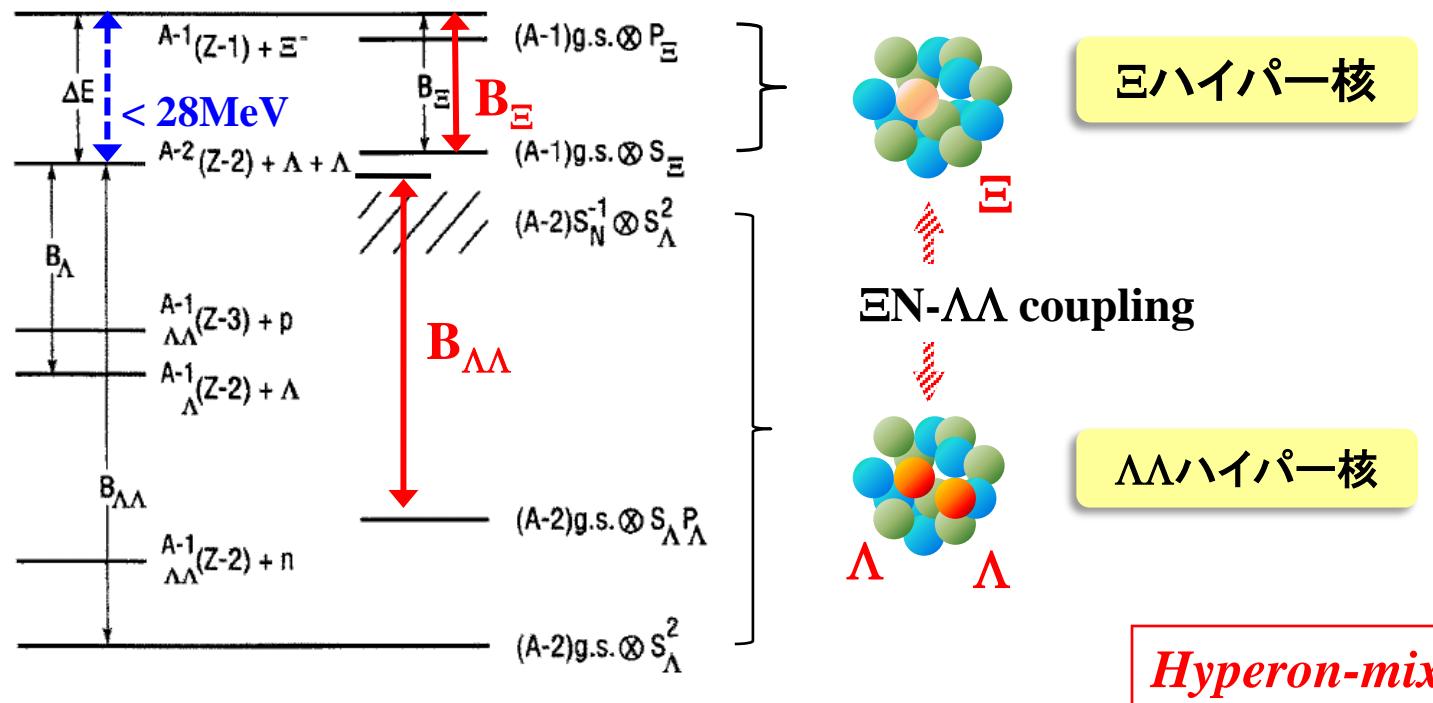
^{16}O



- Spin-stretched Ξ^- states can be populated due to the high momentum transfer.

$$ds/d\Omega [{}^{15}\text{N}(1/2^-) \otimes s_\Xi](1-) = 6 \text{ nb/sr}, \quad ds/d\Omega [{}^{15}\text{N}(1/2^-) \otimes p_\Xi](2+) = 9 \text{ nb/sr} \quad \text{for } V_\Xi = -14 \text{ MeV.}$$

ΛΛハイパー核

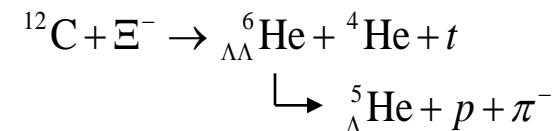
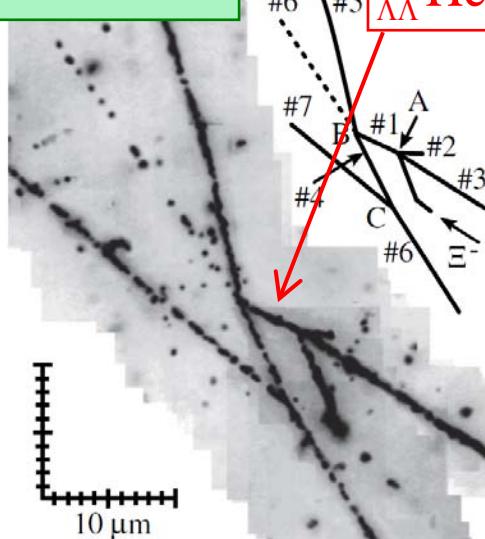


E07@J-PARC

E07: Systematic study of **double strangeness system** with an emulsion-counter hybrid method

Observation of $\Lambda\Lambda$ Hypernuclei in E176/E373 Hybrid Emulsion

NAGARA

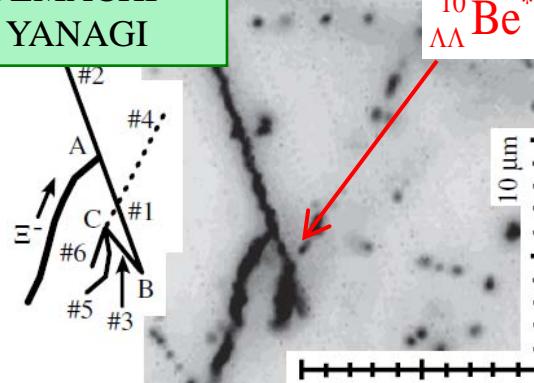


$$2M_\Lambda - B_{\Lambda\Lambda} < M_H$$

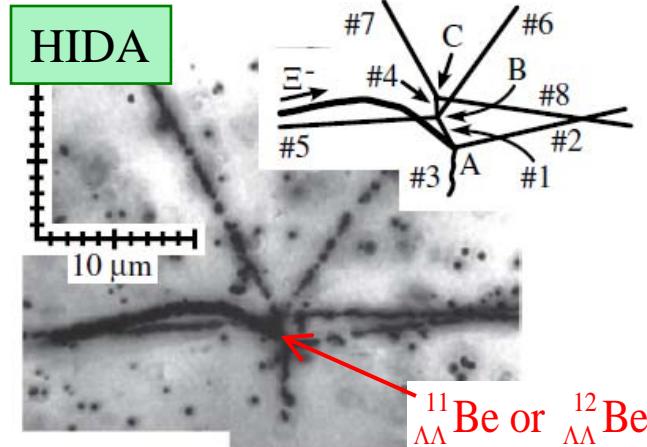
H-dibaryon

Jaffe, PRL38(1977)195

DEMACHI-YANAGI



HIDA



$\Lambda\Lambda$ bound energy

$$\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^A Z) = B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^A Z) - 2B_\Lambda({}_{\Lambda}^{A-1} Z)$$

Hiyama et al.
PRL104(2010)212502

$B_{\Lambda\Lambda}^{\text{Cal}} [\text{MeV}]$
(6.91)

11.88
18.23

14.74

| event | ${}_{\Lambda\Lambda}^A Z$ | Target | $B_{\Lambda\Lambda}$ [MeV] | $\Delta B_{\Lambda\Lambda}$ [MeV] |
|------------------|--|-------------------|----------------------------|-----------------------------------|
| NAGARA | ${}_{\Lambda\Lambda}^6\text{He}$ | ${}^{12}\text{C}$ | 6.91 ± 0.16 | 0.67 ± 0.17 |
| MIKAGE | ${}_{\Lambda\Lambda}^6\text{He}$ | ${}^{12}\text{C}$ | 10.06 ± 1.72 | 3.82 ± 1.72 |
| DEMACHIYANAGI | ${}_{\Lambda\Lambda}^{10}\text{Be}$ | ${}^{12}\text{C}$ | 11.90 ± 0.13 | -1.52 ± 0.15 |
| HIDA | ${}_{\Lambda\Lambda}^{11}\text{Be}$ | ${}^{16}\text{O}$ | 20.49 ± 1.15 | 2.27 ± 1.23 |
| | ${}_{\Lambda\Lambda}^{12}\text{Be}$ | ${}^{14}\text{N}$ | 22.23 ± 1.15 | — |
| E176 | ${}_{\Lambda\Lambda}^{13}\text{B}$ | ${}^{14}\text{N}$ | 23.3 ± 0.7 | 0.6 ± 0.8 |
| Danysz et al[17] | ${}_{\Lambda\Lambda}^{10}\text{Be}({}_{\Lambda}^9\text{Be}^*)$ | ${}^{14}\text{N}$ | 14.7 ± 0.4 | 1.3 ± 0.4 |

H.Takahashi et al., PRL87(2001)212502

K.Nakazawa , NPA 835 (2010)207

K.Nakazawa , H.Takahashi,NPA 835 (2010)207

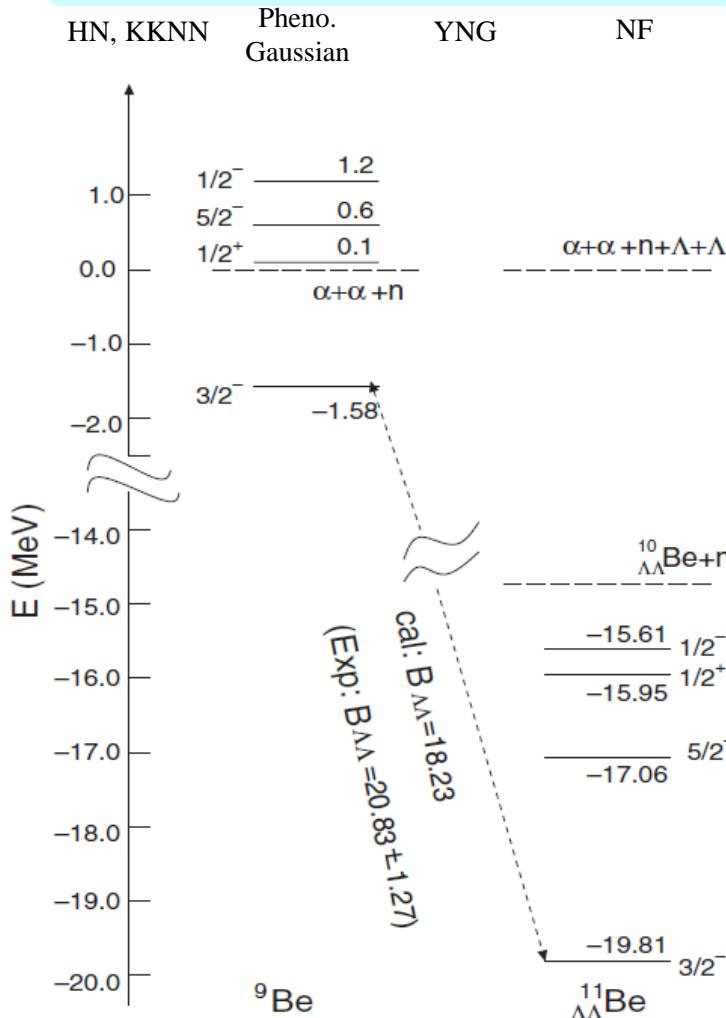
$\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^6\text{He}) \simeq 4.7 \rightarrow 1.01 \rightarrow 0.67$ “weak attractive”
Prowse, 1966 Nagara,2001 Ξ mass update

Five-body Cluster Calculations of the $\Lambda\Lambda$ Hypernucleus

E. Hiyama et al., PRL104(2010)212502

$$^{11}_{\Lambda\Lambda}\text{Be} = \alpha + \alpha + n + \Lambda + \Lambda$$

OCM + 3BF + Λ N pot. + $\Lambda\Lambda$ pot.



The subsystems are reproduced:

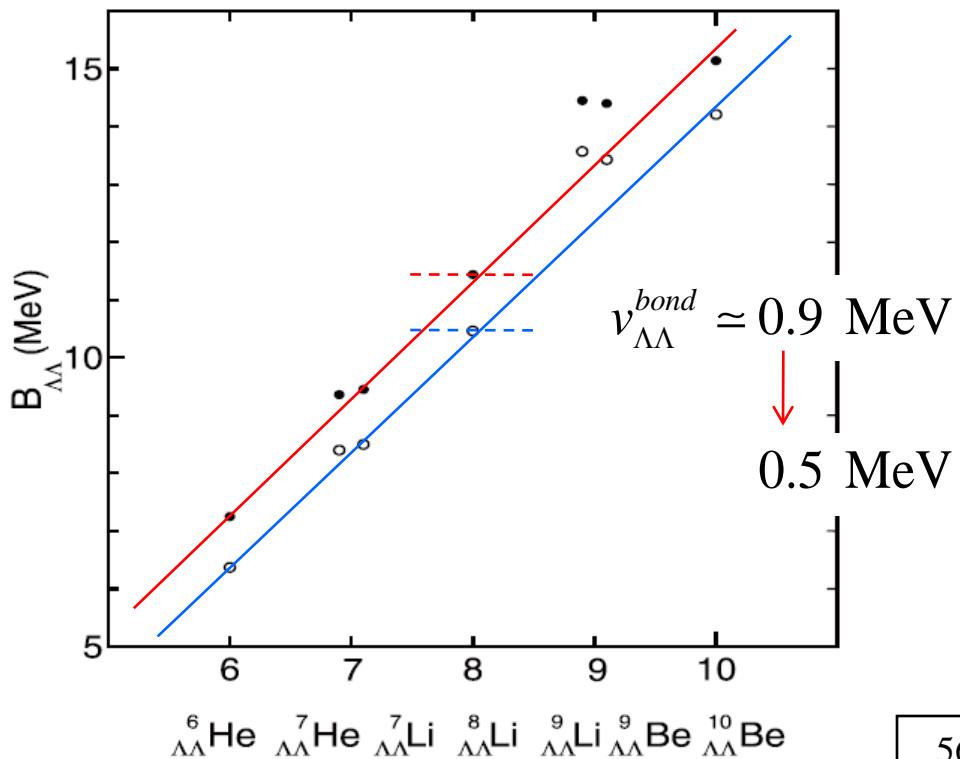
$$^{6}_{\Lambda\Lambda}\text{He} = \alpha + \Lambda + \Lambda \quad B_{\Lambda\Lambda}^{\exp.}(0^+_1) = 6.91 \text{ MeV}$$

$$^{10}_{\Lambda\Lambda}\text{Be} = \alpha + \alpha + \Lambda + \Lambda \quad B_{\Lambda\Lambda}^{\exp.}(2^+_1) = 11.88 \text{ MeV}$$

$\Lambda\Lambda$ bound energy

$$\mathcal{V}_{\Lambda\Lambda}^{\text{bond}}(^A_{\Lambda\Lambda}\text{Z}) \equiv B_{\Lambda\Lambda}(^A_{\Lambda\Lambda}\text{Z}) - B_{\Lambda\Lambda}(^A_{\Lambda\Lambda}\text{Z}; V_{\Lambda\Lambda} = 0)$$

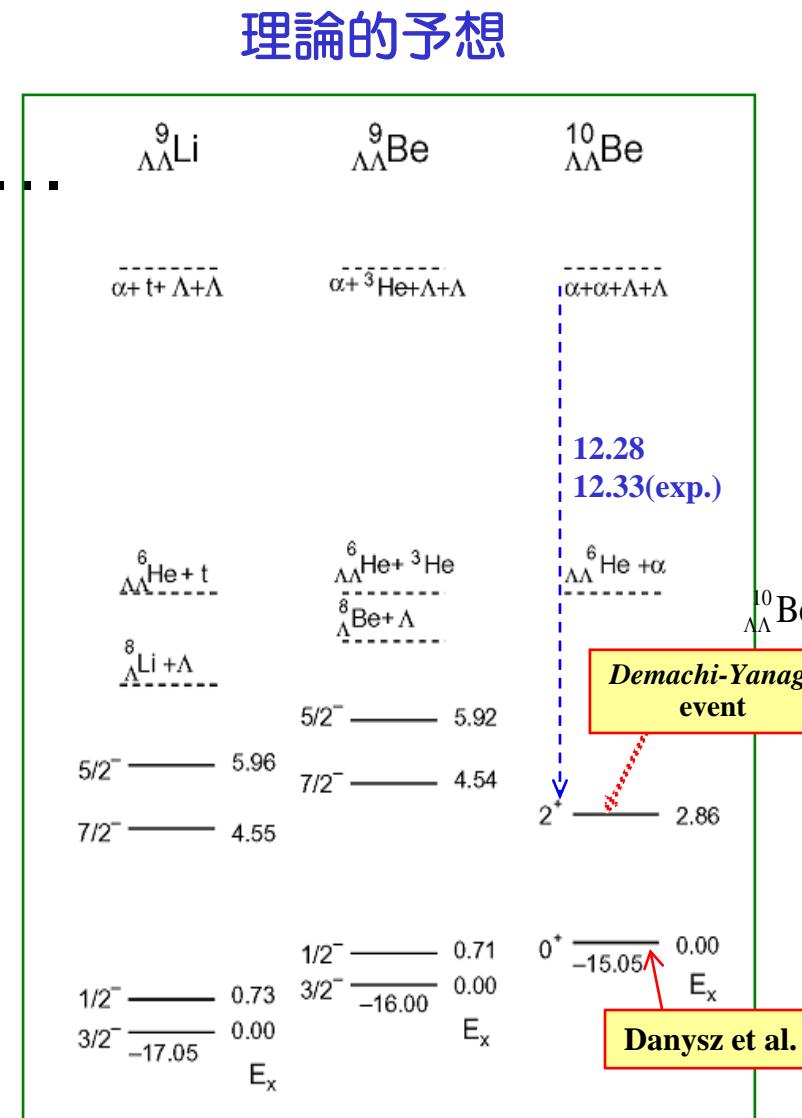
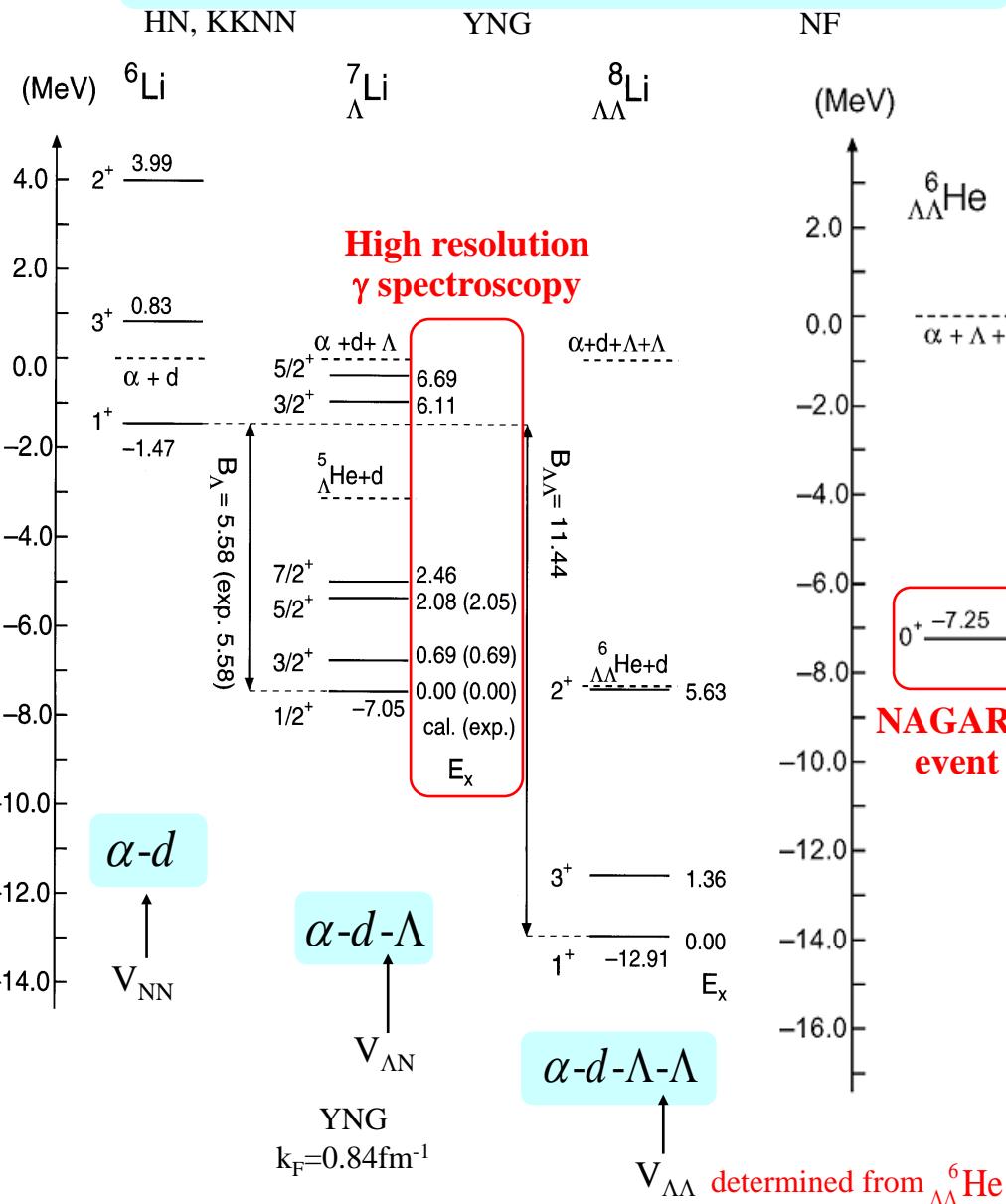
E. Hiyama et al., PTPS183(2010)152



Cluser-Model Calculations for A=6-10 ΛΛ Hypernuclei

E. Hiyama et al, PRC 66(2002)024007

OCM+ΛN potential+ΛΛ potential

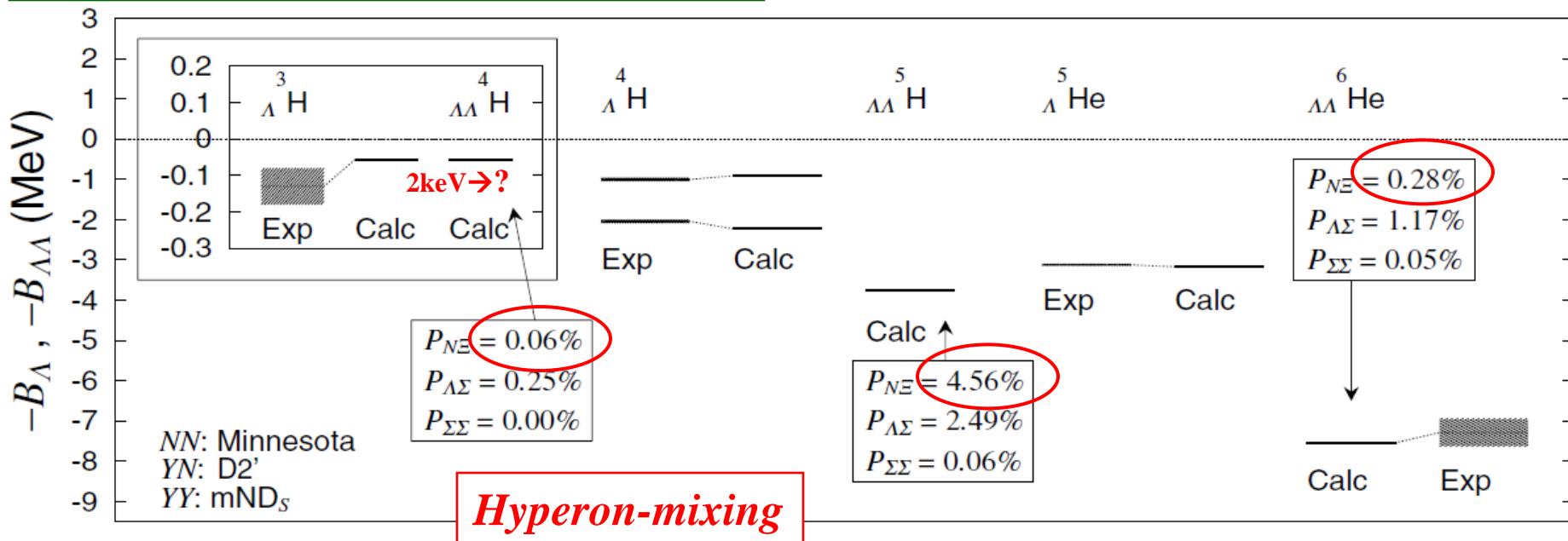


Coupled Channel Approach to Doubly Strange Hypernuclei

Ab initio calculations by SVM

H. Nemura et al.,
PRL94(2005)202502

$\Delta B_{\Lambda\Lambda} ({}^6_{\Lambda\Lambda}\text{He}) \simeq 1.01 \rightarrow 0.67$
Nagara,2001 Ξ mass update



$\alpha\Xi N$ - $\alpha\Lambda\Lambda$ coupled-channel calculations

T. Yamada, PRC69(2004)044301.

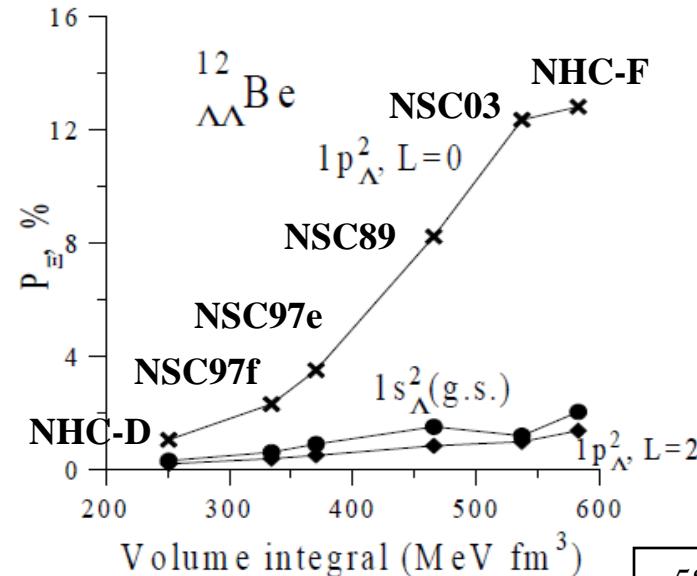
Y. Yamamoto and Th.A. Rijken, PRC69(2004)014303.

$\Lambda\Lambda$ - ΞN s-wave: $P(\Xi) < 1\%$

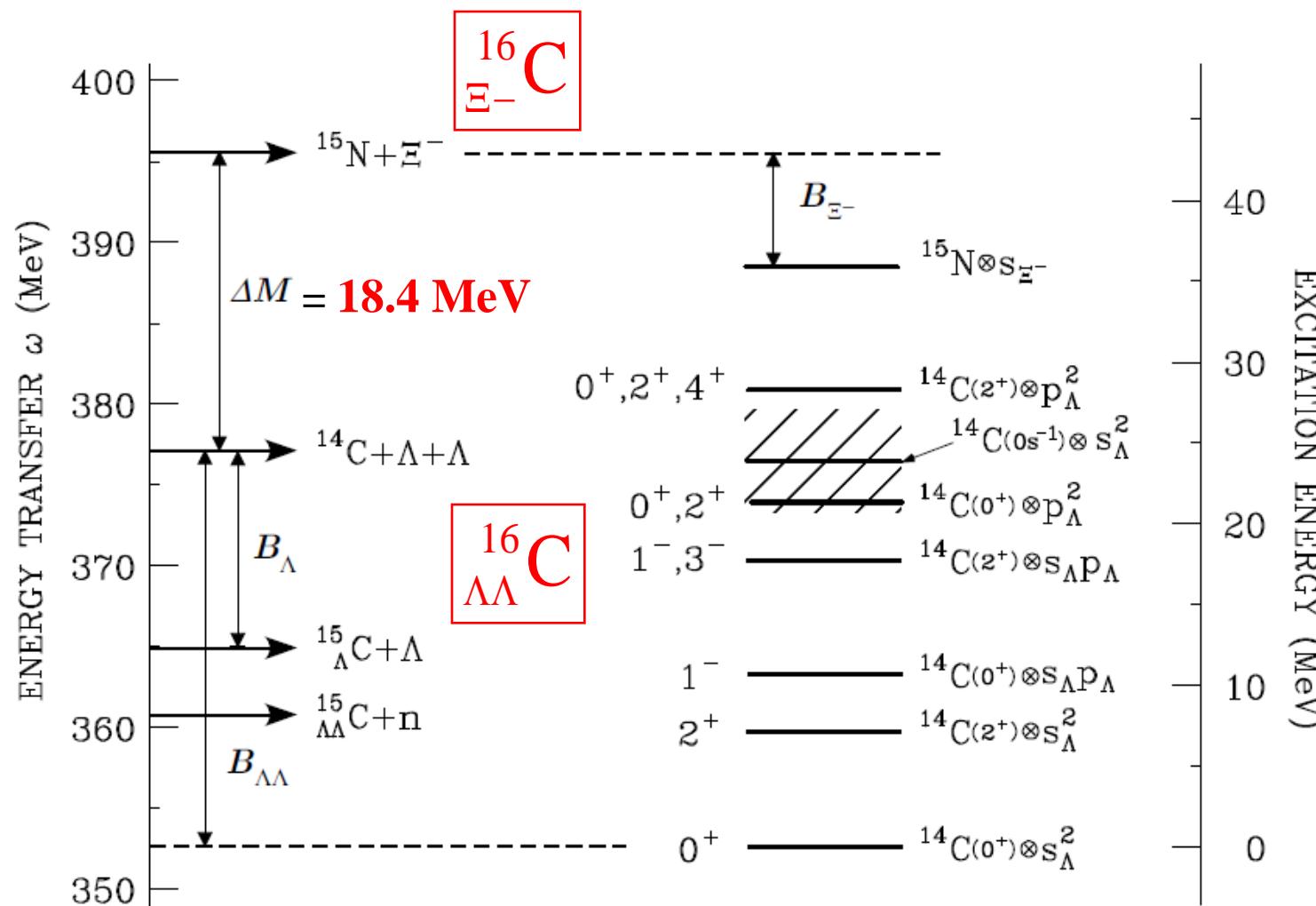
$\Xi\Lambda\Lambda$ coupled-channel calculations

D. E. Lanskoy and Y. Yamamoto, PRC69(2004)014303.

$1s_\Lambda^2$: $P(\Xi) < 1\%$, $1s_\Lambda 1p_\Lambda$: $P(\Xi) \sim 10\%$



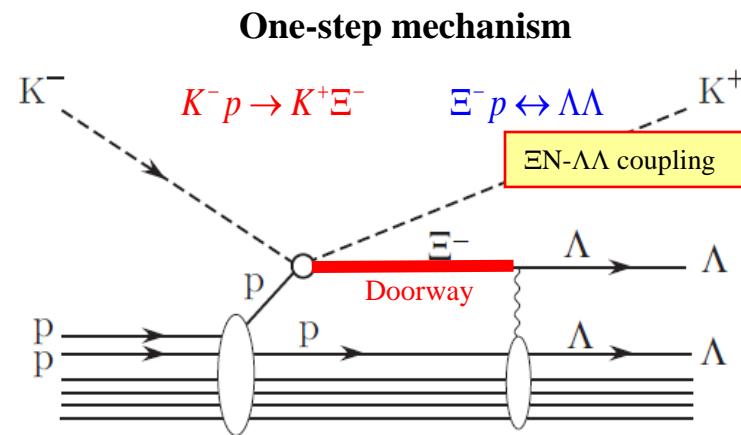
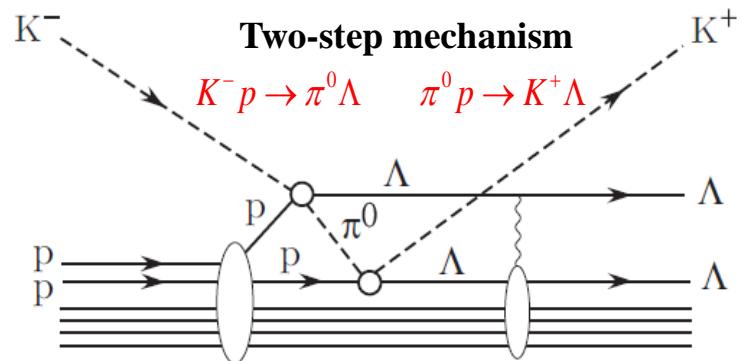
Energy spectrum of Ξ^- and $\Lambda\Lambda$ nuclei on a ^{16}O target



- . The energy shifts $\Delta B_{\Lambda\Lambda}$ are not taken into account.

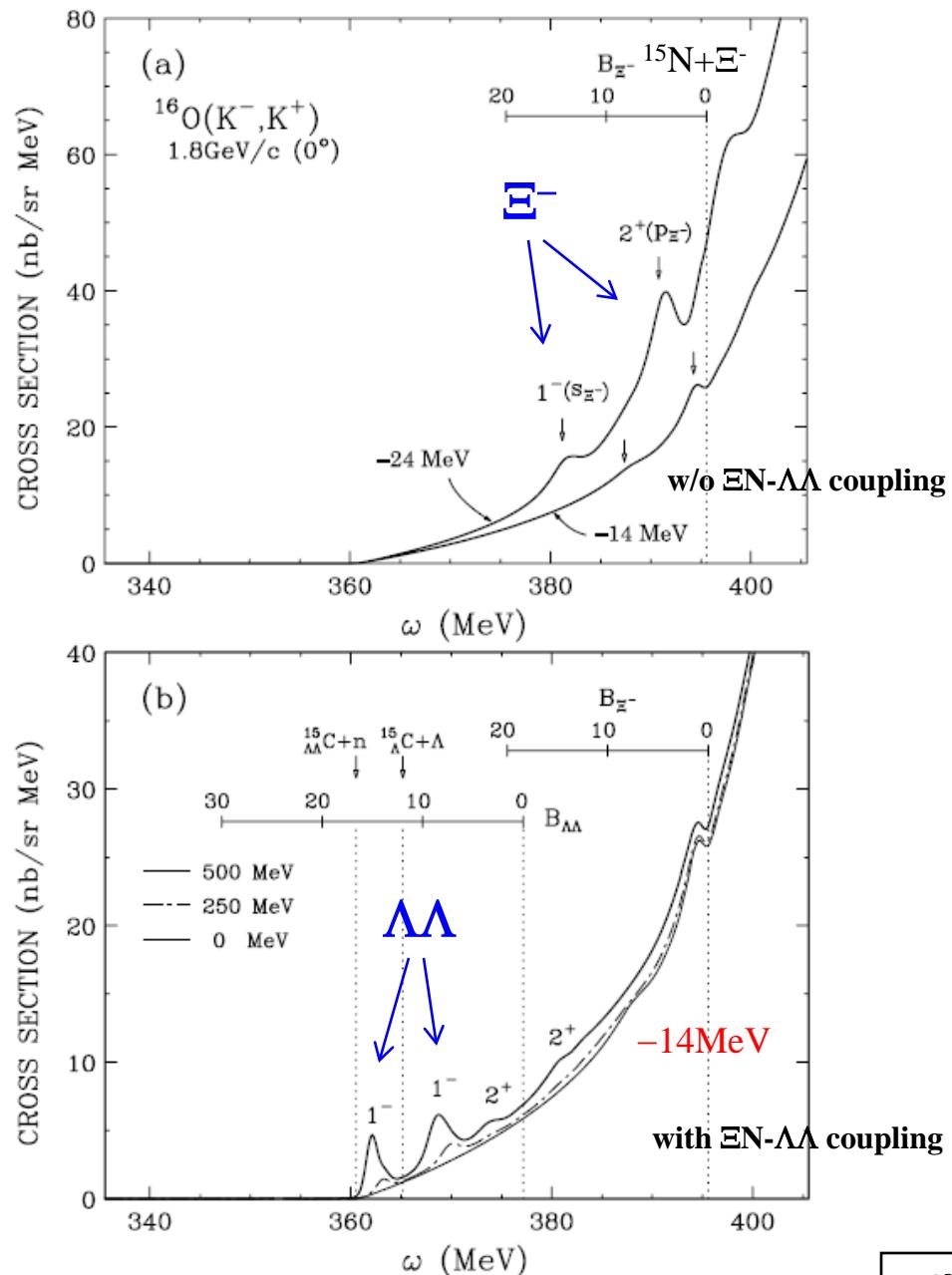
See also Dover, Gal and Millener, NPA572(1994) 85.

Ξ - $\Lambda\Lambda$ spectrum in DCX (K^- , K^+) reactions at 1.8GeV/c



Hyperon-mixing

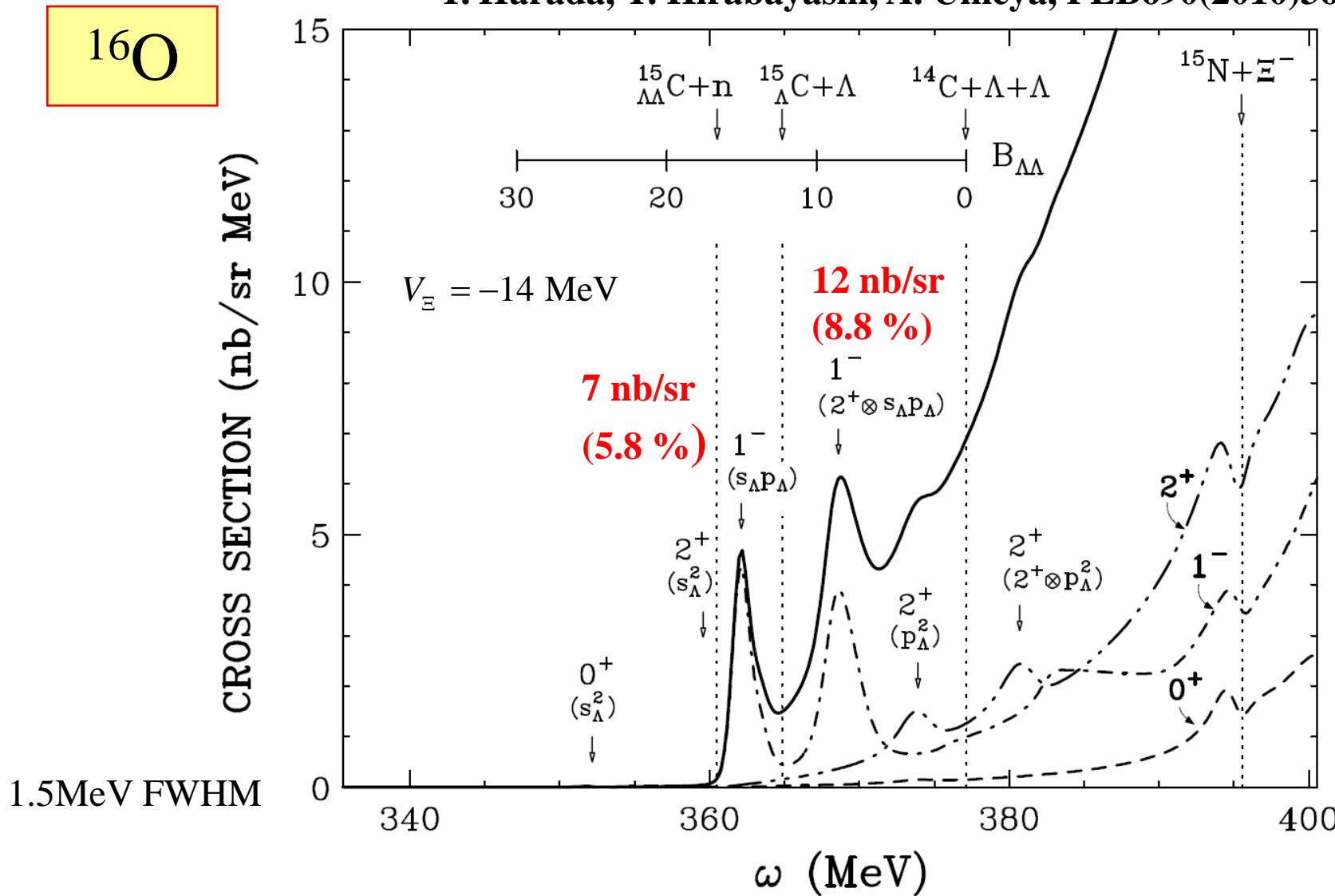
16O



[T. Harada, Y. Hirabayashi, A. Umeya, PLB690(2010)363]

E⁻ spectrum in DCX (K^-, K^+) reactions at 1.8GeV/c

T. Harada, Y. Hirabayashi, A. Umeya, PLB690(2010)363.

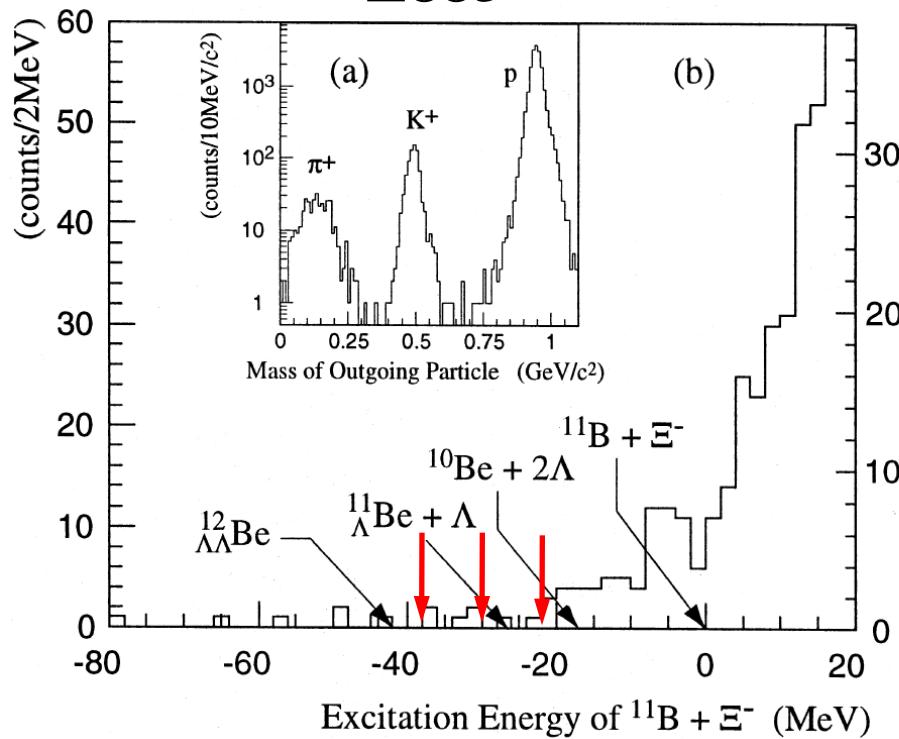


The large momentum transfer $q_{\Xi^-} \simeq 400 \text{ MeV}/c$ leads to the spin-stretched Ξ^- doorways states followed by $[^{15}\text{N}(1/2^-, 3/2^-) \otimes s_{\Xi^-}]1^- \rightarrow [^{14}\text{C}(0^+, 2^+) \otimes s_{\Lambda}p_{\Lambda}]1^-$

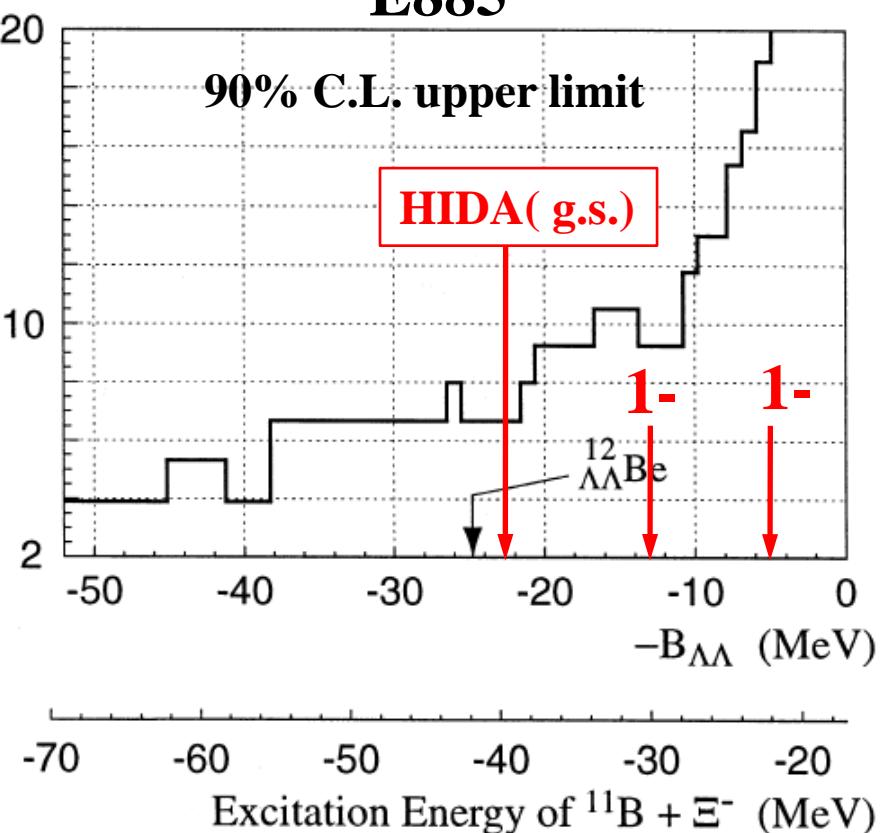
Search for $\Lambda\Lambda$ hypernuclei in the (K^-, K^+) reaction on ^{12}C

K. Yamamoto et al. (E885 Collaboration), PLB478(2000)401.

E885



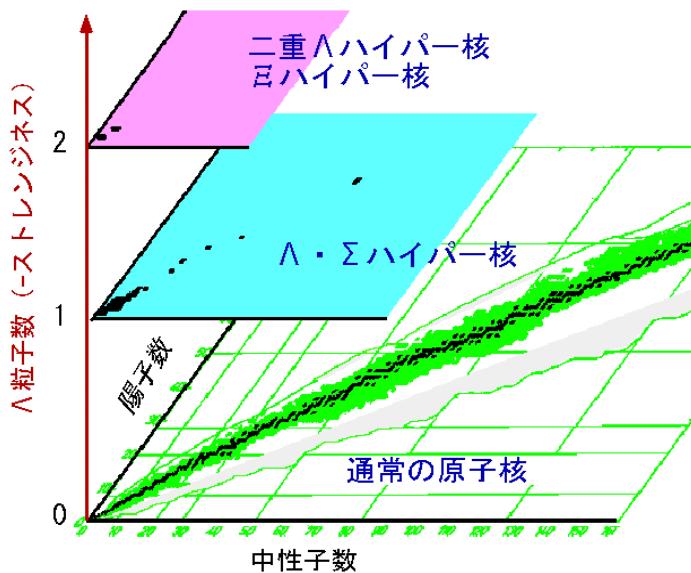
E885



Harada, Hirabayashi, Umeyaの計算値と矛盾しない!!

Remark

Studies of the DCX reactions (π^+, K^-), (K^-, K^+)
for hypernuclear productions
are
very important and promising .



■ Future subjects:

More microscopic calculations based on YN, YY potentials are needed to compare them with the forthcoming experimental data at J-PARC.

5. $K^{\bar{b}a}$ 中間子原子核

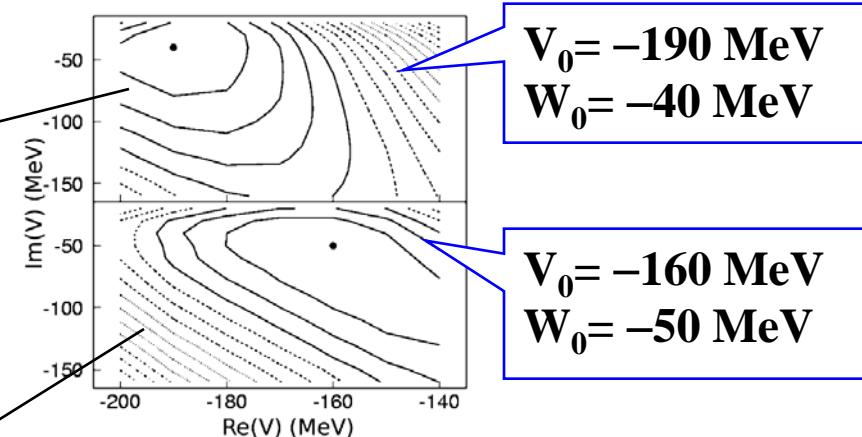
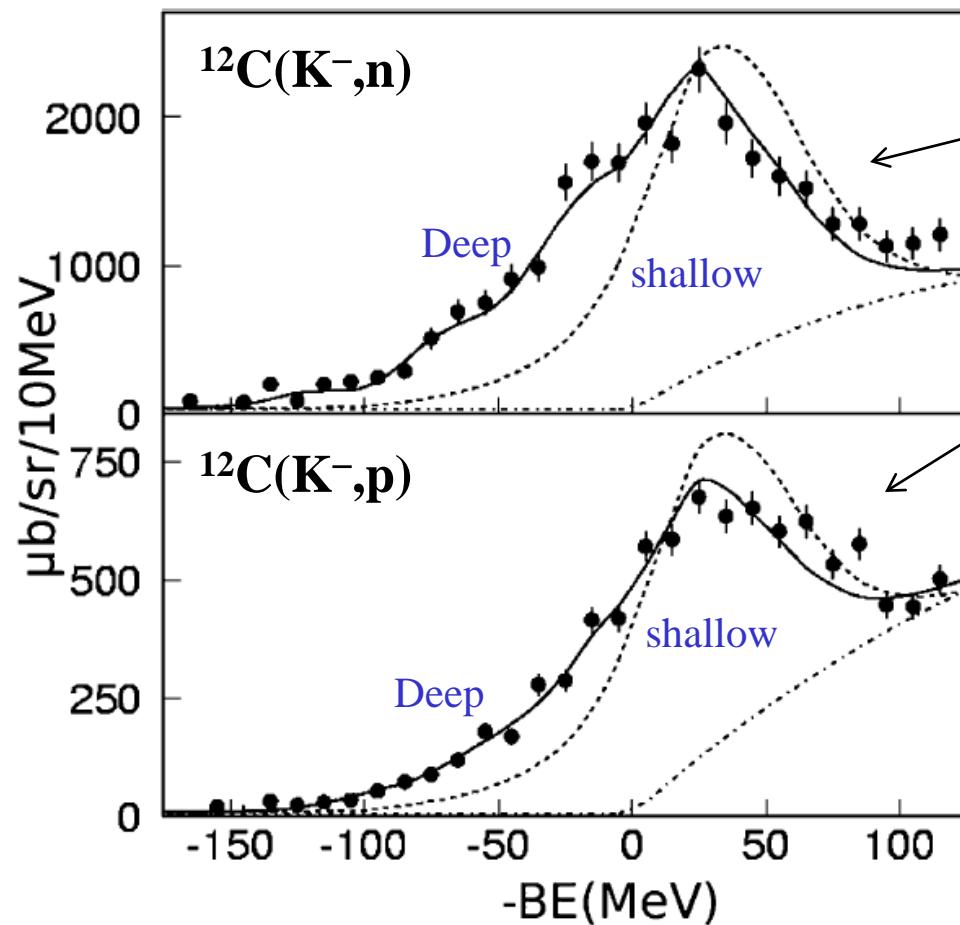
$K^{\bar{b}a{r}}$ 中間子原子核

- Low-energy $K^{\bar{b}a{r}}N$ interaction and Konic hydrogen
- $K^{\bar{b}a{r}}$ nuclear potentials: deep or shallow ?
 - Kaonic atoms
 - (K^-, N) reaction on ^{12}C and ^{16}O
- Deeply-bound kaonic state, $K^- pp$
 - Theoretical calculations
 - Experimental candidates
- $^3He(K^-, N)K^- pp$ reaction E15@J-PARC
- $d(\pi^+, K^+)K^- pp$ reaction E23@J-PARC

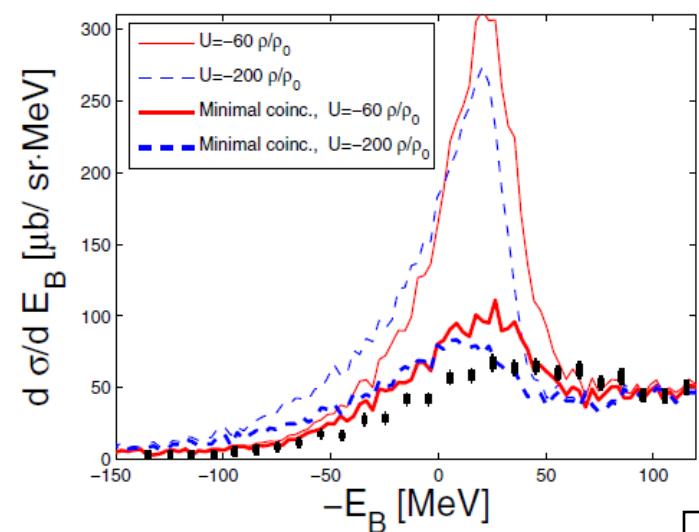
$K^{\bar{b}ar}$ -Nucleus Interaction studied through in-flight (K -, N) reactions

missing mass spectroscopy

T. Kishimoto et al., PTP118(2007)181

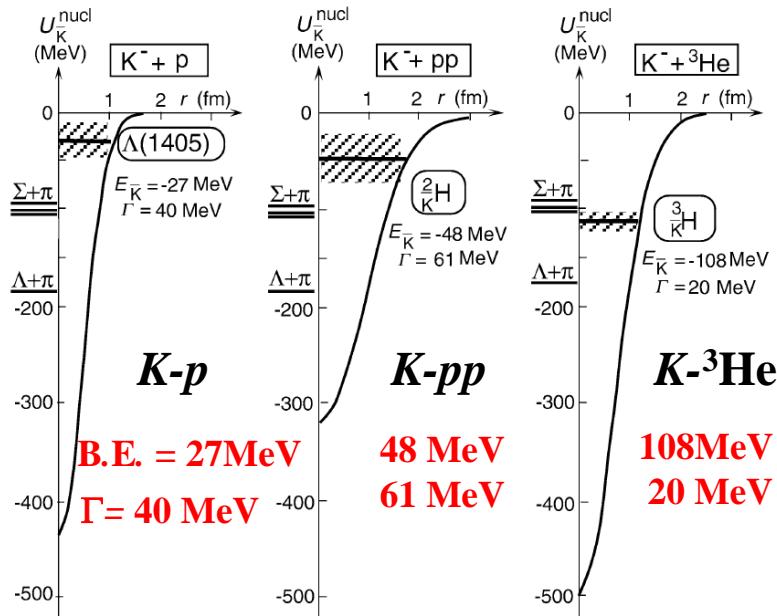


V. K. Magas et al, PRC81(2010)024609



Deep potentialの方が実験データとの一致がよい？

Theoretical prediction for deeply-bound antiKaonic nuclei



Few-body calculations predicted

T.Yamazaki,Y.Akaishi,PLB535(2002)70; PRC65(2002) 044005

- K^-p free scattering data
- (1s) level shifts in kaonic hydrogen atoms
- B.E. and Γ of $\Lambda(1405)=“K^-+p$ quasibound state”

$$V_{\bar{K}N}^{I=0} \quad \Lambda(1405) = "K^- p"$$

Strongly attractive

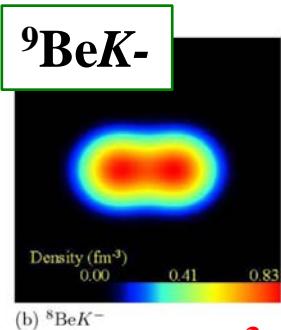
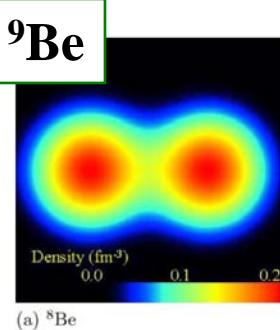
“Super strong nuclear force”

Yamazaki,Akaishi,PJAS. B82(2007)144

Exotic states of antiKaonic nuclei by AMD

A. Doté et al., PLB590(2004)51; PRC70(2004)044313.

AMD+G-matrix NN,KN(AY)

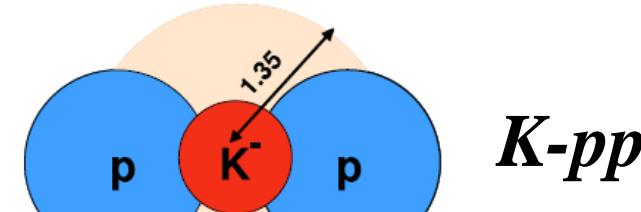


$$\rho_{AV} = 0.33 \text{ fm}^{-3}$$

$pppK^-$



$$0.66 \text{ fm}^{-3}$$



$$[\bar{K}_{1/2}^{0^-} \otimes \{N, N\}_1^{0^+}]_{I=1/2}^{J=0^-}$$

Essential antiKaonic nuclei

高密度ハドロン物質

Experimental Candidates for Deeply-Bound State K^-pp

2011.6

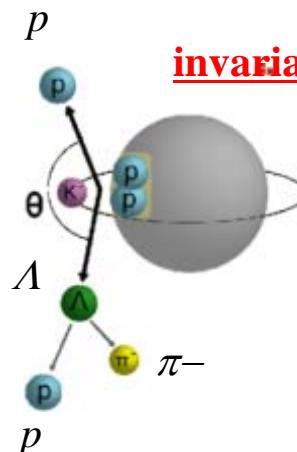
FINUDA Collaboration@DAΦNE

M. Agnello et al., PRL94(2005)212303

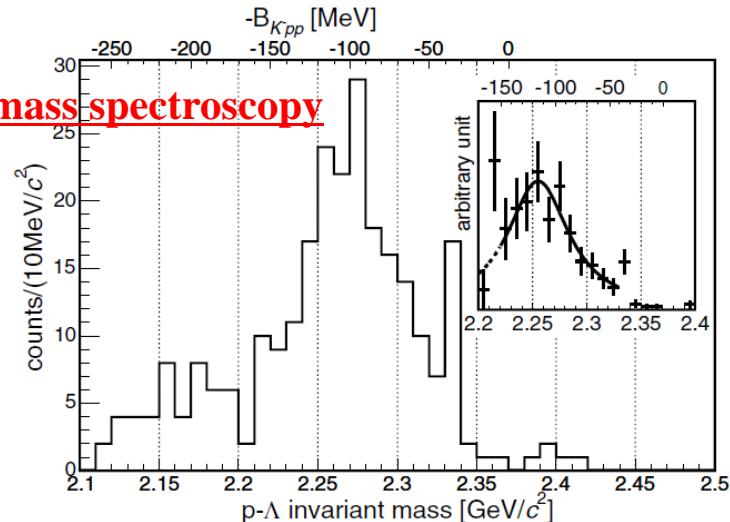
B.E. = 115 ± 9 MeV

$\Gamma = 67^{+16}_{-14}$ MeV

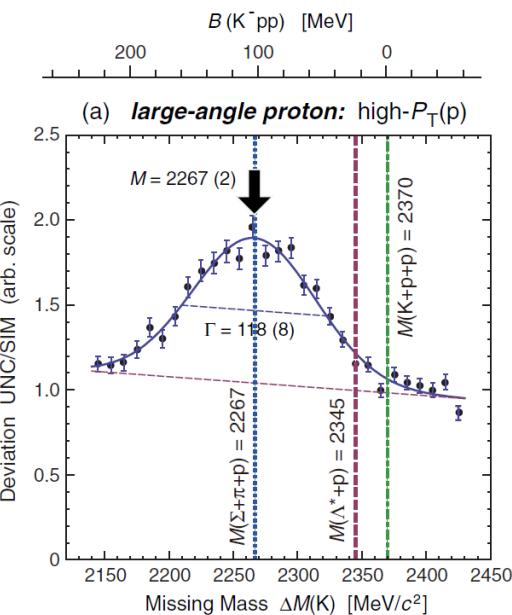
- K^- absorption on
6Li, 7Li, 12C, 27Al at Rest
- Λp invariant mass distrib.



invariant mass spectroscopy



DISTO Collaboration@SATURNE-Saclay



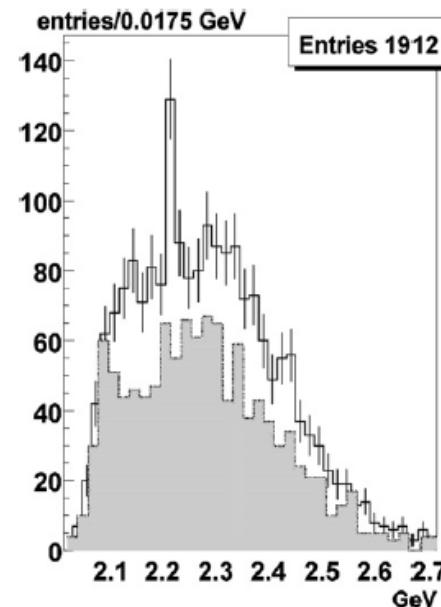
T.Yamazaki et al.,
PRL104(2010)132502

B.E. = $103 \pm 3 \pm 5$ MeV

$\Gamma = 118 \pm 8 \pm 10$ MeV

- $p+p \rightarrow K^+ + \Lambda + p$ at 2.85 GeV
- Λp invariant mass distrib.

OBELIX Collaboration@LEAR-CERN



G. Bendiscioli et al.,
NPA789(2007)222.

B.E. = 160.9 ± 4.9 MeV

$\Gamma < 24.4 \pm 8.0$ MeV

- anti p+4He at rest
- $p\pi^-p$ invariant mass distrib.

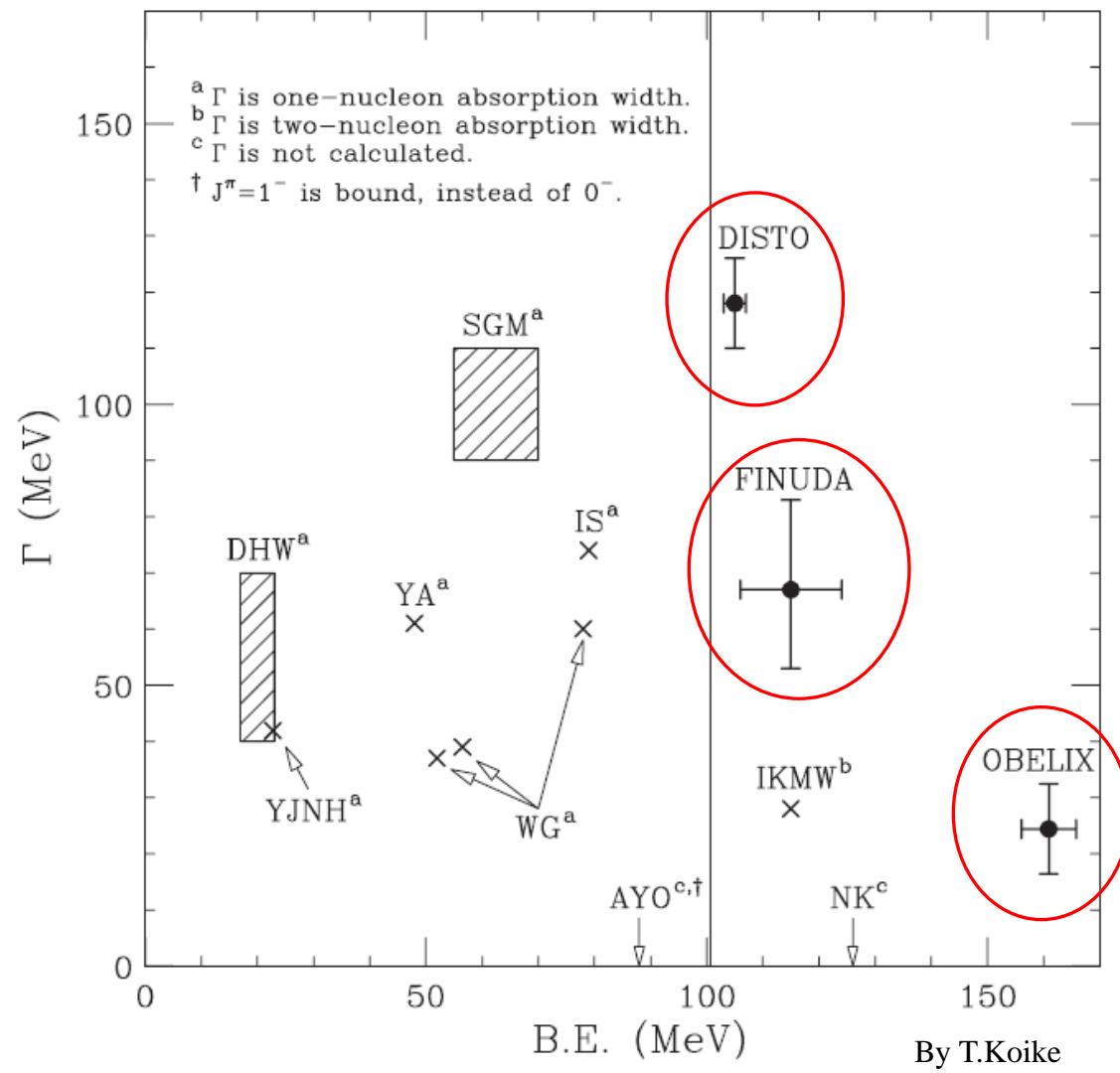
Theoretical predictions of deeply-bound K^-pp

$[I = \frac{1}{2}, J^\pi = 0^-]$

| | B.E. (MeV) | Γ_{mesonic} (MeV) |
|-----|---------------|------------------------------------|
| AY | 48 | 61 |
| DHW | 20 ± 3 | 40-70 |
| IS | 60-95 | 45-80 |
| SGM | 50-70 | 90-110 |
| WG | 40-80 | 40-85 |

Status

- すべての理論計算が準束縛状態の存在を示唆。幅は広い。
- B.E.と Γ の違いは $K^{\bar{N}}$ int. や 3 体系計算方法の違いによるもの？
- “ $\pi\Sigma N$ decay” チャンネル効果が必要



By T.Koike

$^3\text{He}(\text{K}^-, \text{n})\text{K-pp}$ spectrum at 1.0GeV/c (0deg)

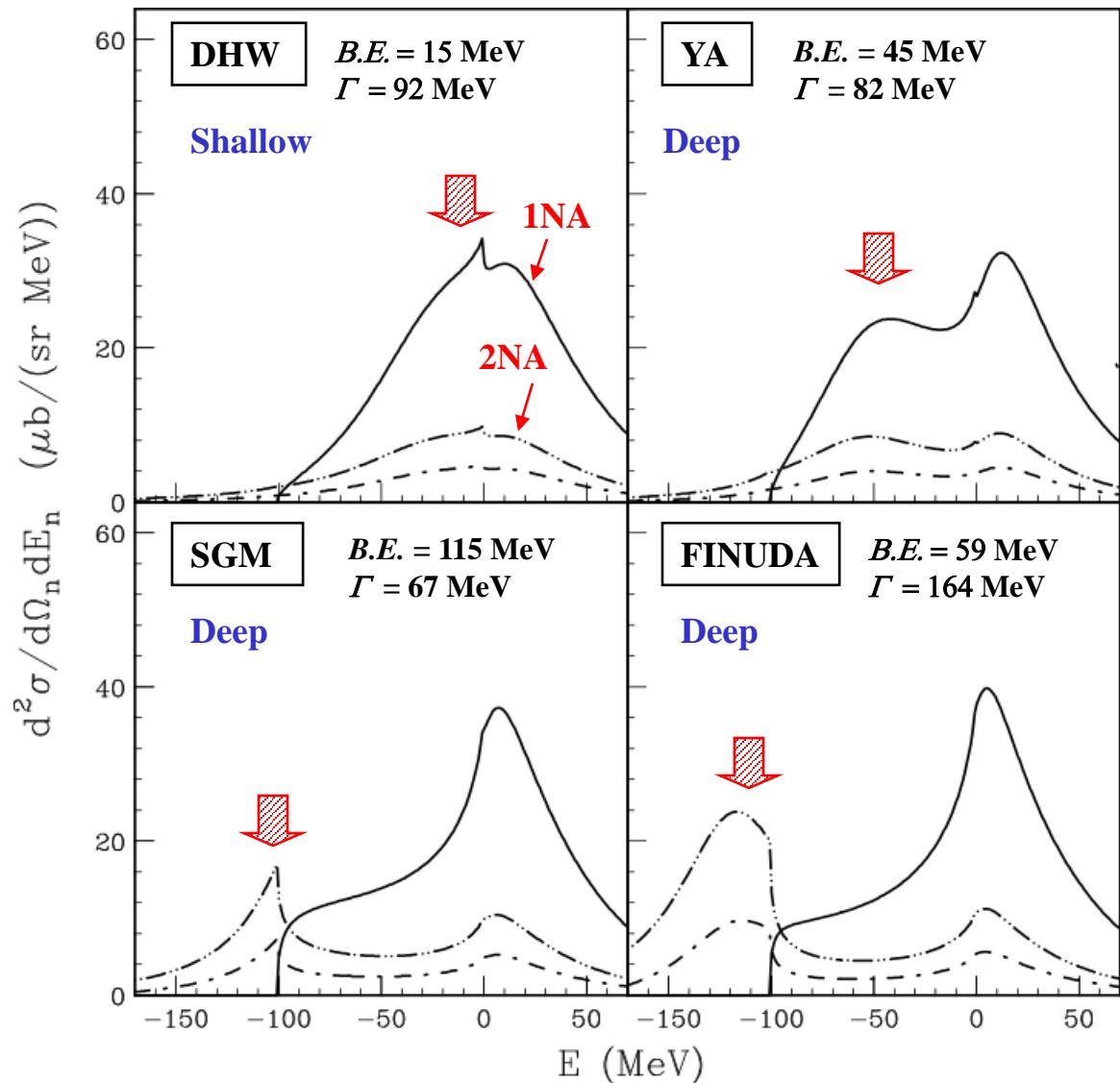
E15@J-PARC A search for deeply-bound kaonic nuclear states by in-flight
 $^3\text{He}(\text{K}^-, \text{n})$ reaction

missing mass spectroscopy +invariant mass spectroscopy

Integrated cross section
in the bound region
 $\sim 3.5 \text{ mb/sr}$ (for YA)

^3He 標的の優位性

- Distortion effects
$$\frac{D_{\text{dist}}[{}^3\text{He}(1s_N \rightarrow 1s_K)]}{D_{\text{dist}}[{}^{12}\text{C}(1p_N \rightarrow 1s_K)]} = 0.47 / 0.095 \rightarrow 5\text{倍}$$
- Recoil effects
 $M_C/M_A \sim 2/3 \rightarrow 1.8\text{倍}$
- Small-size effects
 $L=0$ 状態だけが束縛



Conclusion

Studies of
the production and spectroscopy of
strangeness nuclei are
very interesting and exciting
at J-PARC.

- ストレンジネスが拓く新しい状態の発見、”エキゾチック”な原子核
- バリオン-バリオン間相互作用の理解、短距離斥力の起源
- 高密度QCD物質の理解 → 中性子星の構造・進化の解明

Keyword

“Hyperon mixing”

Thank you very much.